

# Design of Digital Circuits

## Lecture 21: SIMD Processors II and Graphics Processing Units

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# New Course: Bachelor's Seminar in Comp Arch

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- Fall 2018
- 2 credit units
- **Rigorous seminar on fundamental and cutting-edge topics in computer architecture**
- Critical presentation, review, and discussion of seminal works in computer architecture
  - We will cover many ideas & issues, analyze their tradeoffs, perform critical thinking and brainstorming
- Participation, presentation, report and review writing
- Stay tuned for more information

# Agenda for Today & Next Few Lectures

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- Single-cycle Microarchitectures
- Multi-cycle and Microprogrammed Microarchitectures
- Pipelining
- Issues in Pipelining: Control & Data Dependence Handling, State Maintenance and Recovery, ...
- Out-of-Order Execution
- Other Execution Paradigms

# Readings for Today

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- Peleg and Weiser, “[MMX Technology Extension to the Intel Architecture](#),” IEEE Micro 1996.
- Lindholm et al., “[NVIDIA Tesla: A Unified Graphics and Computing Architecture](#),” IEEE Micro 2008.

# Other Approaches to Concurrency (or Instruction Level Parallelism)

# Approaches to (Instruction-Level) Concurrency

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- Pipelining
- Out-of-order execution
- Dataflow (at the ISA level)
- Superscalar Execution
- VLIW
- Fine-Grained Multithreading
- SIMD Processing (Vector and array processors, GPUs)
- Decoupled Access Execute
- Systolic Arrays

# SIMD Processing: Exploiting Regular (Data) Parallelism

# Recall: Flynn's Taxonomy of Computers

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- Mike Flynn, “**Very High-Speed Computing Systems**,” Proc. of IEEE, 1966
- **SISD**: Single instruction operates on single data element
- **SIMD**: Single instruction operates on multiple data elements
  - Array processor
  - Vector processor
- **MISD**: Multiple instructions operate on single data element
  - Closest form: systolic array processor, streaming processor
- **MIMD**: Multiple instructions operate on multiple data elements (multiple instruction streams)
  - Multiprocessor
  - Multithreaded processor

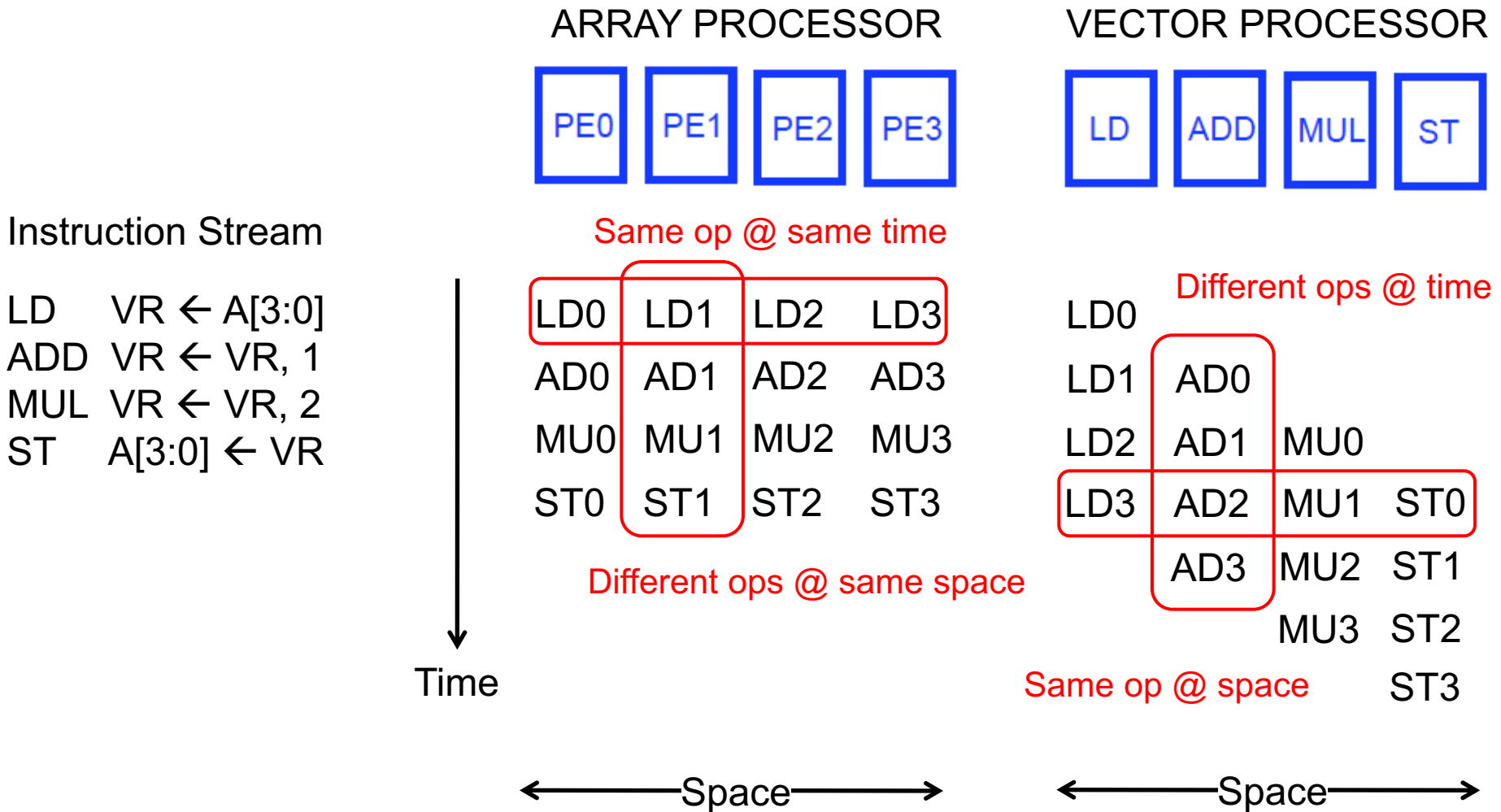


# Recall: SIMD Processing

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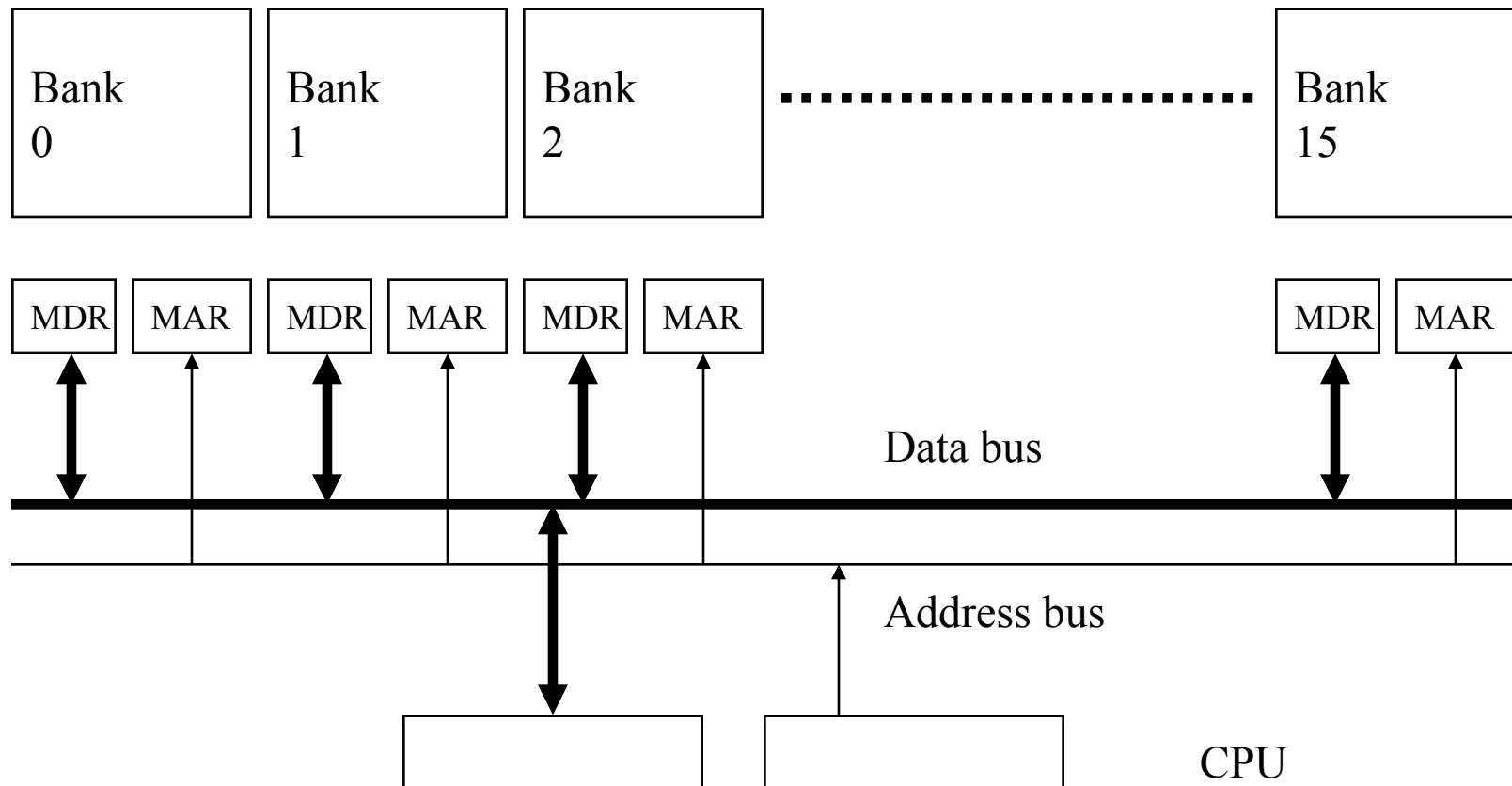
- Single instruction operates on multiple data elements
  - In time or in space
- Multiple processing elements
- Time-space duality
  - **Array processor**: Instruction operates on multiple data elements at the **same time** using **different spaces**
  - **Vector processor**: Instruction operates on multiple data elements in **consecutive time steps** using the **same space**

# Recall: Array vs. Vector Processors



# Recall: Memory Banking

- Memory is divided into **banks** that can be accessed independently; banks share address and data buses (to minimize pin cost)
- Can start and complete one bank access per cycle
- Can sustain N parallel accesses if all N go to different banks



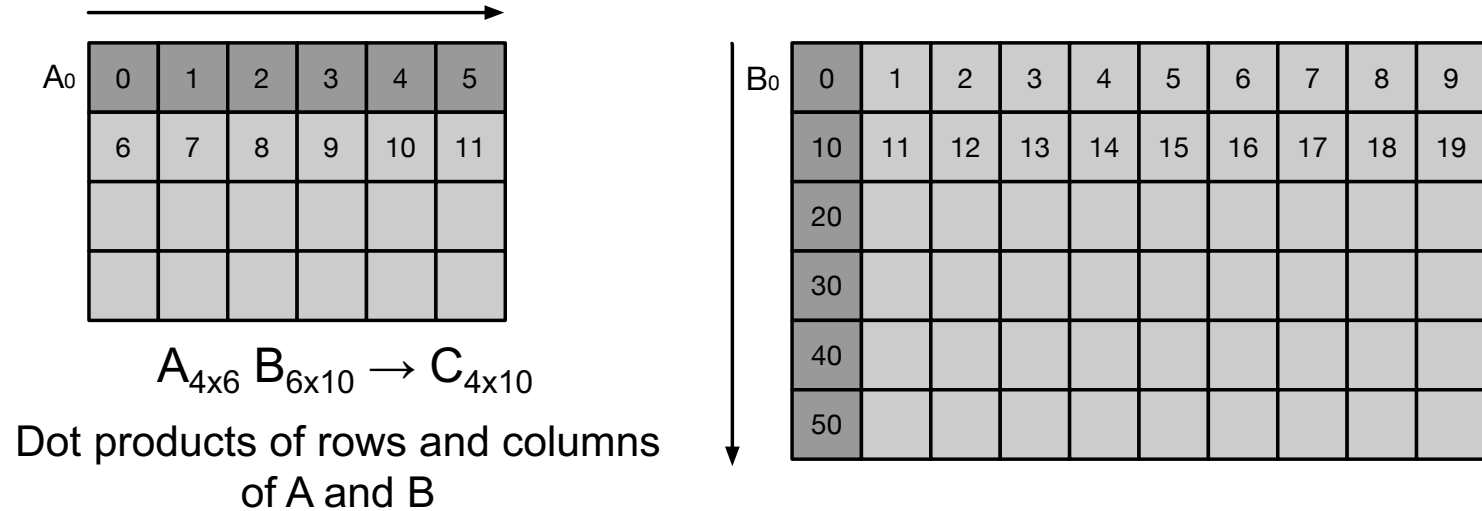
# Some Issues

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- Stride and banking
  - As long as they are *relatively prime* to each other and there are enough banks to cover bank access latency, we can sustain 1 element/cycle throughput
- Storage of a matrix
  - **Row major**: Consecutive elements in a row are laid out consecutively in memory
  - **Column major**: Consecutive elements in a column are laid out consecutively in memory
  - You need to change the stride when accessing a row versus column

# Matrix Multiplication

- A and B, both in **row-major order**



- A: Load A<sub>0</sub> into vector register V<sub>1</sub>
  - Each time, increment address by one to access the next column
  - Accesses have a **stride of 1**
- B: Load B<sub>0</sub> into vector register V<sub>2</sub>
  - Each time, increment address by 10
  - Accesses have a **stride of 10**

Different strides can lead to **bank conflicts**

How do we minimize them?

# Minimizing Bank Conflicts

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- More banks
- Better data layout to match the access pattern
  - Is this always possible?
- Better mapping of address to bank
  - E.g., randomized mapping
  - Rau, “Pseudo-randomly interleaved memory,” ISCA 1991.

# Recall: Questions (II)

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- What if vector data is not stored in a strided fashion in memory? (**irregular memory access to a vector**)
  - Idea: Use indirection to combine/pack elements into vector registers
  - Called scatter/gather operations

# Gather/Scatter Operations

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Want to vectorize loops with indirect accesses:

```
for (i=0; i<N; i++)  
    A[i] = B[i] + C[D[i]]
```

Indexed load instruction (*Gather*)

```
LV vD, rD          # Load indices in D vector  
LVI vC, rC, vD      # Load indirect from rC base  
LV vB, rB          # Load B vector  
ADDV.D vA, vB, vC   # Do add  
SV vA, rA          # Store result
```



# Gather/Scatter Operations

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- Gather/scatter operations often implemented in hardware to handle **sparse vectors (matrices)**
- Vector loads and stores use an index vector which is added to the base register to generate the addresses
- *Scatter* example

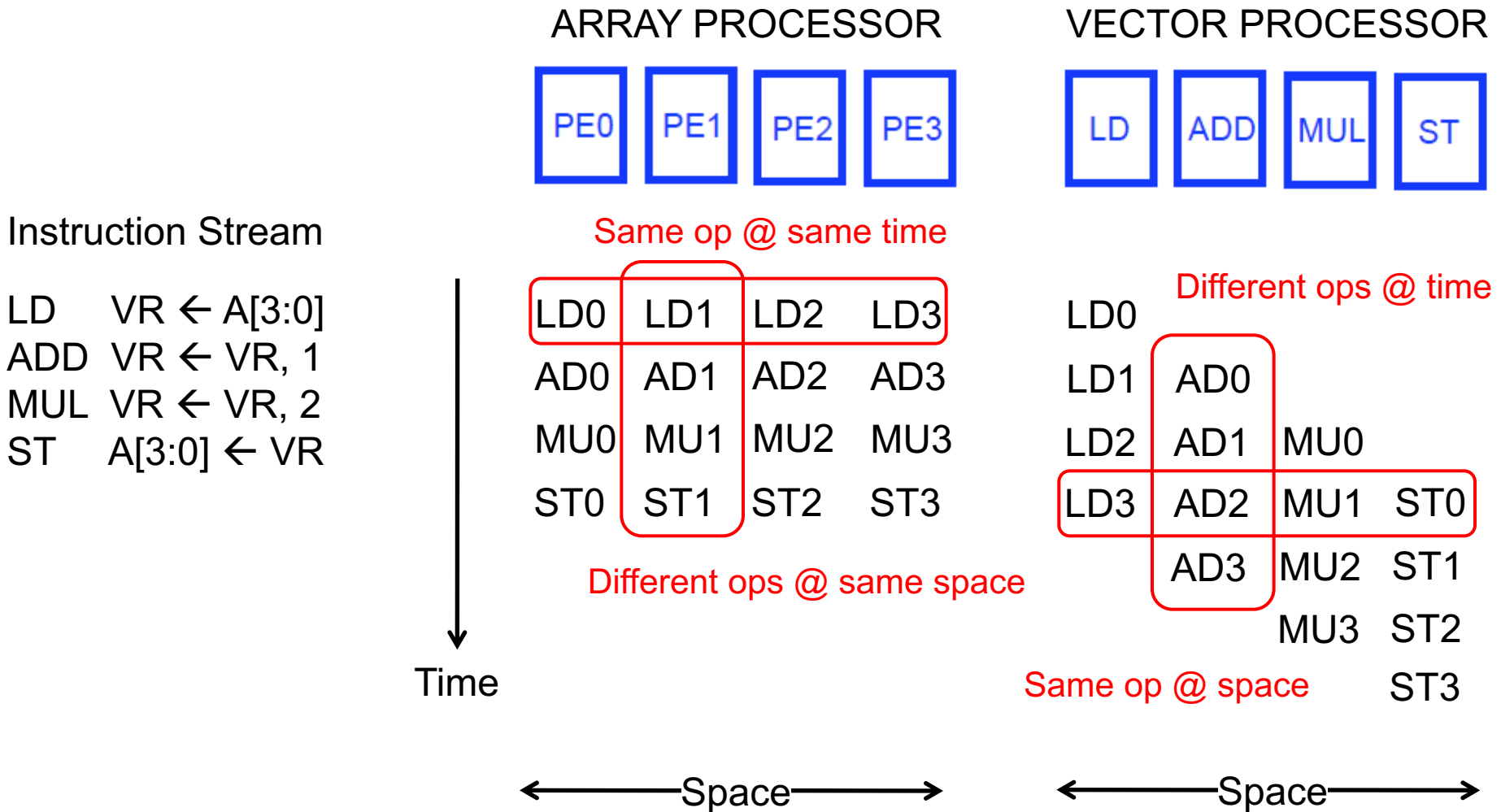
Index Vector	Data Vector (to Store)	Stored Vector (in Memory)	
0	3.14	Base+0	3.14
2	6.5	Base+1	X
6	71.2	Base+2	6.5
7	2.71	Base+3	X
		Base+4	X
		Base+5	X
		Base+6	71.2
		Base+7	2.71

# Array vs. Vector Processors, Revisited

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- Array vs. vector processor distinction is a “purist’s” distinction
- Most “modern” SIMD processors are a combination of both
  - They exploit data parallelism in both time and space
  - GPUs are a prime example we will cover in a bit more detail

# Recall: Array vs. Vector Processors

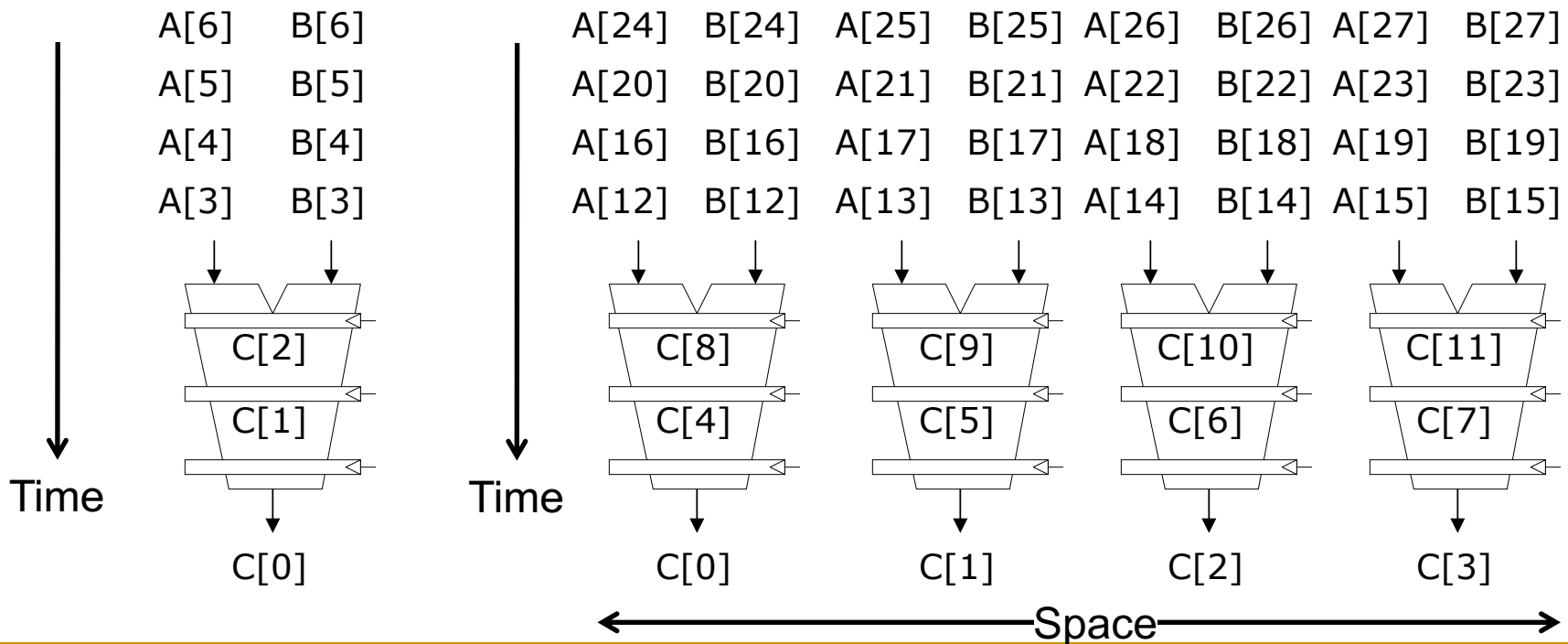


# Vector Instruction Execution

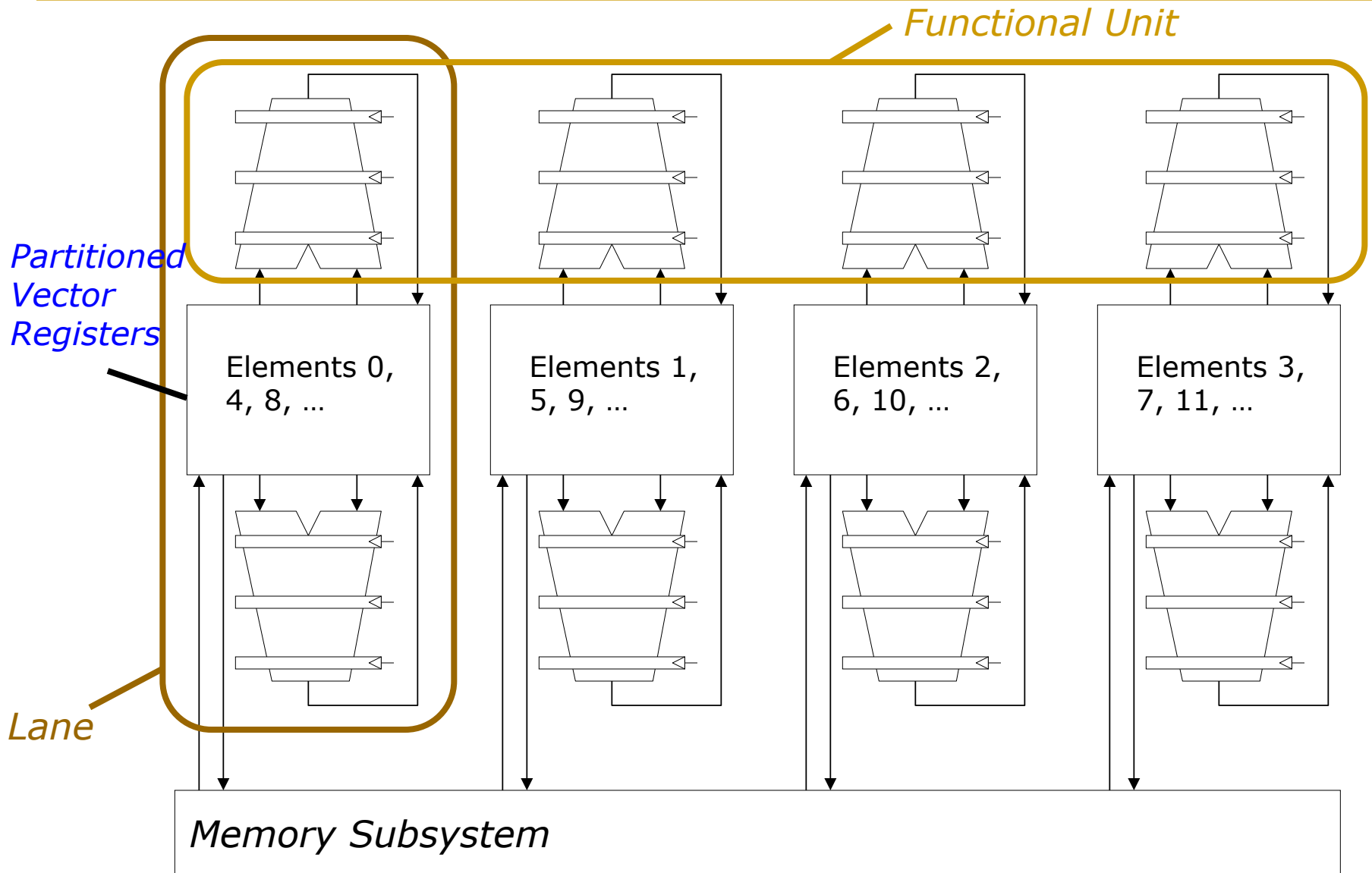
VADD A,B → C

*Execution using  
one pipelined  
functional unit*

*Execution using  
four pipelined  
functional units*



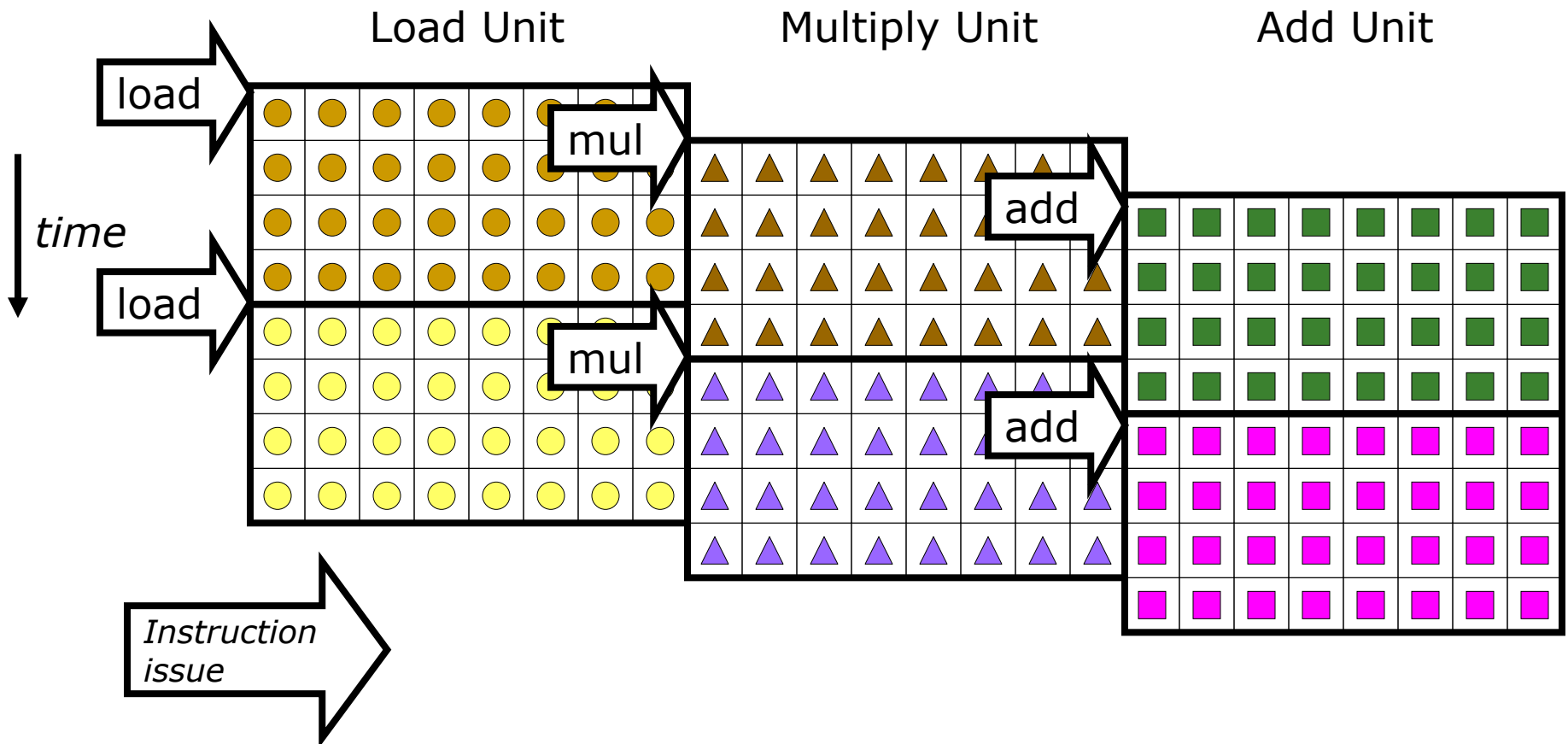
# Vector Unit Structure



# Vector Instruction Level Parallelism

Can overlap execution of multiple vector instructions

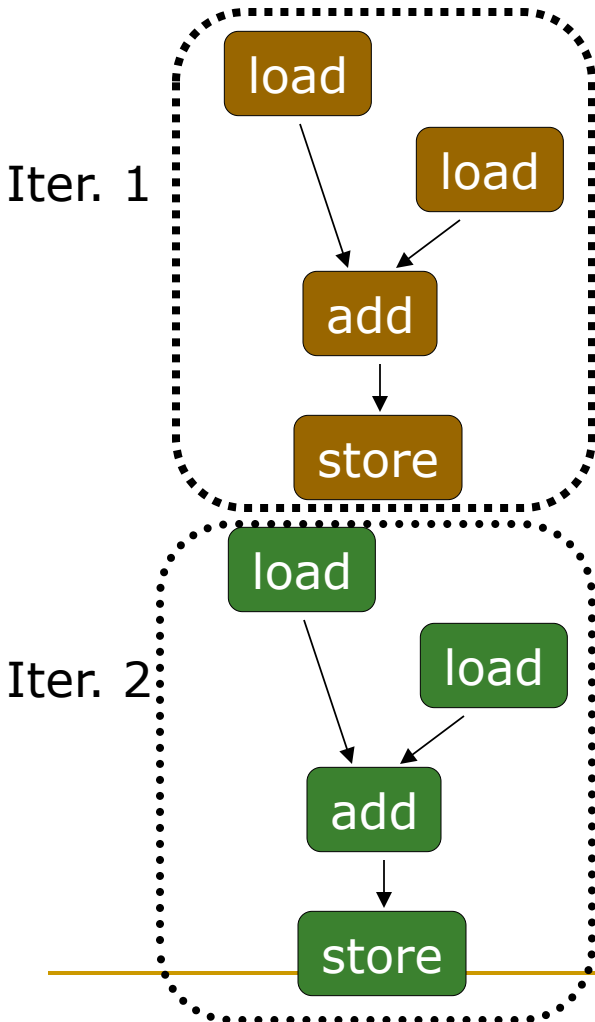
- Example machine has 32 elements per vector register and 8 lanes
- Completes 24 operations/cycle while issuing 1 vector instruction/cycle



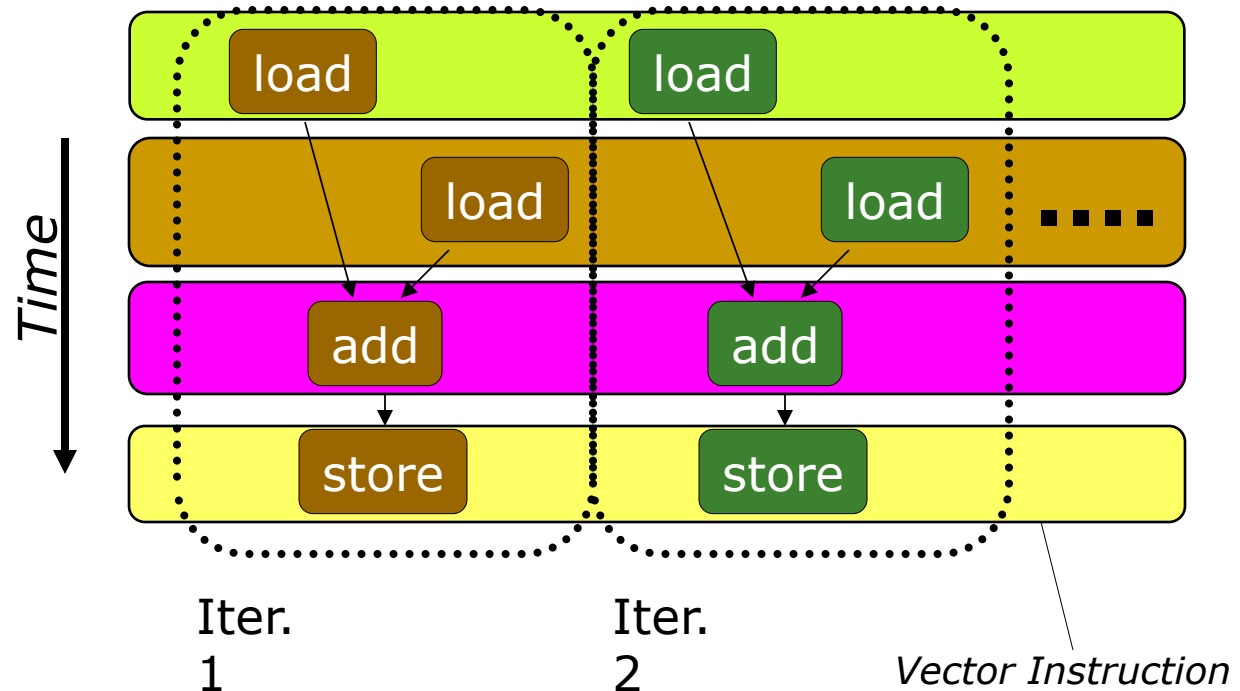
# Automatic Code Vectorization

```
for (i=0; i < N; i++)  
  C[i] = A[i] + B[i];
```

*Scalar Sequential Code*



*Vectorized Code*



Vectorization is a compile-time reordering of operation sequencing  
⇒ requires extensive loop dependence analysis

# Vector/SIMD Processing Summary

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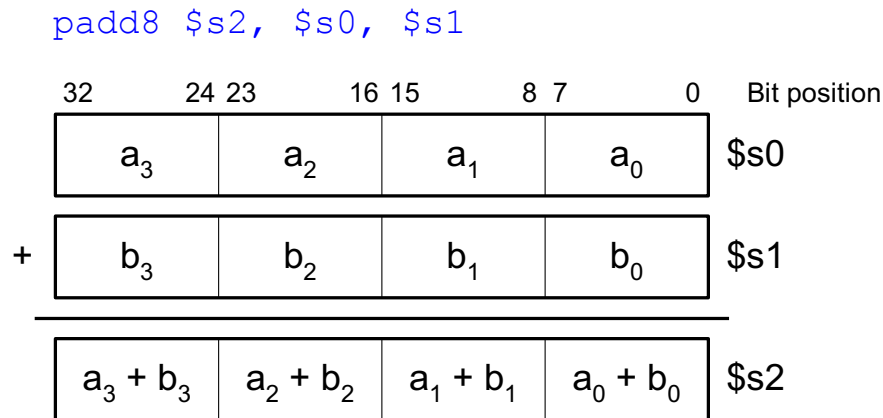
- Vector/SIMD machines are good at exploiting **regular data-level parallelism**
  - ❑ Same operation performed on many data elements
  - ❑ Improve performance, simplify design (no intra-vector dependencies)
- **Performance improvement limited by vectorizability** of code
  - ❑ Scalar operations limit vector machine performance
  - ❑ Remember **Amdahl's Law**
  - ❑ CRAY-1 was the fastest SCALAR machine at its time!
- Many existing ISAs include (vector-like) SIMD operations
  - ❑ Intel MMX/SSEn/AVX, PowerPC AltiVec, ARM Advanced SIMD



# SIMD Operations in Modern ISAs

# SIMD ISA Extensions

- Single Instruction Multiple Data (SIMD) extension instructions
  - Single instruction acts on multiple pieces of data at once
  - Common application: graphics
  - Perform short arithmetic operations (also called *packed arithmetic*)
- For example: add four 8-bit numbers
- Must modify ALU to eliminate carries between 8-bit values



# Intel Pentium MMX Operations

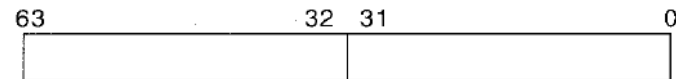
- Idea: One instruction operates on multiple data elements **simultaneously**
  - ❑ *A la* array processing (yet much more limited)
  - ❑ Designed with multimedia (graphics) operations in mind



(a)



(b)



(c)



(d)

No VLEN register

**Opcode** determines data type:

8 8-bit bytes

4 16-bit words

2 32-bit doublewords

1 64-bit quadword

**Stride** is always equal to 1.

Peleg and Weiser, “**MMX Technology Extension to the Intel Architecture**,”  
IEEE Micro, 1996.

Figure 1. MMX technology data types: packed byte (a), packed word (b), packed doubleword (c), and quadword (d).

# MMX Example: Image Overlaying (I)

- Goal: Overlay the human in image 1 on top of the background in image 2



Figure 8. Chroma keying: image overlay using a background color.

```
for (i=0; i<image_size; i++) {
    if (x[i] == Blue) new_image[i] = y[i];
    else new_image[i] = x[i];
}
```

PCMPEQB MM1, MM3

MM1	Blue	Blue	Blue	Blue	Blue	Blue	Blue	Blue
MM3	X7!=blue	X6!=blue	X5=blue	X4=blue	X3!=blue	X2!=blue	X1=blue	X0=blue
MM1	0x0000	0x0000	0xFFFF	0xFFFF	0x0000	0x0000	0xFFFF	0xFFFF



Bitmask

Figure 9. Generating the selection bit mask.

# MMX Example: Image Overlaying (II)

PAND MM4, MM1

Y = Blossom image

PANDN MM1, MM3

X = Woman's image

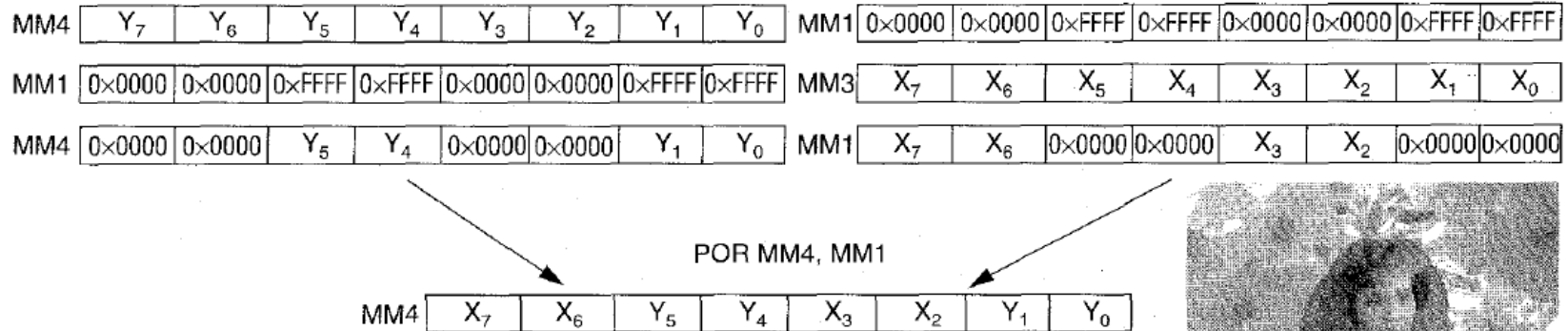


Figure 10. Using the mask with logical MMX instructions to perform a conditional select.

```

Movq    mm3, mem1    /* Load eight pixels from
                      woman's image
Movq    mm4, mem2    /* Load eight pixels from the
                      blossom image
Pcmpeqb mm1, mm3
Pand    mm4, mm1
Pandn   mm1, mm3
Por     mm4, mm1
    
```

Figure 11. MMX code sequence for performing a conditional select.

# GPUs (Graphics Processing Units)

# GPUs are SIMD Engines Underneath

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- The **instruction pipeline operates like a SIMD pipeline** (e.g., an array processor)
- However, the **programming is done using threads**, NOT SIMD instructions
- To understand this, let's go back to our parallelizable code example
- But, before that, let's distinguish between
  - **Programming Model (Software)**
  - vs.
  - **Execution Model (Hardware)**

# Programming Model vs. Hardware Execution Model

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- Programming Model refers to **how the programmer expresses the code**
  - E.g., Sequential (von Neumann), Data Parallel (SIMD), Dataflow, Multi-threaded (MIMD, SPMD), ...
- Execution Model refers to **how the hardware executes the code underneath**
  - E.g., Out-of-order execution, Vector processor, Array processor, Dataflow processor, Multiprocessor, Multithreaded processor, ...
- **Execution Model can be very different from the Programming Model**
  - E.g., von Neumann model implemented by an OoO processor
  - E.g., SPMD model implemented by a SIMD processor (a GPU)

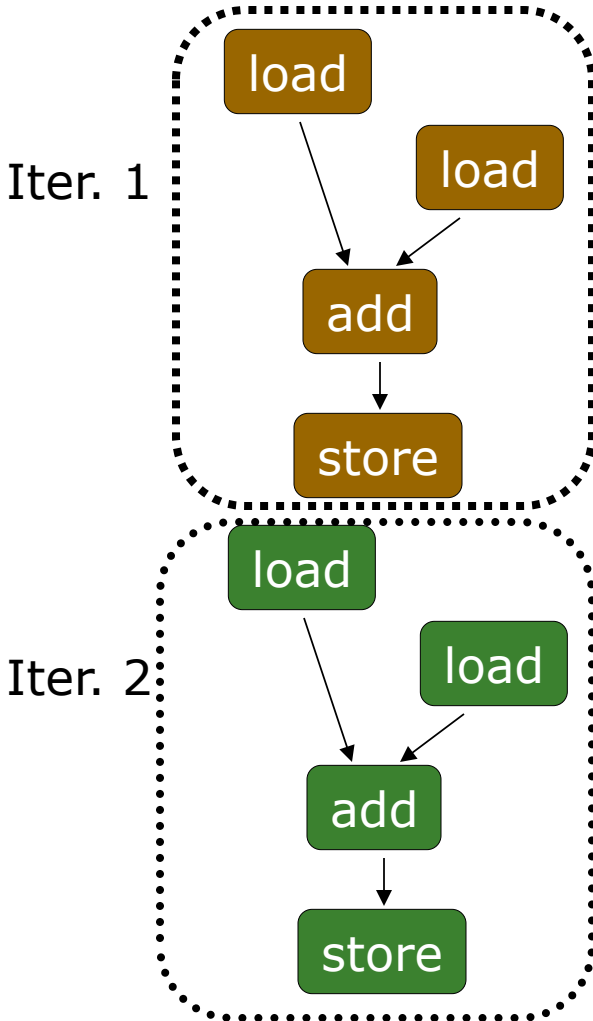


# How Can You Exploit Parallelism Here?

```
for (i=0; i < N; i++)
```

*Scalar Sequential Code*

```
C[i] = A[i] + B[i];
```



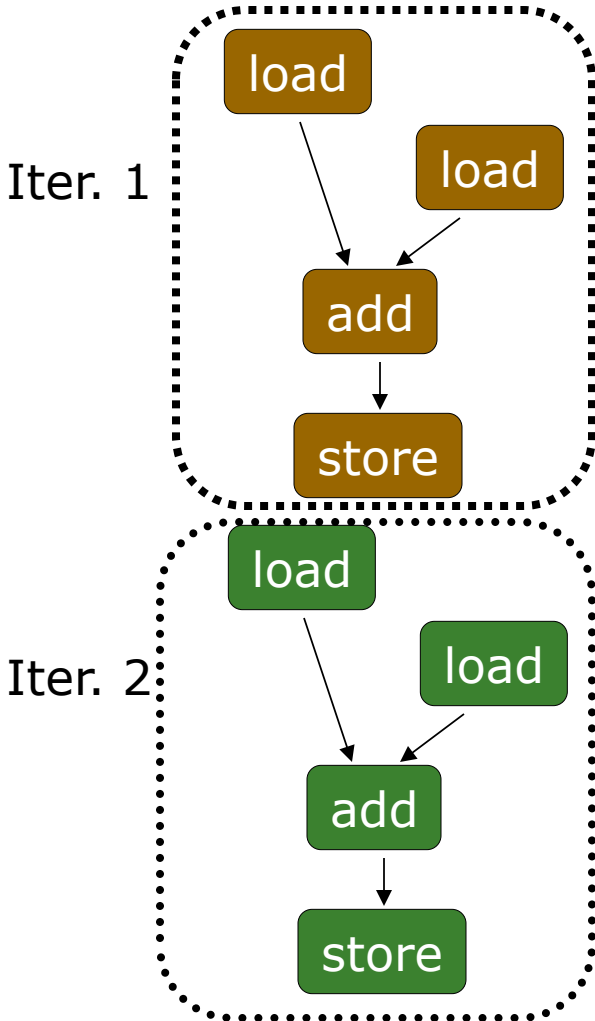
Let's examine three programming options to exploit instruction-level parallelism present in this sequential code:

1. Sequential (SISD)
2. Data-Parallel (SIMD)
3. Multithreaded (MIMD/SPMD)

# Prog. Model 1: Sequential (SISD)

```
for (i=0; i < N; i++)  
    C[i] = A[i] + B[i];
```

## Scalar Sequential Code



- Can be executed on a:
  - Pipelined processor
  - Out-of-order execution processor
    - ❑ Independent instructions executed when ready
    - ❑ Different iterations are present in the instruction window and can execute in parallel in multiple functional units
    - ❑ In other words, the loop is dynamically unrolled by the hardware
  - Superscalar or VLIW processor
    - ❑ Can fetch and execute multiple instructions per cycle

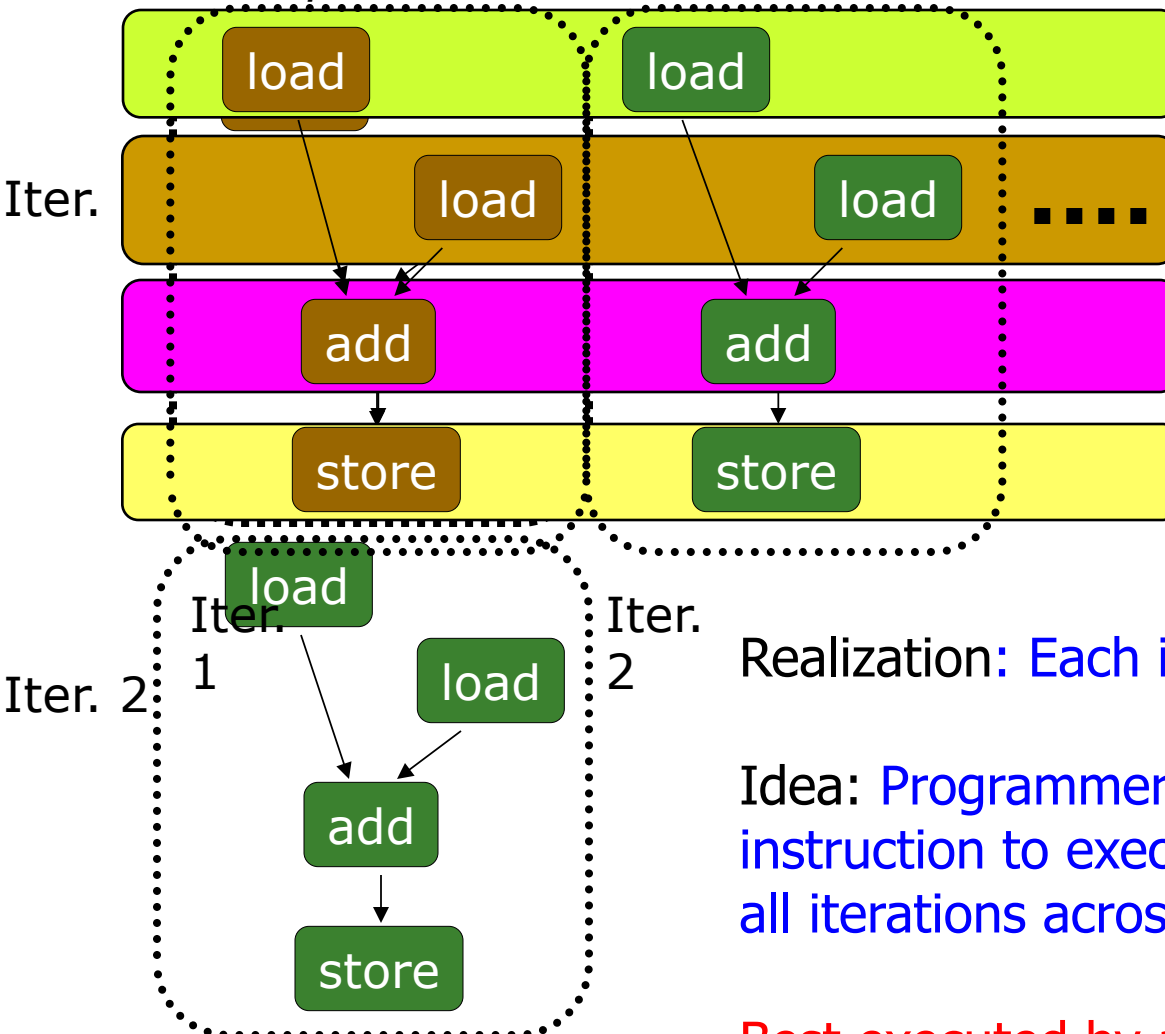
# Prog. Model 2: Data Parallel (SIMD)

```
for (i=0; i < N; i++)  
    C[i] = A[i] + B[i];
```

Scalar Sequential Code

Vector Instruction

Vectorized Code



Realization: Each iteration is independent

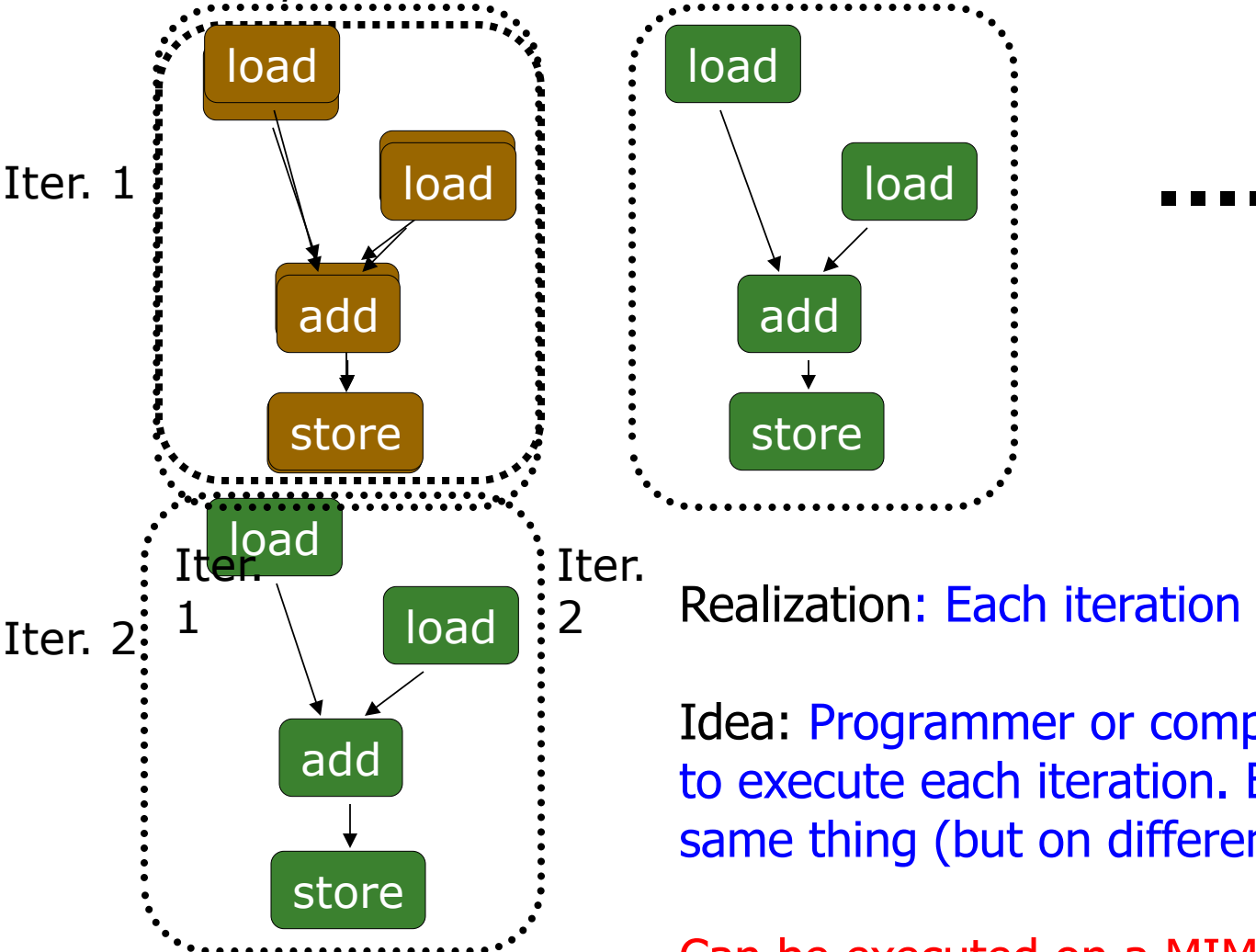
Idea: Programmer or compiler generates a SIMD instruction to execute the same instruction from all iterations across different data

Best executed by a SIMD processor (vector, array)

# Prog. Model 3: Multithreaded

```
for (i=0; i < N; i++)  
  C[i] = A[i] + B[i];
```

## Scalar Sequential Code



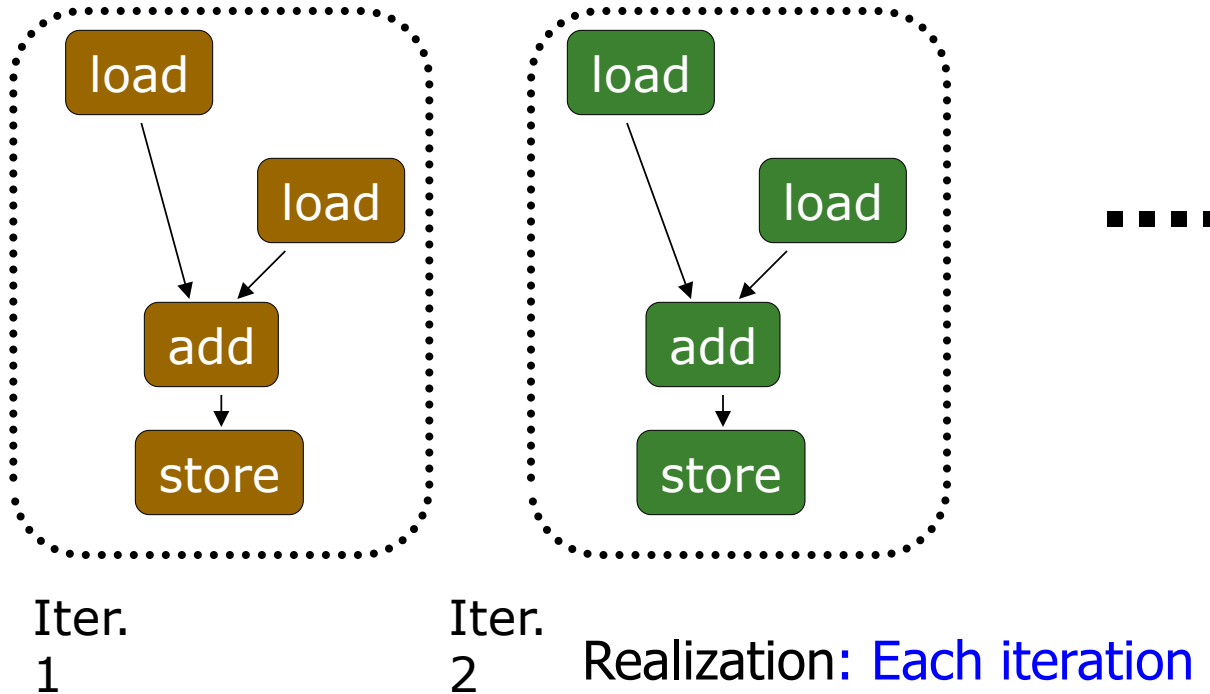
Realization: Each iteration is independent

Idea: Programmer or compiler generates a thread to execute each iteration. Each thread does the same thing (but on different data)

Can be executed on a MIMD machine

# Prog. Model 3: Multithreaded

```
for (i=0; i < N; i++)  
  C[i] = A[i] + B[i];
```



Realization: Each iteration is independent

This particular model is also called:

**SPMD: Single Program Multiple Data**

Can be executed on a SIMT machine

**Single Instruction Multiple Thread**

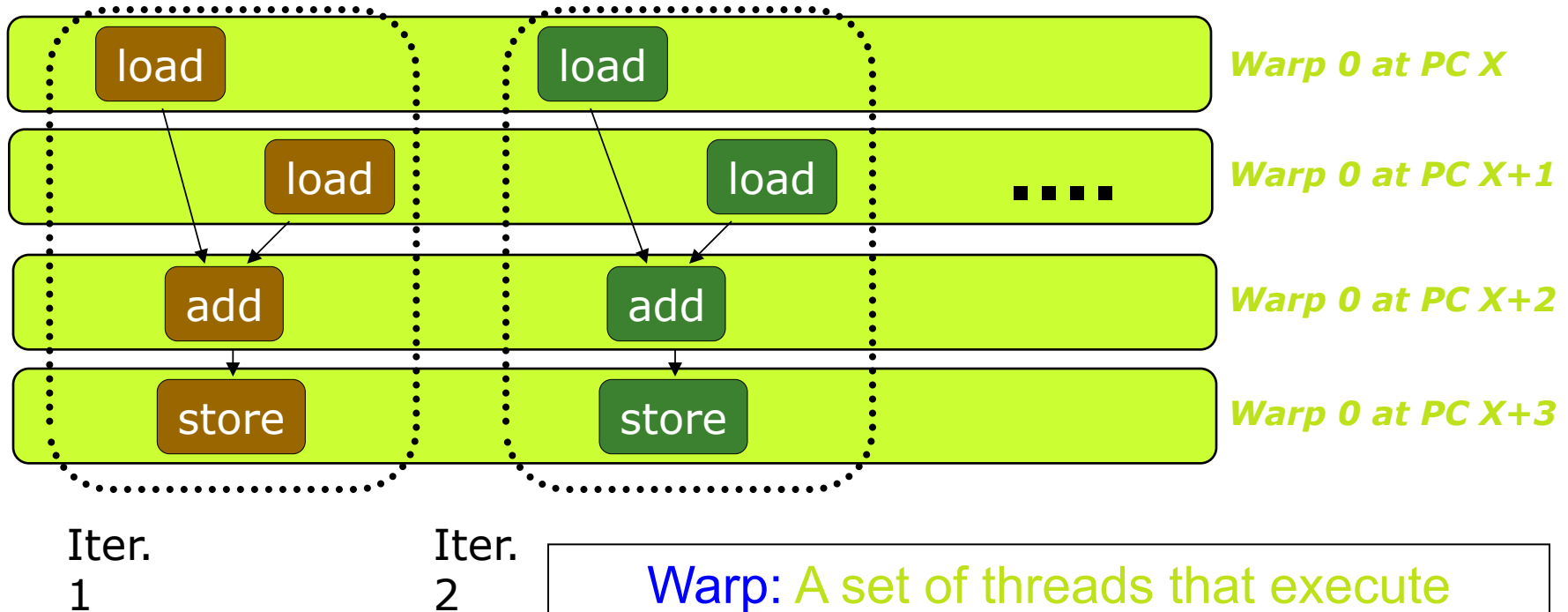
# A GPU is a SIMD (SIMT) Machine

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- Except it is **not** programmed using SIMD instructions
- It is **programmed using threads** (SPMD programming model)
  - Each thread executes the same code but operates a different piece of data
  - Each thread has its own context (i.e., can be treated/restarted/executed independently)
- A set of threads executing the same instruction are dynamically grouped into a **warp (wavefront)** by the hardware
  - A warp is essentially a **SIMD operation formed by hardware!**

# SPMD on SIMT Machine

```
for (i=0; i < N; i++)
    C[i] = A[i] + B[i];
```



**Warp:** A set of threads that execute the same instruction (i.e., at the same PC)

This particular model is also called:

## SPMD: Single Program Multiple Data

A GPU executes it using the SIMT model:  
Single Instruction Multiple Thread

# Graphics Processing Units

SIMD not Exposed to Programmer (SIMT)



# SIMD vs. SIMT Execution Model

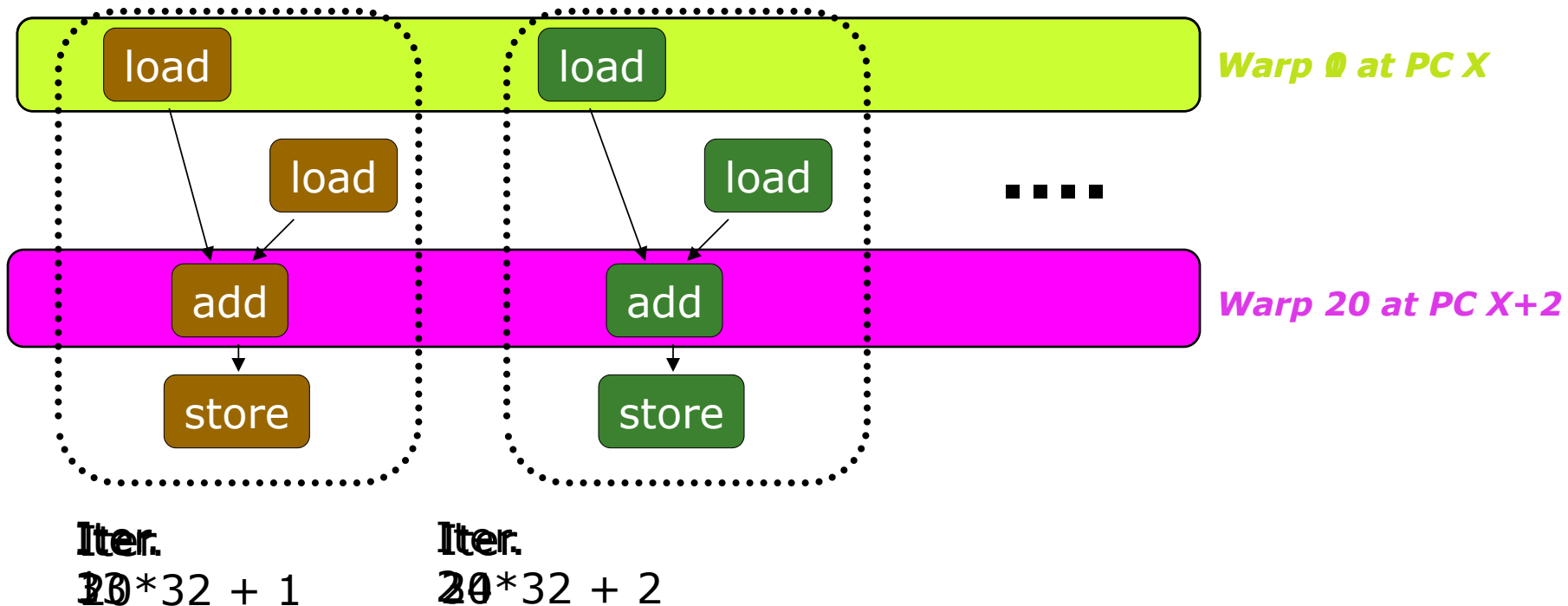
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- SIMD: A single sequential instruction stream of SIMD instructions → each instruction specifies multiple data inputs
  - [VLD, VLD, VADD, VST], VLEN
- SIMT: Multiple instruction streams of scalar instructions → threads grouped dynamically into warps
  - [LD, LD, ADD, ST], NumThreads
- Two Major SIMT Advantages:
  - Can treat each thread separately → i.e., can execute each thread independently (on any type of scalar pipeline) → MIMD processing
  - Can group threads into warps flexibly → i.e., can group threads that are supposed to *truly* execute the same instruction → dynamically obtain and maximize benefits of SIMD processing

# Multithreading of Warps

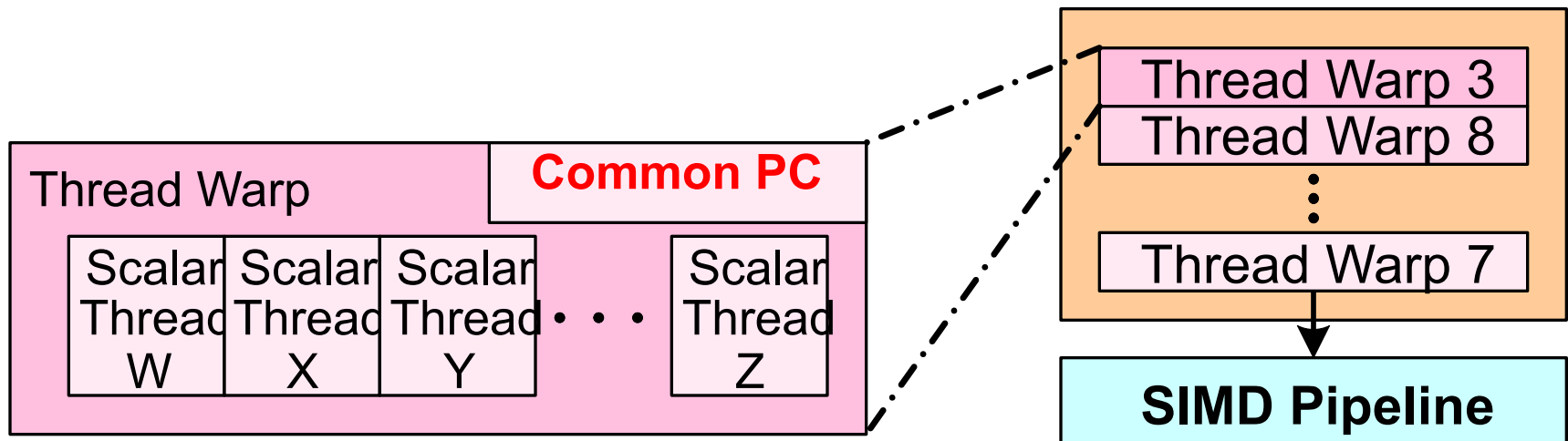
```
for (i=0; i < N; i++)  
    C[i] = A[i] + B[i];
```

- Assume a warp consists of 32 threads
- If you have 32K iterations, and 1 iteration/thread  $\rightarrow$  1K warps
- Warps can be interleaved on the same pipeline  $\rightarrow$  Fine grained multithreading of warps

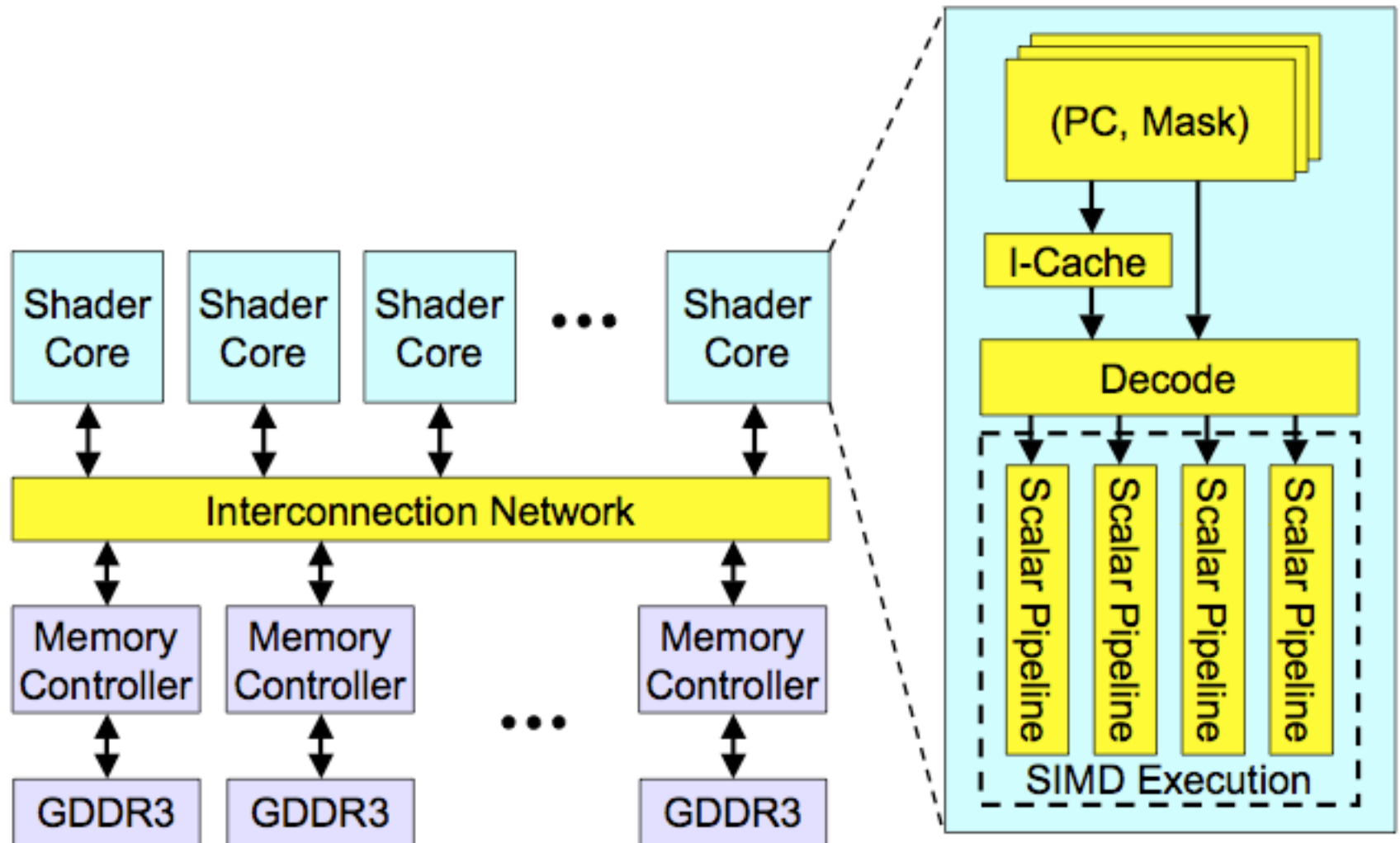


# Warps and Warp-Level FGMT

- Warp: A set of threads that execute the same instruction (on different data elements) → SIMT (Nvidia-speak)
- All threads run the same code
- Warp: The threads that run lengthwise in a woven fabric ...

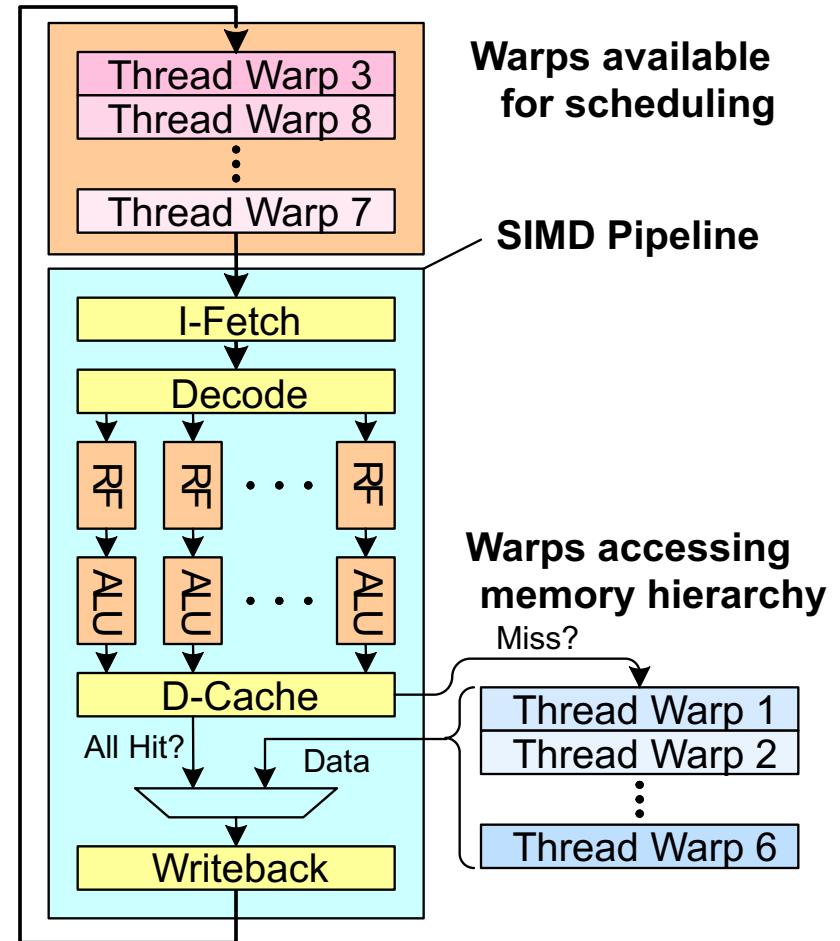


# High-Level View of a GPU



# Latency Hiding via Warp-Level FGMT

- Warp: A set of threads that execute the same instruction (on different data elements)
- Fine-grained multithreading
  - One instruction per thread in pipeline at a time (No interlocking)
  - Interleave warp execution to hide latencies
- Register values of all threads stay in register file
- FGMT enables long latency tolerance
  - Millions of pixels

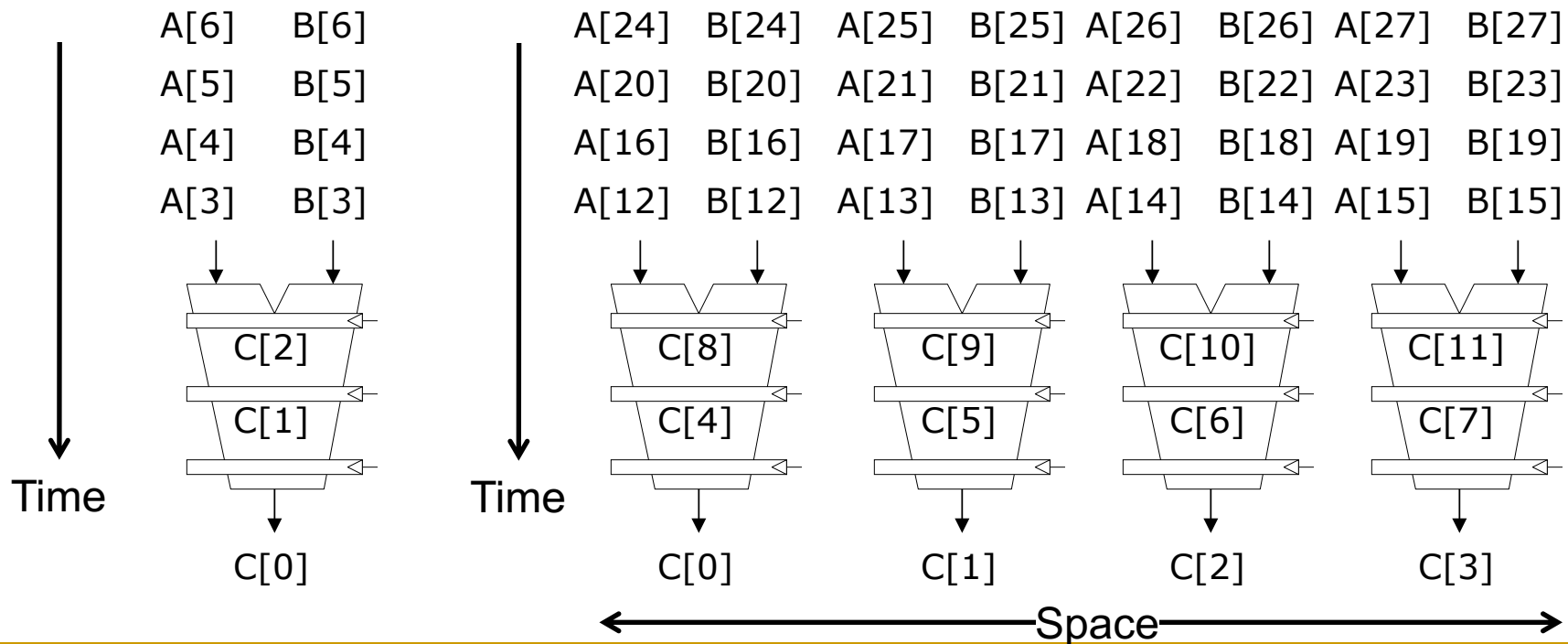


# Warp Execution (Recall the Slide)

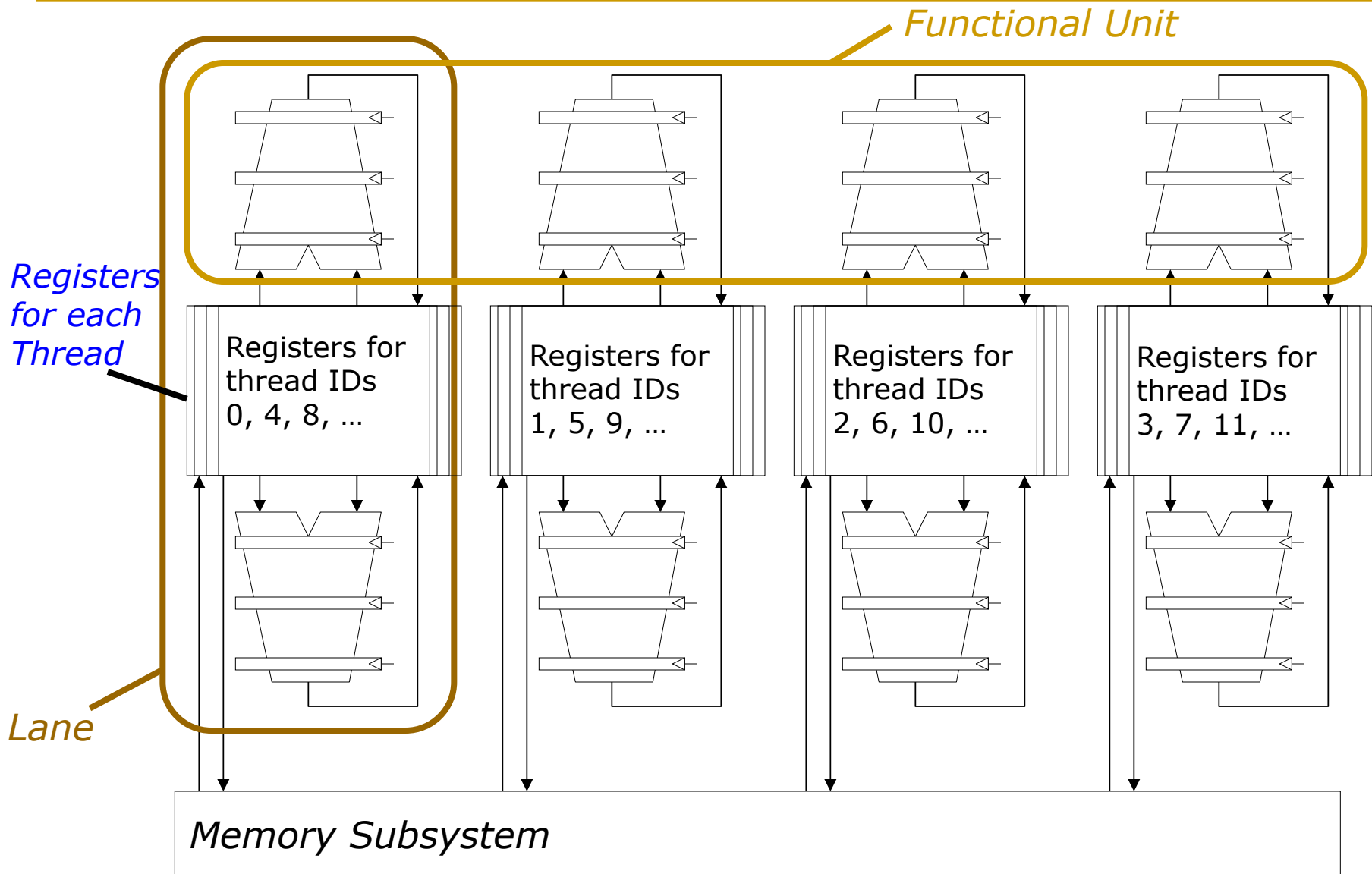
32-thread warp executing  $\text{ADD } A[\text{tid}], B[\text{tid}] \rightarrow C[\text{tid}]$

*Execution using  
one pipelined  
functional unit*

*Execution using  
four pipelined  
functional units*



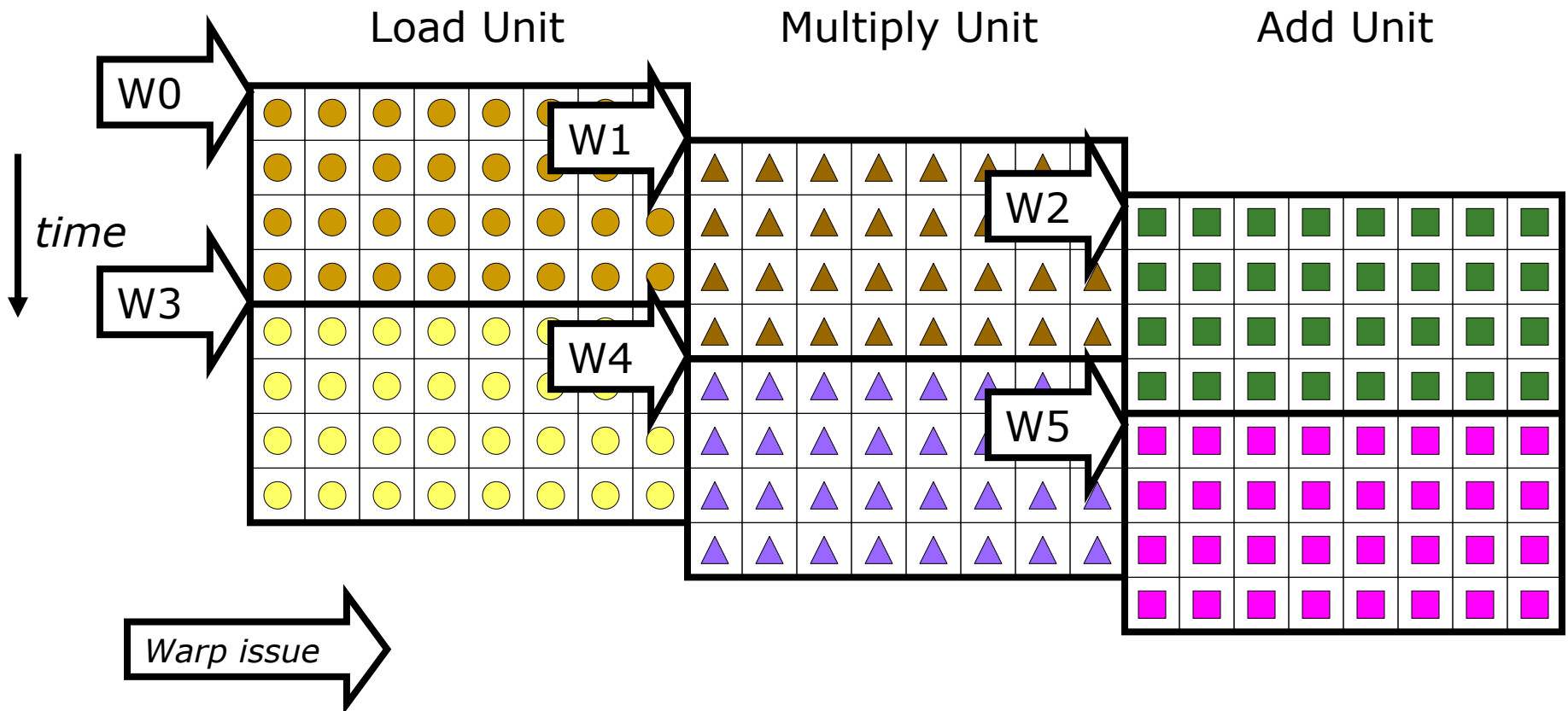
# SIMD Execution Unit Structure



# Warp Instruction Level Parallelism

Can overlap execution of multiple instructions

- Example machine has 32 threads per warp and 8 lanes
- Completes 24 operations/cycle while issuing 1 warp/cycle

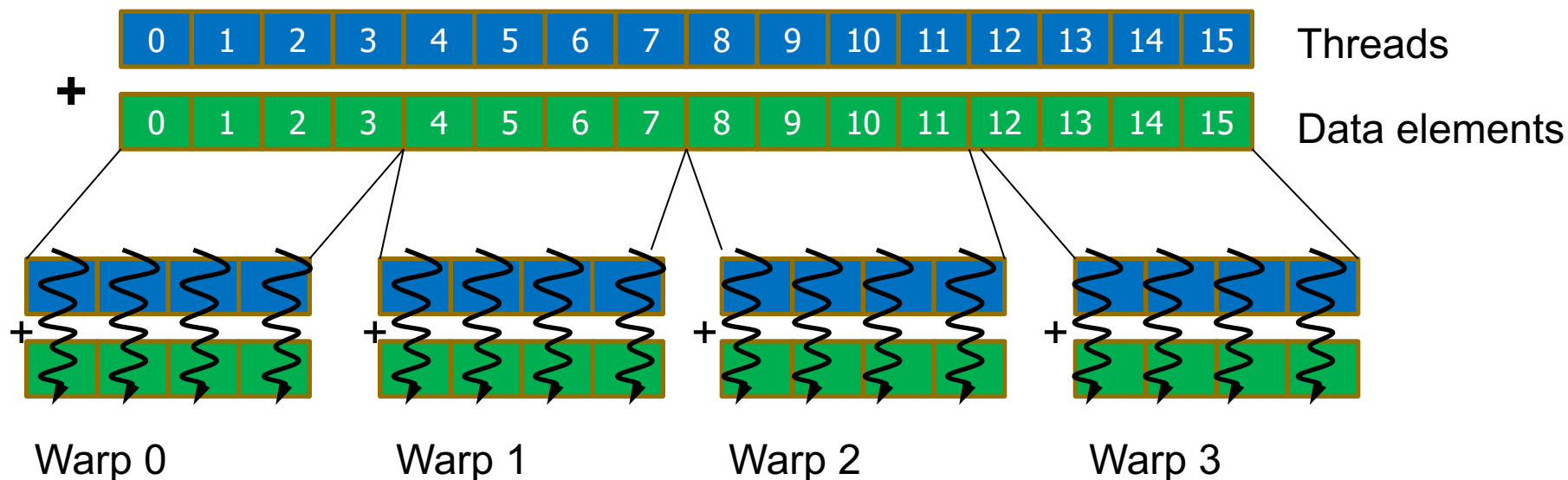




# SIMT Memory Access

- Same instruction in different threads uses **thread id** to index and access different data elements

Let's assume  $N=16$ , 4 threads per warp  $\rightarrow$  4 warps



# Sample GPU SIMT Code (Simplified)

---

CPU code

```
for (ii = 0; ii < 100000; ++ii) {  
    C[ii] = A[ii] + B[ii];  
}
```



CUDA code

```
// there are 100000 threads  
__global__ void KernelFunction(...) {  
    int tid = blockDim.x * blockIdx.x + threadIdx.x;  
    int varA = aa[tid];  
    int varB = bb[tid];  
    C[tid] = varA + varB;  
}
```

# Sample GPU Program (Less Simplified)

## CPU Program

```
void add matrix
( float *a, float* b, float *c, int N) {
    int index;
    for (int i = 0; i < N; ++i)
        for (int j = 0; j < N; ++j) {
            index = i + j*N;
            c[index] = a[index] + b[index];
        }
}

int main () {

    add matrix (a, b, c, N);
}
```

## GPU Program

```
__global__ add_matrix
( float *a, float *b, float *c, int N) {
    int i = blockIdx.x * blockDim.x + threadIdx.x;
    int j = blockIdx.y * blockDim.y + threadIdx.y;
    int index = i + j*N;
    if (i < N && j < N)
        c[index] = a[index]+b[index];
}

int main() {
    dim3 dimBlock( blocksize, blocksize) ;
    dim3 dimGrid (N/dimBlock.x, N/dimBlock.y);
    add_matrix<<<dimGrid, dimBlock>>>( a, b, c, N);
}
```

# Warp-based SIMD vs. Traditional SIMD

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- Traditional **SIMD** contains a single thread
  - Sequential instruction execution; lock-step operations in a SIMD instruction
  - Programming model is SIMD (no extra threads) → SW needs to know vector length
  - ISA contains vector/SIMD instructions
- Warp-based **SIMD** consists of multiple scalar threads executing in a SIMD manner (i.e., same instruction executed by all threads)
  - Does not have to be lock step
  - Each thread can be treated individually (i.e., placed in a different warp) → programming model not SIMD
    - SW does not need to know vector length
    - Enables multithreading and flexible dynamic grouping of threads
  - ISA is scalar → SIMD operations can be formed dynamically
  - Essentially, it is SPMD programming model implemented on SIMD hardware

# SPMD

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- Single procedure/program, multiple data
  - This is a programming model rather than computer organization
- Each processing element executes the same procedure, except on different data elements
  - Procedures can synchronize at certain points in program, e.g. barriers
- Essentially, multiple instruction streams execute the same program
  - Each program/procedure 1) works on different data, 2) can execute a different control-flow path, at run-time
  - Many scientific applications are programmed this way and run on MIMD hardware (multiprocessors)
  - Modern GPUs programmed in a similar way on a SIMD hardware

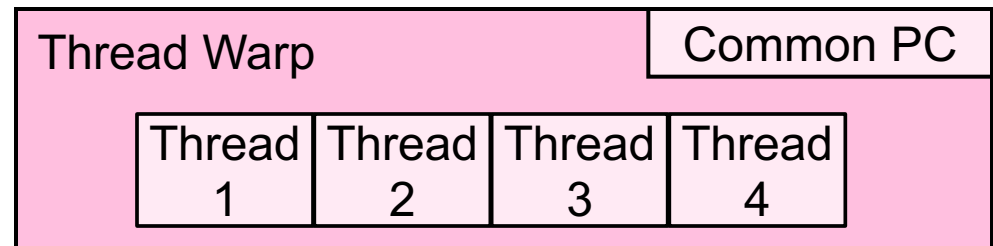
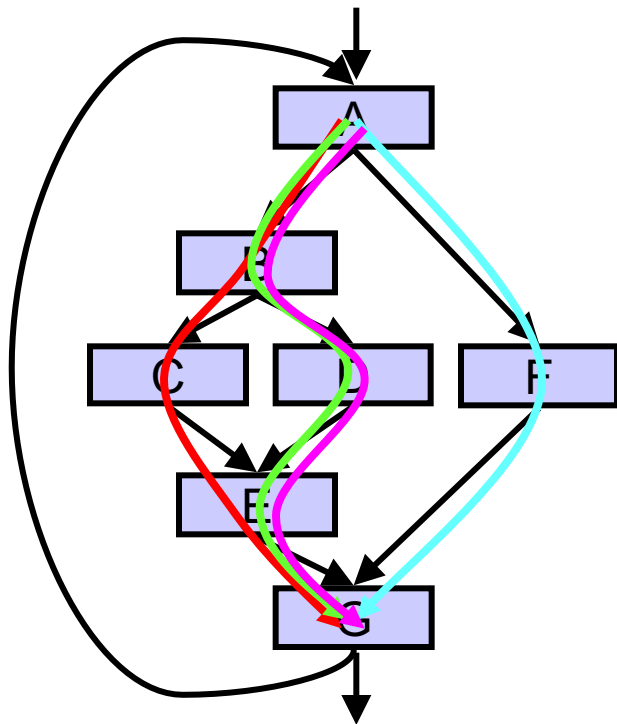
# SIMD vs. SIMT Execution Model

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- SIMD: A single **sequential instruction stream** of **SIMD instructions** → each instruction specifies multiple data inputs
  - [VLD, VLD, VADD, VST], VLEN
- SIMT: **Multiple instruction streams** of **scalar instructions** → threads grouped dynamically into warps
  - [LD, LD, ADD, ST], NumThreads
- Two Major SIMT Advantages:
  - **Can treat each thread separately** → i.e., can execute each thread independently on any type of scalar pipeline → MIMD processing
  - **Can group threads into warps flexibly** → i.e., can group threads that are supposed to *truly* execute the same instruction → dynamically obtain and maximize benefits of SIMD processing

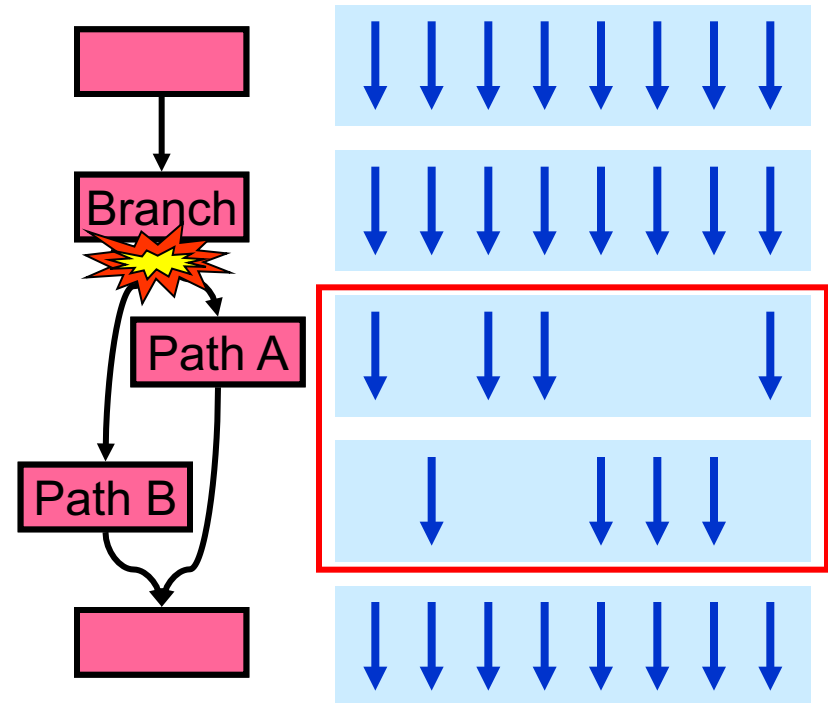
# Threads Can Take Different Paths in Warp-based SIMD

- Each thread can have **conditional control flow instructions**
- Threads can execute different control flow paths



# Control Flow Problem in GPUs/SIMT

- A GPU uses a SIMD pipeline to save area on control logic
  - Groups scalar threads into warps
- **Branch divergence** occurs when threads inside warps branch to different execution paths



**This is the same as conditional/predicated/masked execution.  
Recall the Vector Mask and Masked Vector Operations?**



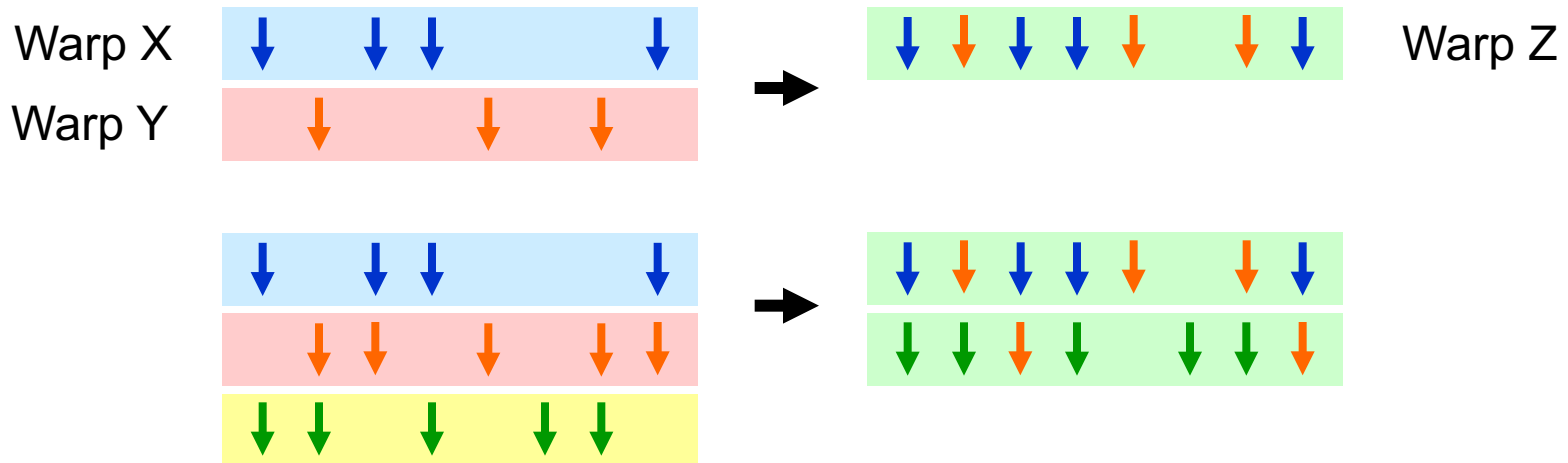
# Remember: Each Thread Is Independent

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- Two Major SIMT Advantages:
  - Can treat each thread separately → i.e., can execute each thread independently on any type of scalar pipeline → MIMD processing
  - Can group threads into warps flexibly → i.e., can group threads that are supposed to *truly* execute the same instruction → dynamically obtain and maximize benefits of SIMD processing
- If we have many threads
- We can find individual threads that are at the same PC
- And, group them together into a single warp dynamically
- This reduces “divergence” → improves SIMD utilization
  - SIMD utilization: fraction of SIMD lanes executing a useful operation (i.e., executing an active thread)

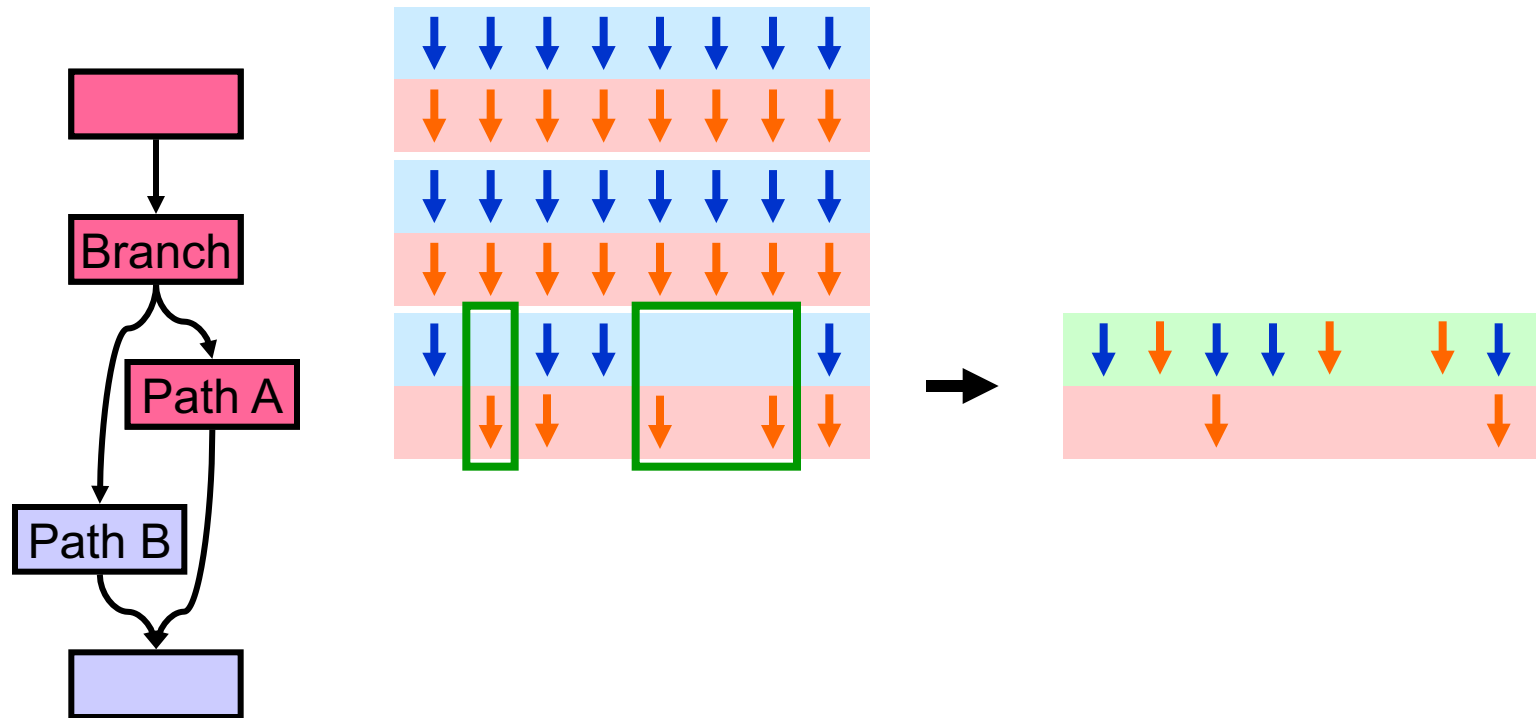
# Dynamic Warp Formation/Merging

- Idea: Dynamically merge threads executing the same instruction (after branch divergence)
- Form new warps from warps that are waiting
  - Enough threads branching to each path enables the creation of full new warps



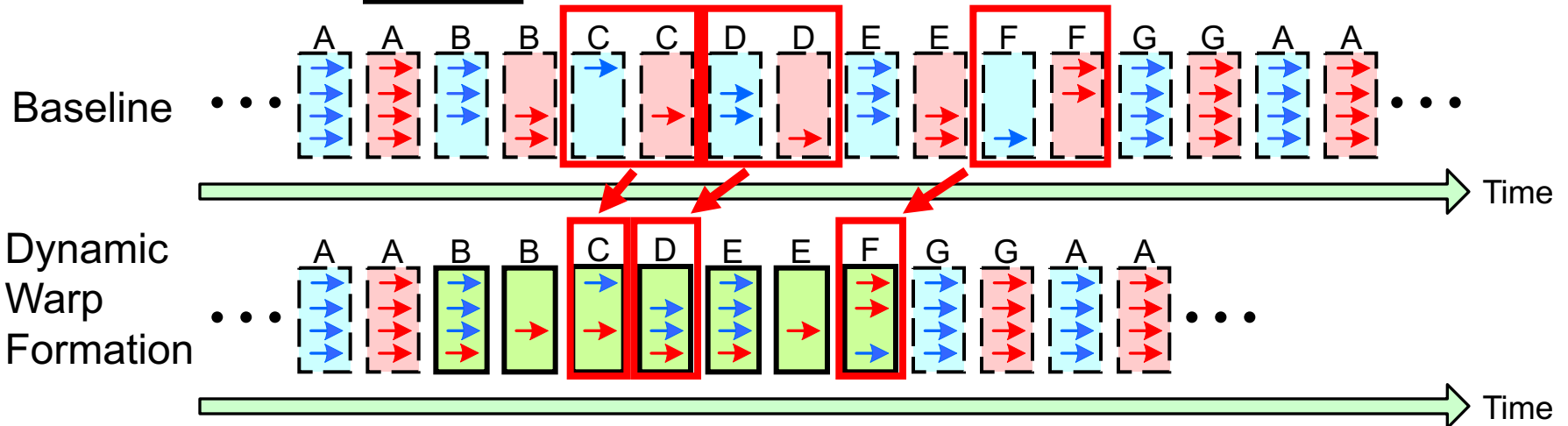
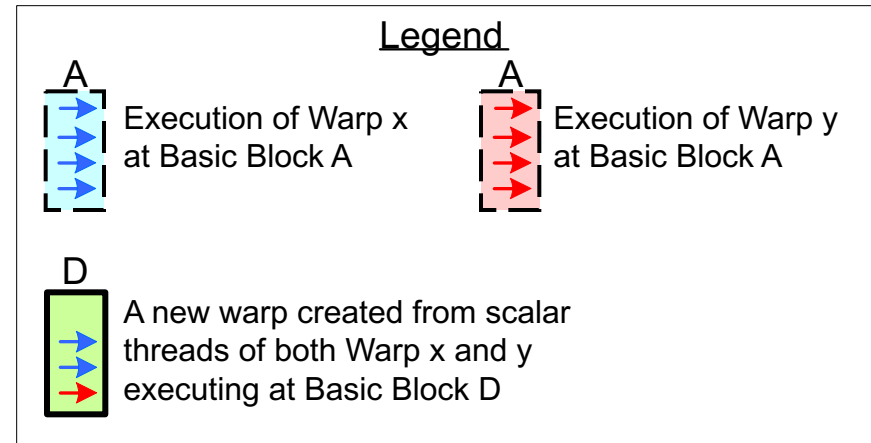
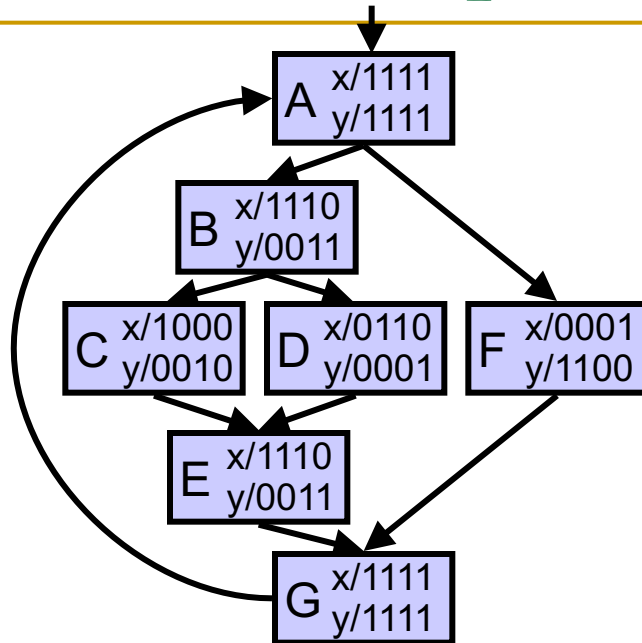
# Dynamic Warp Formation/Merging

- Idea: Dynamically merge threads executing the same instruction (after branch divergence)

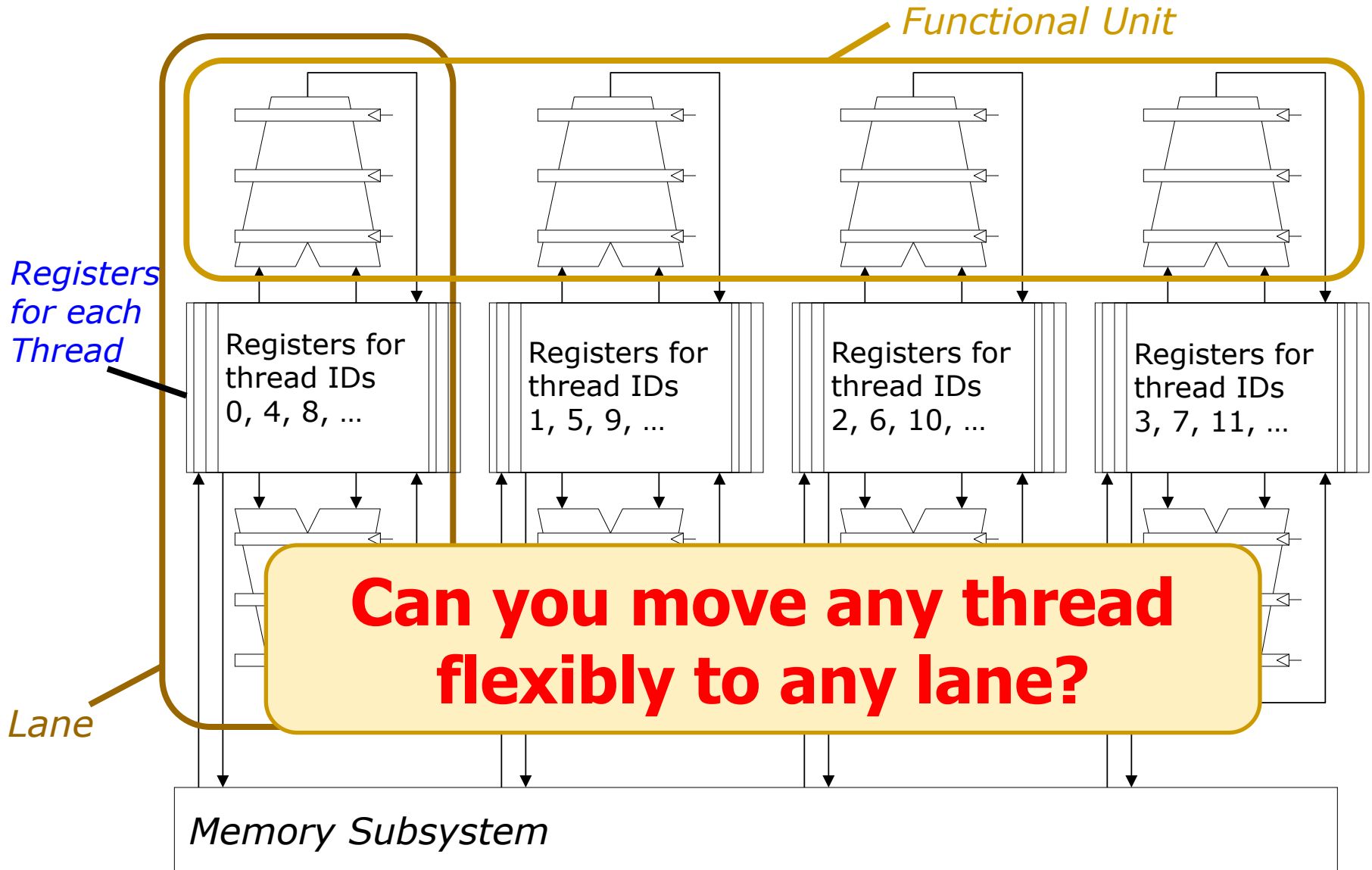


- Fung et al., “Dynamic Warp Formation and Scheduling for Efficient GPU Control Flow,” MICRO 2007.

# Dynamic Warp Formation Example



# Hardware Constraints Limit Flexibility of Warp Grouping



# Design of Digital Circuits

## Lecture 21: SIMD Processors II and Graphics Processing Units

Dr. Juan Gómez Luna

Prof. Onur Mutlu

ETH Zurich

Spring 2018

17 May 2018

We did not cover the following slides in lecture.  
These are for your preparation for the next lecture.

# An Example GPU



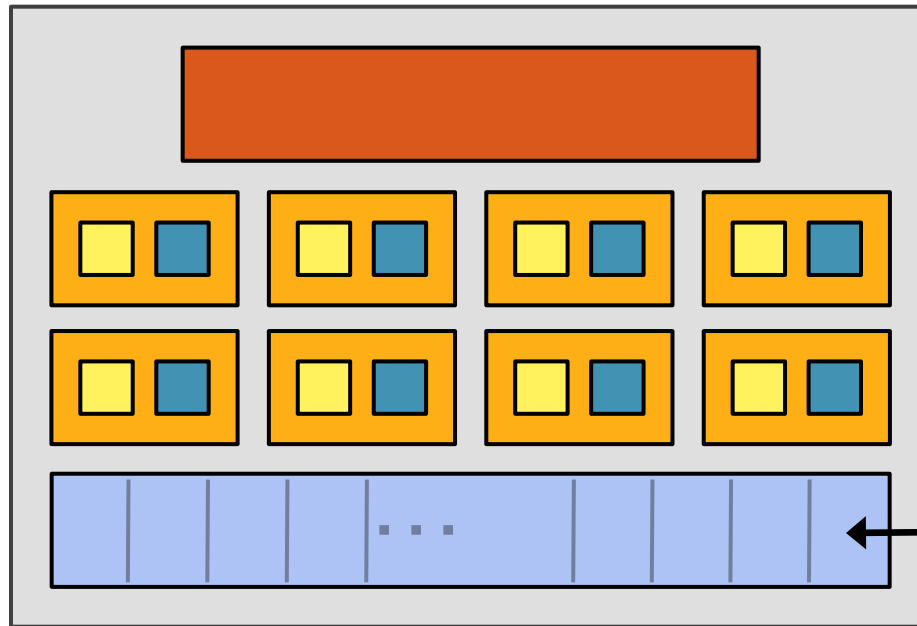
# NVIDIA GeForce GTX 285

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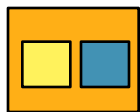
- NVIDIA-speak:
  - ❑ 240 stream processors
  - ❑ “SIMT execution”
- Generic speak:
  - ❑ 30 cores
  - ❑ 8 SIMD functional units per core



# NVIDIA GeForce GTX 285 “core”



64 KB of storage  
for thread contexts  
(registers)



= SIMD functional unit, control  
shared across 8 units



= multiply-add



= multiply



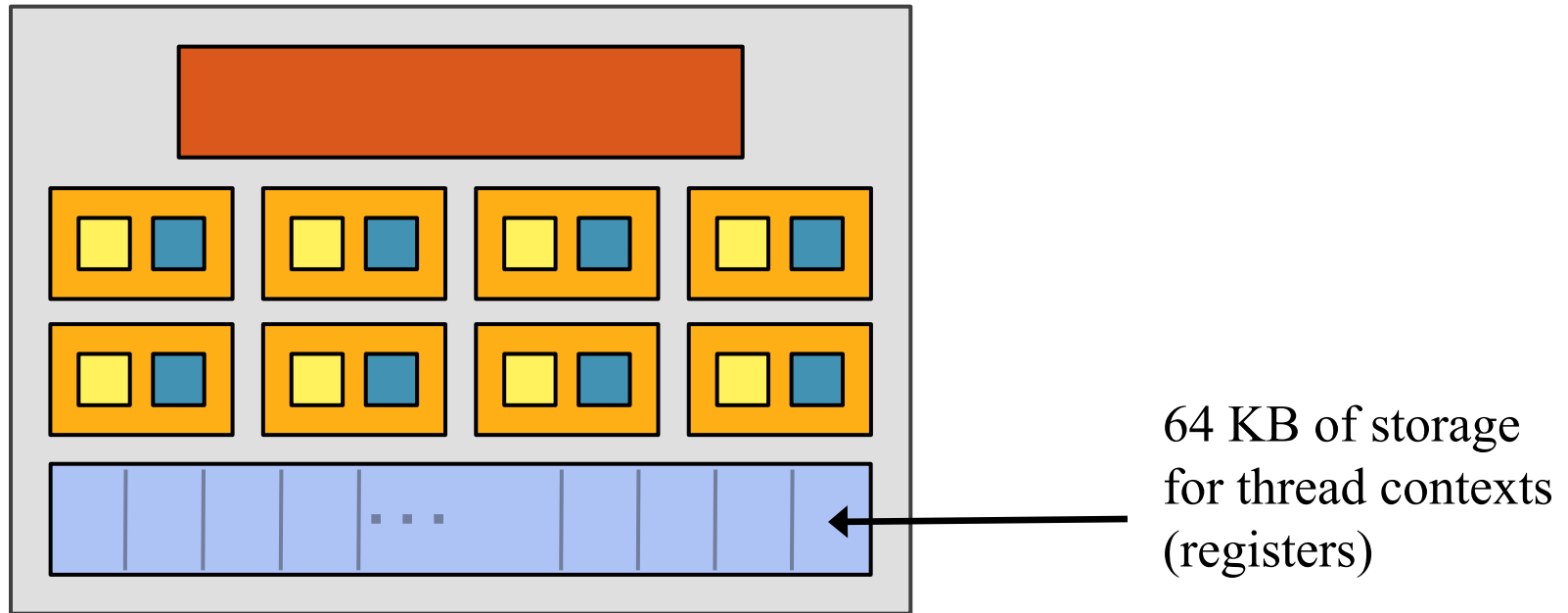
= instruction stream decode



= execution context storage

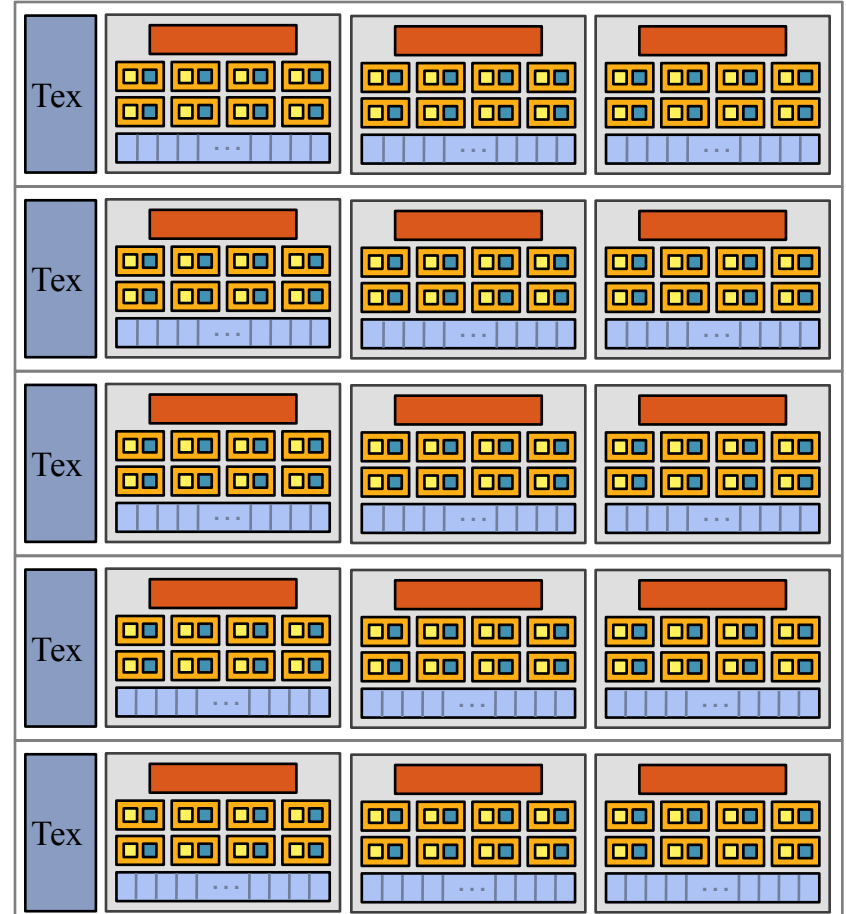
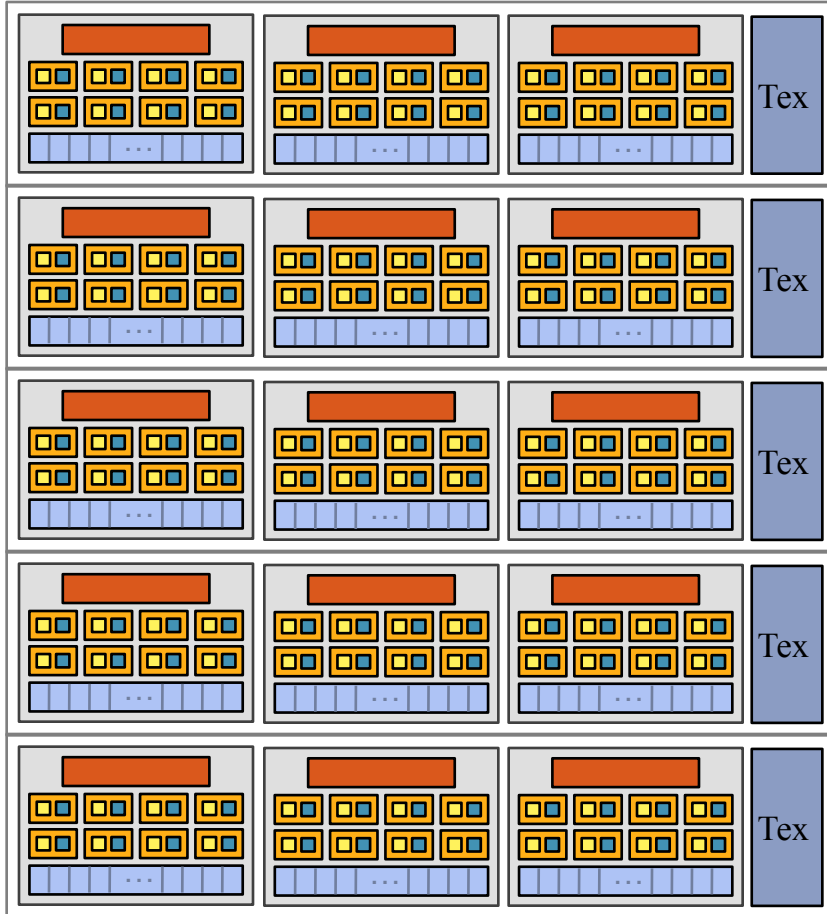
# NVIDIA GeForce GTX 285 “core”

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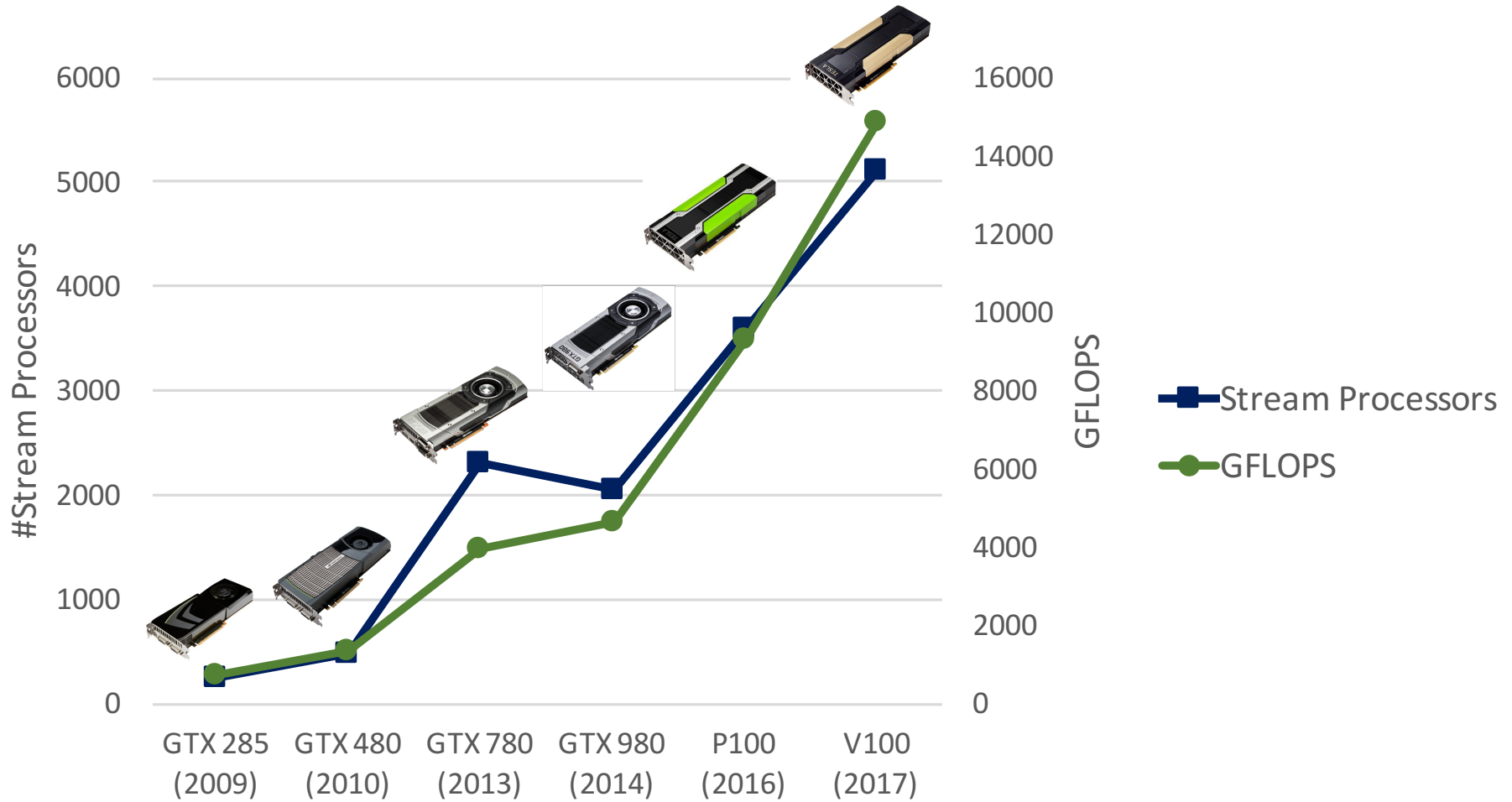
- Groups of 32 **threads** share instruction stream (each group is a Warp)
- Up to 32 warps are simultaneously interleaved
- Up to 1024 thread contexts can be stored

# NVIDIA GeForce GTX 285



30 cores on the GTX 285: 30,720 threads

# Evolution of NVIDIA GPUs



# NVIDIA V100

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- NVIDIA-speak:
  - ❑ 5120 stream processors
  - ❑ “SIMT execution”
- Generic speak:
  - ❑ 80 cores
  - ❑ 64 SIMD functional units per core
  - ❑ Tensor cores for Machine Learning



# NVIDIA V100 Block Diagram



<https://devblogs.nvidia.com/inside-volta/>

## 80 cores on the V100

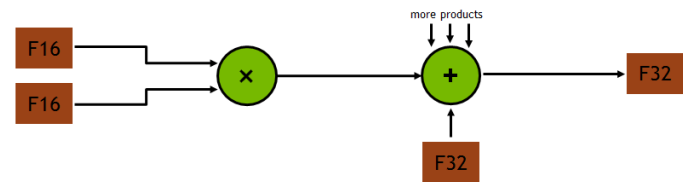
The diagram illustrates the L1 Instruction Cache architecture for the NVIDIA RTX 3090, showing four identical cache units arranged in a 2x2 grid. Each unit contains the following components:

- L0 Instruction Cache**: A blue header bar at the top of each unit.
- Warp Scheduler (32 thread/clock)**: An orange bar below the L0 cache.
- Dispatch Unit (32 thread/clock)**: An orange bar below the warp scheduler.
- Register File (16,384 x 32-bit)**: A large green grid below the dispatch unit, divided into FP64, INT, and FP32 sections.
- SFU (Special Function Unit)**: A red bar at the bottom of each unit, divided into TENSOR CORE and SFU sections.

A yellow circle highlights the TENSOR CORE section in the top-right unit.

## 7.8 TFLOPS Double Precision

FP16 storage/input	Full precision product	Sum with FP32 accumulator	Convert to FP32 result
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$$D = \begin{pmatrix} A_{0,0} & A_{0,1} & A_{0,2} & A_{0,3} \\ A_{1,0} & A_{1,1} & A_{1,2} & A_{1,3} \\ A_{2,0} & A_{2,1} & A_{2,2} & A_{2,3} \\ A_{3,0} & A_{3,1} & A_{3,2} & A_{3,3} \end{pmatrix} \begin{pmatrix} B_{0,0} & B_{0,1} & B_{0,2} & B_{0,3} \\ B_{1,0} & B_{1,1} & B_{1,2} & B_{1,3} \\ B_{2,0} & B_{2,1} & B_{2,2} & B_{2,3} \\ B_{3,0} & B_{3,1} & B_{3,2} & B_{3,3} \end{pmatrix} + \begin{pmatrix} C_{0,0} & C_{0,1} & C_{0,2} & C_{0,3} \\ C_{1,0} & C_{1,1} & C_{1,2} & C_{1,3} \\ C_{2,0} & C_{2,1} & C_{2,2} & C_{2,3} \\ C_{3,0} & C_{3,1} & C_{3,2} & C_{3,3} \end{pmatrix}$$