

Design of Digital Circuits

Lecture 23a: More Caches

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Readings

- Caches

- Required

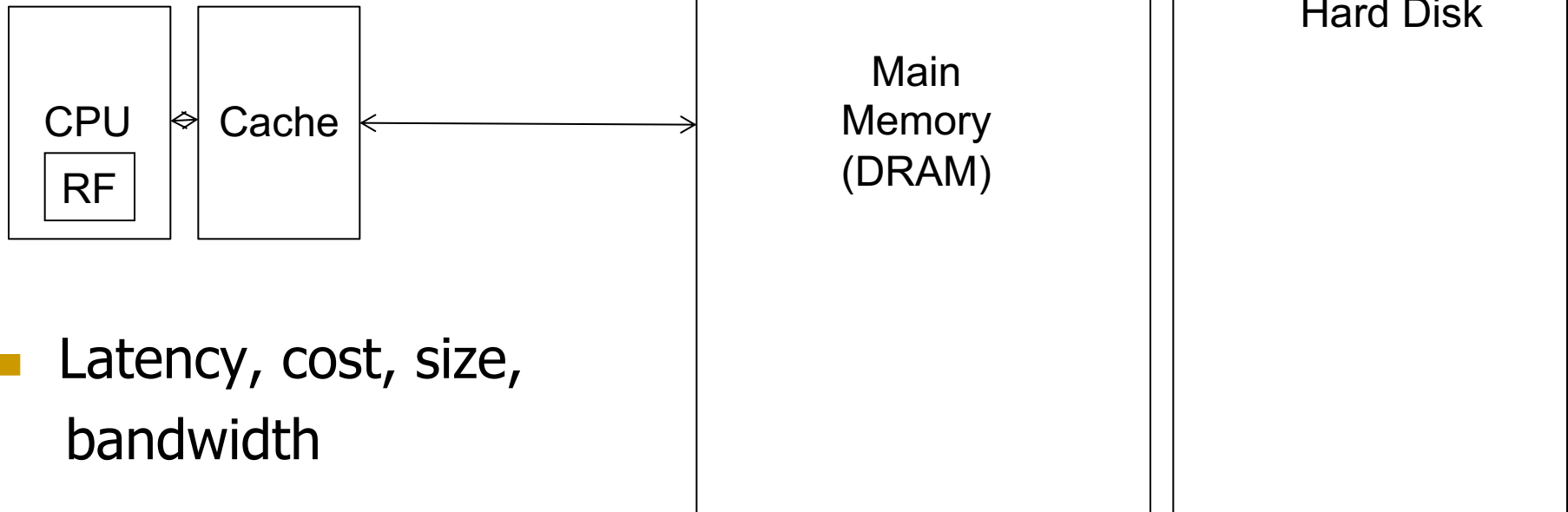
- H&H Chapters 8.1-8.3
- Refresh: P&P Chapter 3.5

- Recommended

- An early cache paper by Maurice Wilkes
 - Wilkes, “**Slave Memories and Dynamic Storage Allocation**,” IEEE Trans. On Electronic Computers, 1965.

Memory Hierarchy

- Fundamental tradeoff
 - Fast memory: small
 - Large memory: slow
- Idea: **Memory hierarchy**



- Latency, cost, size, bandwidth

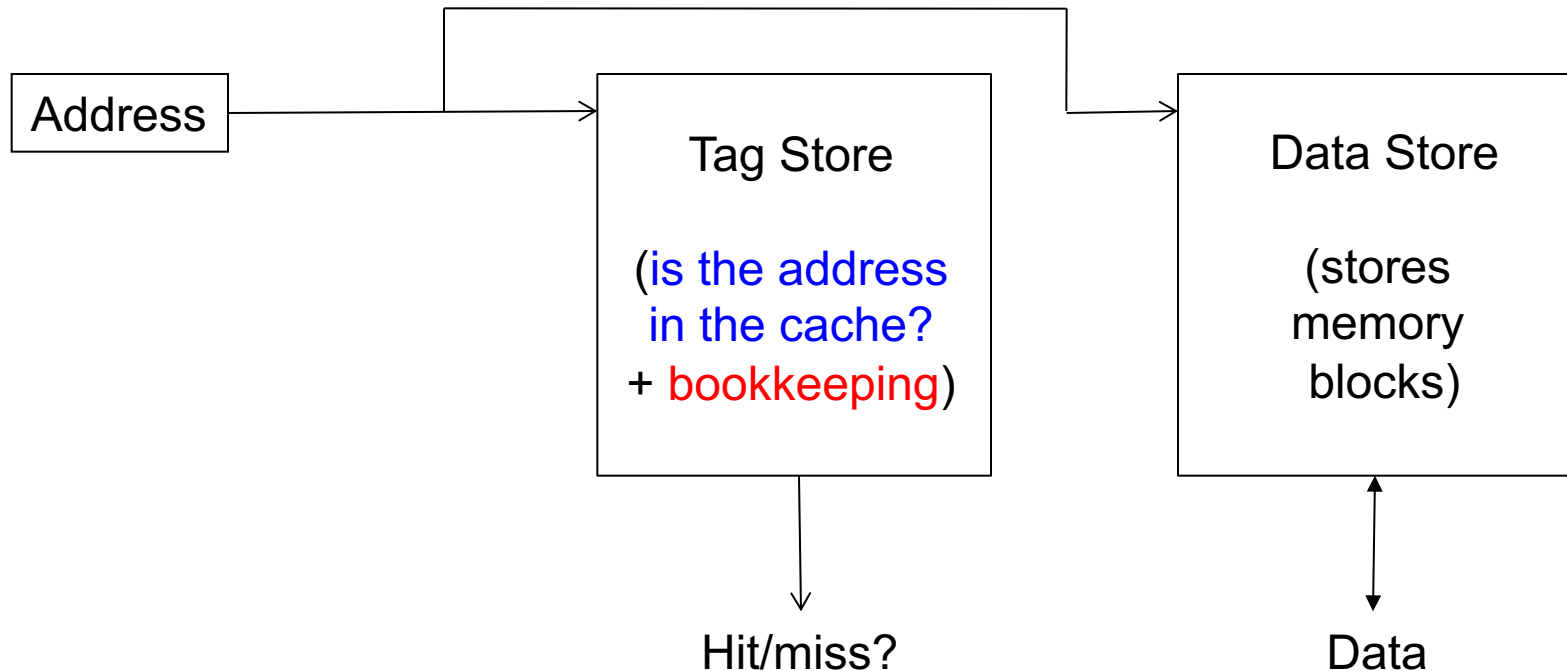
Cache

- Generically, any structure that “memoizes” frequently used results to avoid repeating the long-latency operations required to reproduce the results from scratch, e.g. a web cache
- Most commonly in the processor design context: an automatically-managed memory structure based on SRAM
 - memoize in SRAM the most frequently accessed DRAM memory locations to avoid repeatedly paying for the DRAM access latency

Caching Basics

- **Block (line):** Unit of storage in the cache
 - Memory is logically divided into cache blocks that map to locations in the cache
- On a reference:
 - **HIT:** If in cache, use cached data instead of accessing memory
 - **MISS:** If not in cache, bring block into cache
 - Maybe have to kick something else out to do it
- Some important cache design decisions
 - **Placement:** where and how to place/find a block in cache?
 - **Replacement:** what data to remove to make room in cache?
 - **Granularity of management:** large or small blocks? Subblocks?
 - **Write policy:** what do we do about writes?
 - **Instructions/data:** do we treat them separately?

Cache Abstraction and Metrics



- Cache hit rate = $(\# \text{ hits}) / (\# \text{ hits} + \# \text{ misses}) = (\# \text{ hits}) / (\# \text{ accesses})$
- Average memory access time (AMAT)
 $= (\text{hit-rate} * \text{hit-latency}) + (\text{miss-rate} * \text{miss-latency})$
- Aside: *Is reducing AMAT always beneficial for performance?*

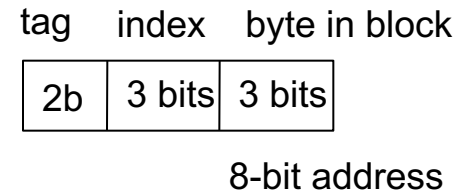
A Basic Hardware Cache Design

- We will start with a basic hardware cache design
- Then, we will examine a multitude of ideas to make it better

Blocks and Addressing the Cache

- Memory is logically divided into fixed-size blocks
- Each block maps to a location in the cache, determined by the **index bits** in the address

- used to index into the tag and data stores

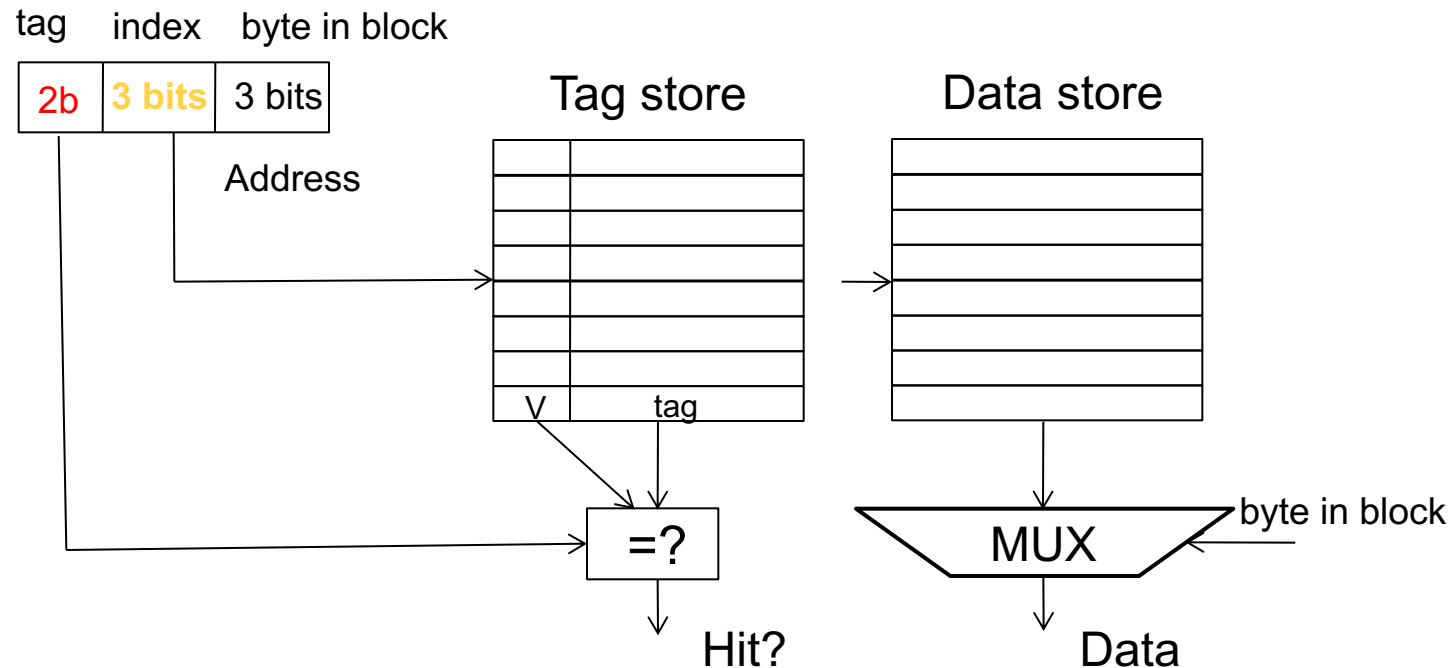


- Cache access:
 - 1) index into the tag and data stores with index bits in address
 - 2) check valid bit in tag store
 - 3) compare tag bits in address with the stored tag in tag store
- If a block is in the cache (cache hit), **the stored tag should be valid and match the tag of the block**

Direct-Mapped Cache: Placement and Access

Block: 00000
Block: 00001
Block: 00010
Block: 00011
Block: 00100
Block: 00101
Block: 00110
Block: 00111
Block: 01000
Block: 01001
Block: 01010
Block: 01011
Block: 01100
Block: 01101
Block: 01110
Block: 01111
Block: 10000
Block: 10001
Block: 10010
Block: 10011
Block: 10100
Block: 10101
Block: 10110
Block: 10111
Block: 11000
Block: 11001
Block: 11010
Block: 11011
Block: 11100
Block: 11101
Block: 11110
Block: 11111

- Assume byte-addressable memory:
256 bytes, 8-byte blocks → 32 blocks
- Assume cache: 64 bytes, 8 blocks
 - Direct-mapped: A block can go to only one location



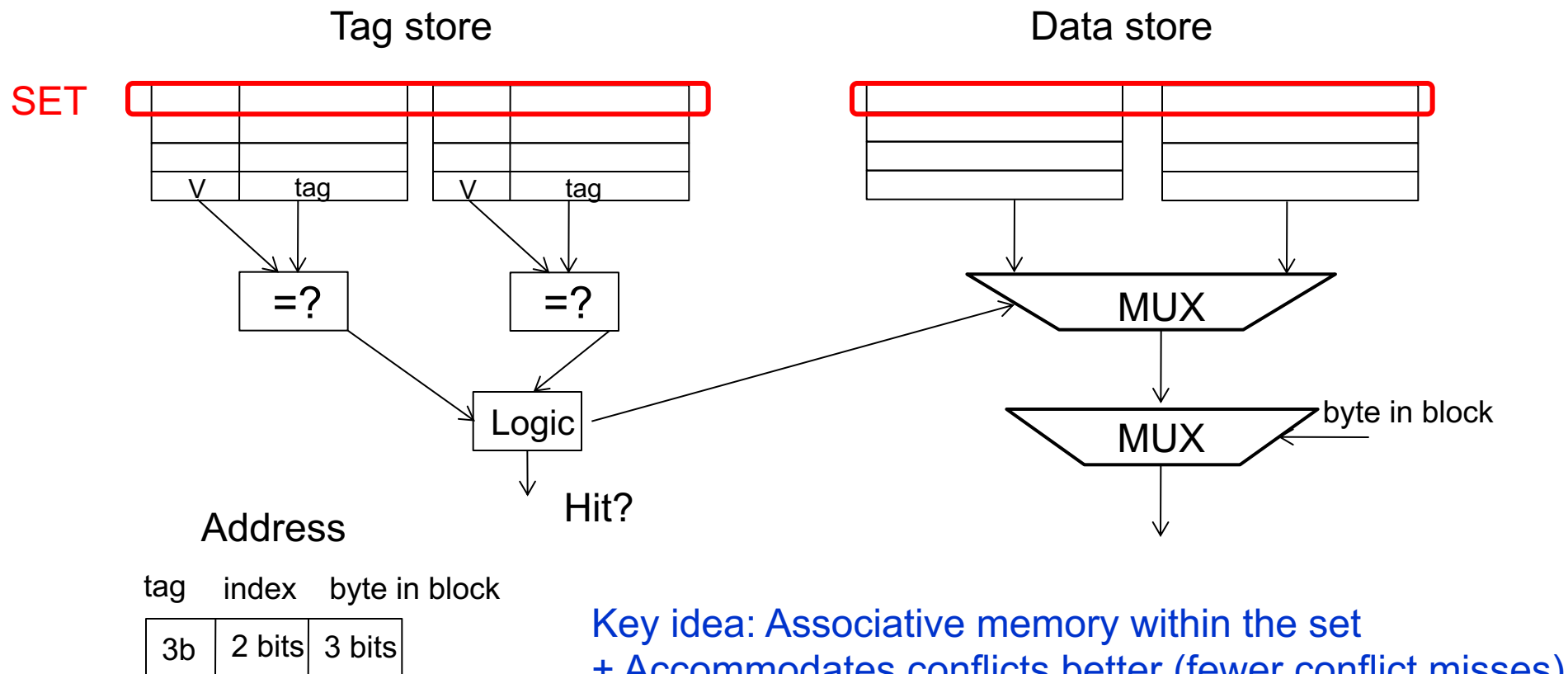
- Addresses with same index contend for the same location
 - Cause conflict misses

Direct-Mapped Caches

- **Direct-mapped cache:** Two blocks in memory that map to the same index in the cache cannot be present in the cache at the same time
 - One index \rightarrow one entry
- Can lead to 0% hit rate if more than one block accessed in an interleaved manner map to the same index
 - Assume addresses A and B have the same index bits but different tag bits
 - A, B, A, B, A, B, A, B, ... \rightarrow conflict in the cache index
 - All accesses are **conflict misses**

Set Associativity

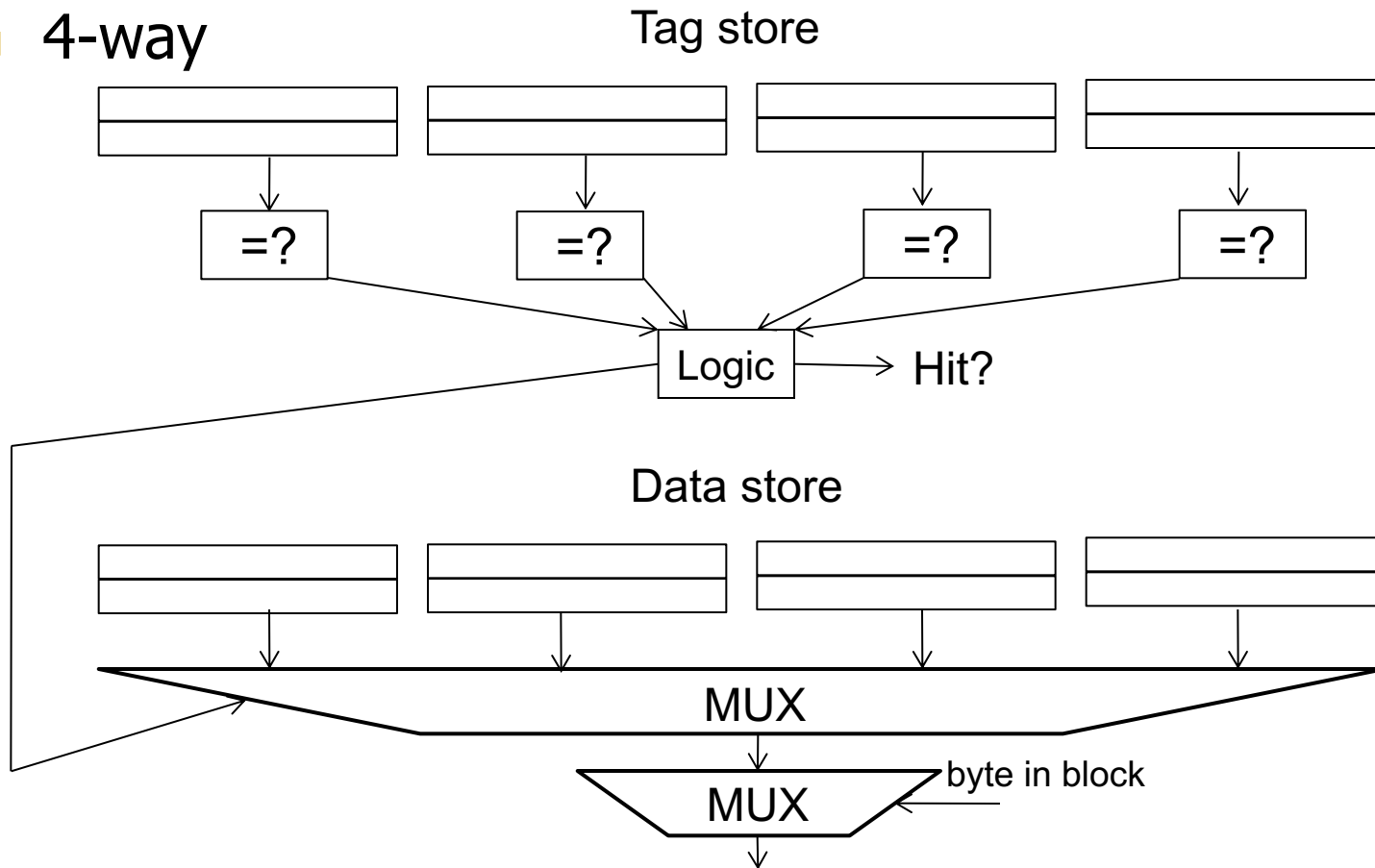
- Addresses 0 and 8 always conflict in direct mapped cache
- Instead of having one column of 8, have 2 columns of 4 blocks



Key idea: Associative memory within the set
+ Accommodates conflicts better (fewer conflict misses)
-- More complex, slower access, larger tag store

Higher Associativity

■ 4-way

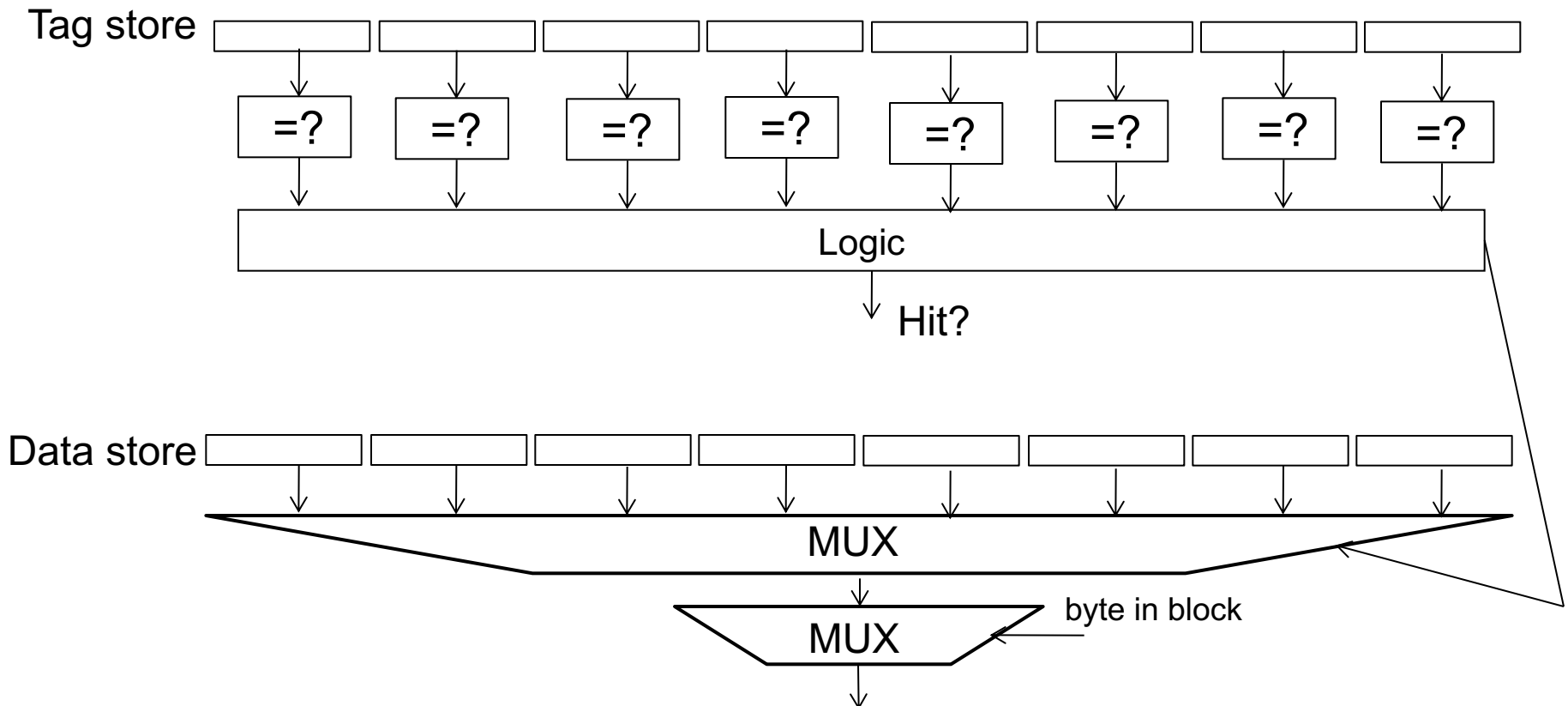


+ Likelihood of conflict misses even lower

-- More tag comparators and wider data mux; larger tags

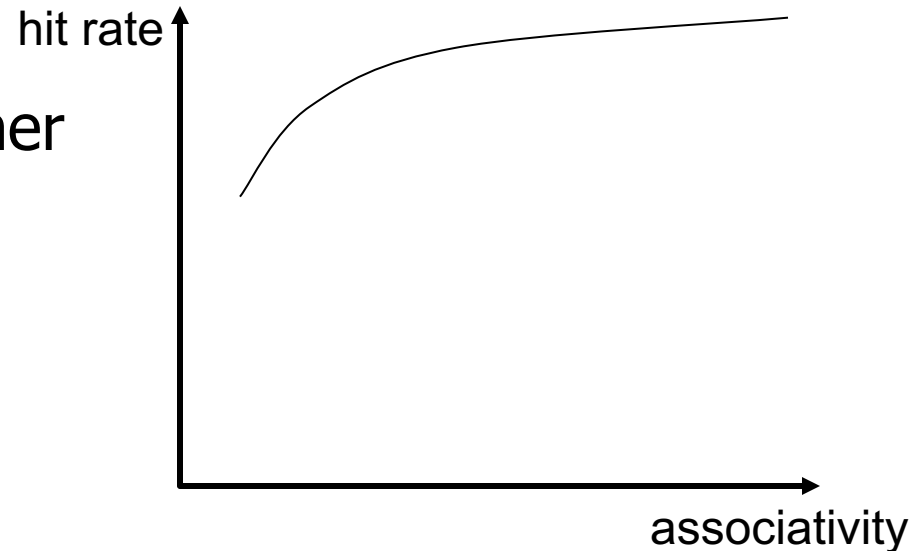
Full Associativity

- Fully associative cache
 - A block can be placed in **any** cache location



Associativity (and Tradeoffs)

- **Degree of associativity**: How many blocks can map to the same index (or set)?
- Higher associativity
 - ++ Higher hit rate
 - Slower cache access time (hit latency and data access latency)
 - More expensive hardware (more comparators)
- Diminishing returns from higher associativity



Issues in Set-Associative Caches

- Think of each block in a set having a “priority”
 - Indicating how important it is to keep the block in the cache
- Key issue: How do you determine/adjust block priorities?
- There are three key decisions in a set:
 - Insertion, promotion, eviction (replacement)
- Insertion: What happens to priorities on a cache fill?
 - Where to insert the incoming block, whether or not to insert the block
- Promotion: What happens to priorities on a cache hit?
 - Whether and how to change block priority
- Eviction/replacement: What happens to priorities on a cache miss?
 - Which block to evict and how to adjust priorities

Eviction/Replacement Policy

- Which block in the set to replace on a cache miss?
 - Any invalid block first
 - If all are valid, consult the replacement policy
 - Random
 - FIFO
 - Least recently used (how to implement?)
 - Not most recently used
 - Least frequently used?
 - Least costly to re-fetch?
 - Why would memory accesses have different cost?
 - Hybrid replacement policies
 - Optimal replacement policy?

Implementing LRU

- Idea: Evict the least recently accessed block
- Problem: Need to keep track of access ordering of blocks
- Question: 2-way set associative cache:
 - What do you need to implement LRU perfectly?
- Question: 4-way set associative cache:
 - What do you need to implement LRU perfectly?
 - How many different orderings possible for the 4 blocks in the set?
 - How many bits needed to encode the LRU order of a block?
 - What is the logic needed to determine the LRU victim?

Approximations of LRU

- Most modern processors do not implement “true LRU” (also called “perfect LRU”) in highly-associative caches
- Why?
 - True LRU is complex
 - LRU is an approximation to predict locality anyway (i.e., not the best possible cache management policy)
- Examples:
 - Not MRU (not most recently used)
 - Hierarchical LRU: divide the N-way set into M “groups”, track the MRU group and the MRU way in each group
 - Victim-NextVictim Replacement: Only keep track of the victim and the next victim

Cache Replacement Policy: LRU or Random

- LRU vs. Random: Which one is better?
 - Example: 4-way cache, cyclic references to A, B, C, D, E
 - 0% hit rate with LRU policy
- **Set thrashing:** When the “program working set” in a set is larger than set associativity
 - Random replacement policy is better when thrashing occurs
- In practice:
 - Depends on workload
 - Average hit rate of LRU and Random are similar
- Best of both Worlds: Hybrid of LRU and Random
 - How to choose between the two? **Set sampling**
 - See Qureshi et al., “**A Case for MLP-Aware Cache Replacement**,” ISCA 2006.

What Is the Optimal Replacement Policy?

- Belady's OPT
 - Replace the block that is going to be referenced furthest in the future by the program
 - Belady, “A study of replacement algorithms for a virtual-storage computer,” IBM Systems Journal, 1966.
 - How do we implement this? Simulate?

- Is this optimal for minimizing miss rate?
- Is this optimal for minimizing execution time?
 - No. Cache miss latency/cost varies from block to block!
 - Two reasons: Remote vs. local caches and miss overlapping
 - Qureshi et al. “A Case for MLP-Aware Cache Replacement,” ISCA 2006.

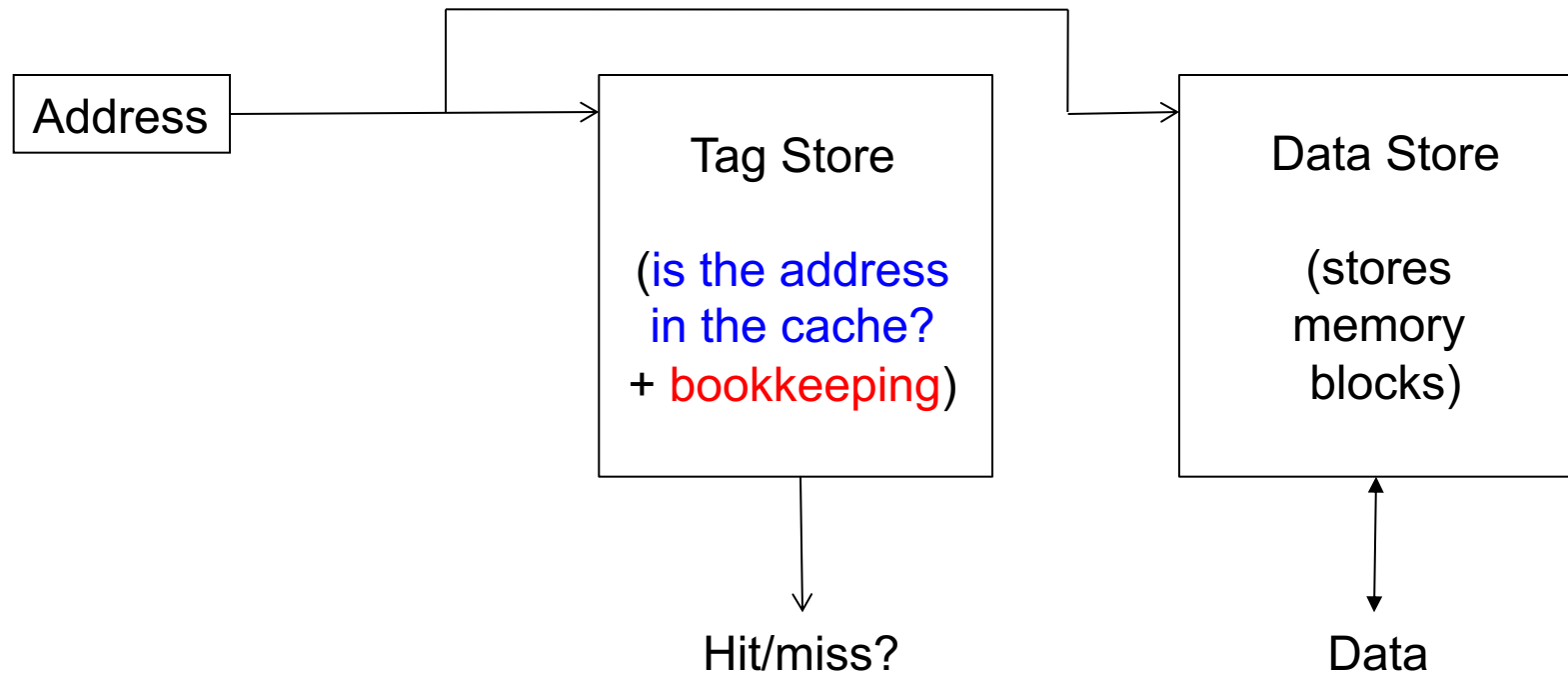
Reading

- Key observation: **Some misses more costly than others** as their latency is exposed as stall time. **Reducing miss rate is not always good for performance.** Cache replacement should take into account MLP of misses.
- Moinuddin K. Qureshi, Daniel N. Lynch, Onur Mutlu, and Yale N. Patt, **"A Case for MLP-Aware Cache Replacement"**
Proceedings of the 33rd International Symposium on Computer Architecture (ISCA), pages 167-177, Boston, MA, June 2006. [Slides \(ppt\)](#)

A Case for MLP-Aware Cache Replacement

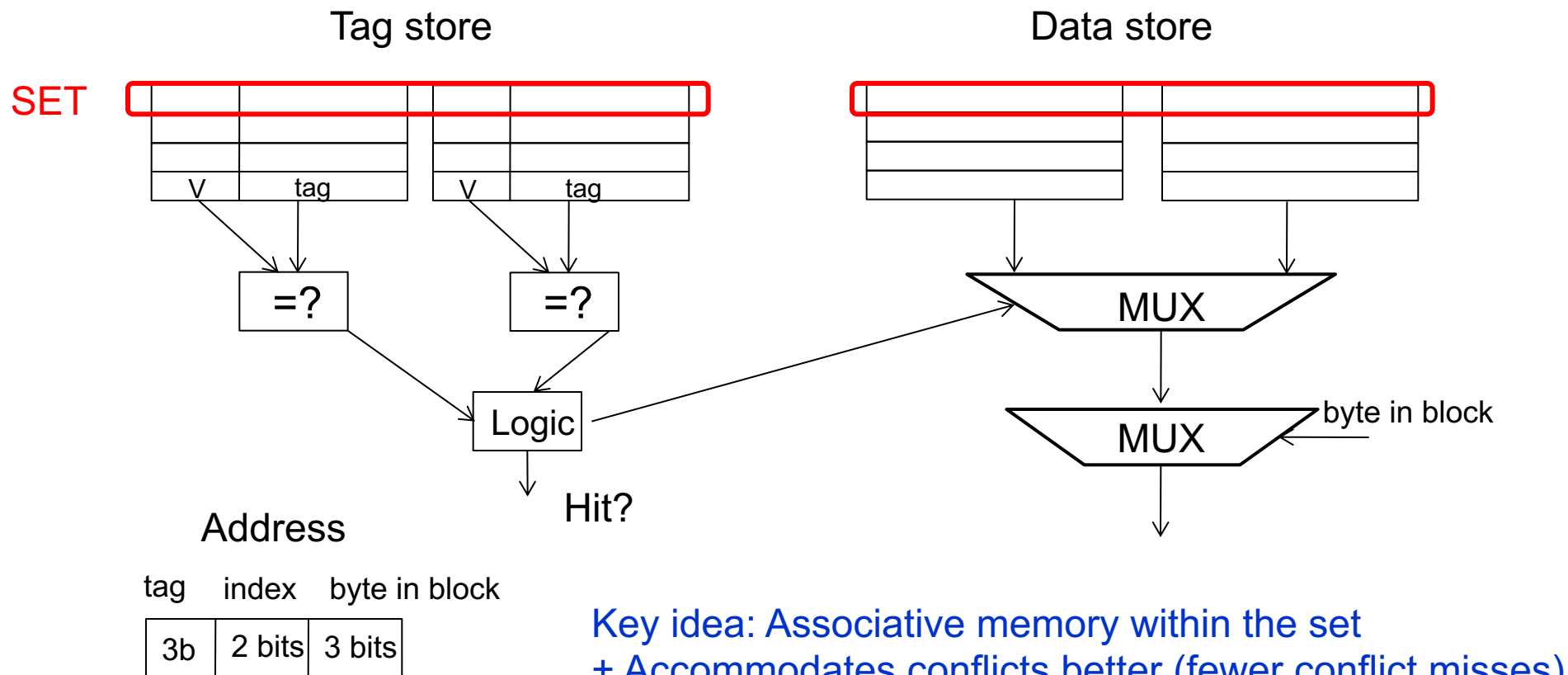
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Recall: Cache Structure



Recall: Set Associativity

- Addresses 0 and 8 always conflict in direct mapped cache
- Instead of having one column of 8, have 2 columns of 4 blocks



**Key idea: Associative memory within the set
+ Accommodates conflicts better (fewer conflict misses)
-- More complex, slower access, larger tag store**

What's In A Tag Store Entry?

- Valid bit
- Tag
- Replacement policy bits

- Dirty bit?
 - Write back vs. write through caches

Handling Writes (I)

- When do we write the modified data in a cache to the next level?
 - Write through: At the time the write happens
 - Write back: When the block is evicted

- Write-back
 - + Can combine multiple writes to the same block before eviction
 - Potentially saves bandwidth between cache levels + saves energy
 - Need a bit in the tag store indicating the block is “dirty/modified”

- Write-through
 - + Simpler
 - + All levels are up to date. Consistency: Simpler cache coherence because no need to check close-to-processor caches' tag stores for presence
 - More bandwidth intensive; no combining of writes

Handling Writes (II)

- Do we allocate a cache block on a write miss?
 - Allocate on write miss: Yes
 - No-allocate on write miss: No

- Allocate on write miss
 - + Can combine writes instead of writing each of them individually to next level
 - + Simpler because write misses can be treated the same way as read misses
 - Requires transfer of the whole cache block

- No-allocate
 - + Conserves cache space if locality of writes is low (potentially better cache hit rate)

Handling Writes (III)

- What if the processor writes to an entire block over a small amount of time?
- Is there any need to bring the block into the cache from memory in the first place?
- Why do we not simply write to only a *portion* of the block, i.e., subblock
 - E.g., 4 bytes out of 64 bytes
 - Problem: Valid and dirty bits are associated with the entire 64 bytes, not with each individual 4 bytes

Subblocked (Sectored) Caches

- Idea: Divide a block into subblocks (or sectors)
 - Have separate valid and dirty bits for each subblock (sector)
 - Allocate only a subblock (or a subset of subblocks) on a request
- ++ No need to transfer the entire cache block into the cache
(A write simply validates and updates a subblock)
- ++ More freedom in transferring subblocks into the cache (a cache block does not need to be in the cache fully)
(How many subblocks do you transfer on a read?)
- More complex design
- May not exploit spatial locality fully



Instruction vs. Data Caches

- **Separate or Unified?**
- **Pros and Cons of Unified:**
 - + Dynamic sharing of cache space: no overprovisioning that might happen with static partitioning (i.e., separate I and D caches)
 - Instructions and data can thrash each other (i.e., no guaranteed space for either)
 - I and D are accessed in different places in the pipeline. Where do we place the unified cache for fast access?
- First level caches are almost always split
 - Mainly for the last reason above
- Higher level caches are almost always unified

Multi-level Caching in a Pipelined Design

- First-level caches (instruction and data)
 - Decisions very much affected by cycle time
 - Small, lower associativity; latency is critical
 - Tag store and data store accessed in parallel
- Second-level caches
 - Decisions need to balance hit rate and access latency
 - Usually large and highly associative; latency not as important
 - Tag store and data store accessed serially
- Serial vs. Parallel access of levels
 - Serial: Second level cache accessed only if first-level misses
 - Second level does not see the same accesses as the first
 - First level acts as a filter (filters some temporal and spatial locality)
 - Management policies are therefore different

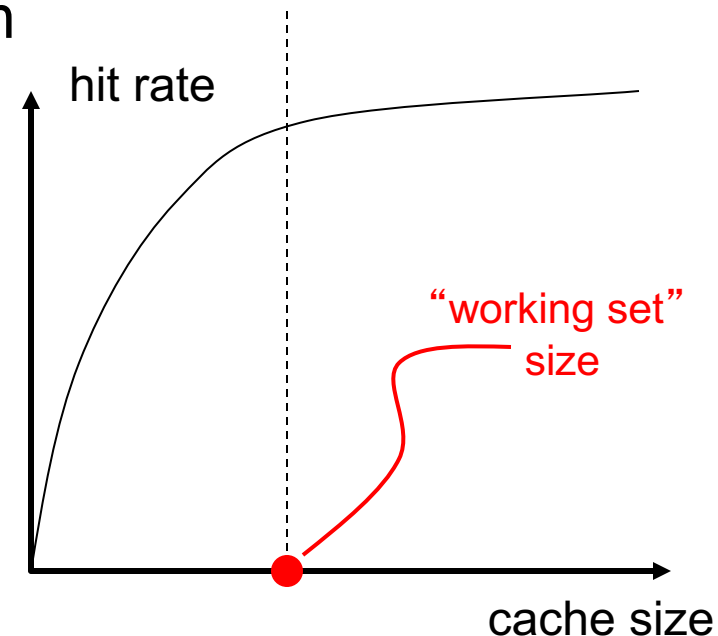
Cache Performance

Cache Parameters vs. Miss/Hit Rate

- Cache size
- Block size
- Associativity
- Replacement policy
- Insertion/Placement policy

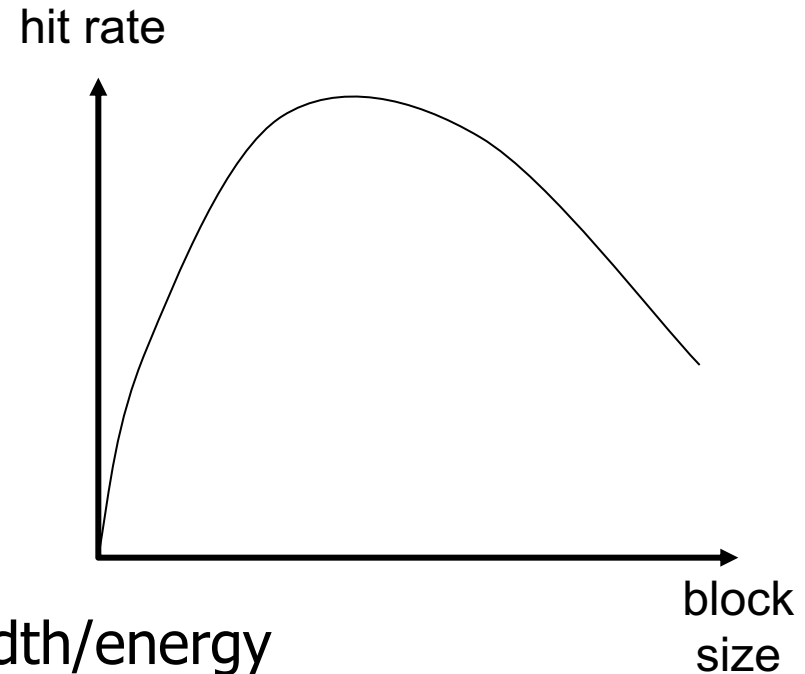
Cache Size

- Cache size: total data (not including tag) capacity
 - bigger can exploit temporal locality better
 - not ALWAYS better
- **Too large** a cache adversely affects hit and miss latency
 - smaller is faster => bigger is slower
 - access time may degrade critical path
- **Too small** a cache
 - doesn't exploit temporal locality well
 - useful data replaced often
- **Working set**: the whole set of data the executing application references
 - Within a time interval



Block Size

- Block size is the data that is associated with an address tag
 - not necessarily the unit of transfer between hierarchies
 - Sub-blocking: A block divided into multiple pieces (each w/ V/D bits)
- Too small blocks
 - don't exploit spatial locality well
 - have larger tag overhead
- Too large blocks
 - too few total # of blocks \rightarrow less temporal locality exploitation
 - waste of cache space and bandwidth/energy if spatial locality is not high



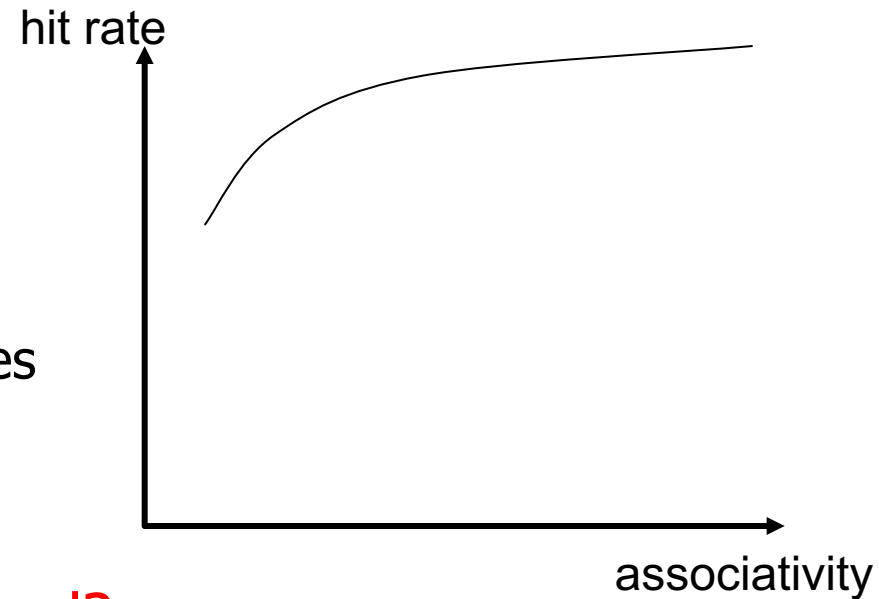
Large Blocks: Critical-Word and Subblocking

- Large cache blocks can take a long time to fill into the cache
 - ❑ fill cache line **critical word first**
 - ❑ restart cache access before complete fill
- Large cache blocks can waste bus bandwidth
 - ❑ divide a block into subblocks
 - ❑ associate separate valid and dirty bits for each subblock
 - ❑ **Recall: When is this useful?**



Associativity

- How many blocks can be present in the same index (i.e., set)?
- Larger associativity
 - ❑ lower miss rate (reduced conflicts)
 - ❑ higher hit latency and area cost (plus diminishing returns)
- Smaller associativity
 - ❑ lower cost
 - ❑ lower hit latency
 - Especially important for L1 caches
- Is power of 2 associativity required?



Classification of Cache Misses

■ Compulsory miss

- ❑ first reference to an address (block) always results in a miss
- ❑ subsequent references should hit unless the cache block is displaced for the reasons below

■ Capacity miss

- ❑ cache is too small to hold everything needed
- ❑ defined as the misses that would occur even in a fully-associative cache (with optimal replacement) of the same capacity

■ Conflict miss

- ❑ defined as any miss that is neither a compulsory nor a capacity miss

How to Reduce Each Miss Type

■ Compulsory

- ❑ Caching cannot help
- ❑ Prefetching can: Anticipate which blocks will be needed soon

■ Conflict

- ❑ More associativity
- ❑ Other ways to get more associativity without making the cache associative
 - Victim cache
 - Better, randomized indexing
 - Software hints?

■ Capacity

- ❑ Utilize cache space better: keep blocks that will be referenced
- ❑ Software management: divide working set and computation such that each “computation phase” fits in cache

How to Improve Cache Performance

- Three fundamental goals
- Reducing miss rate
 - Caveat: reducing miss rate can reduce performance if more costly-to-refetch blocks are evicted
- Reducing miss latency or miss cost
- Reducing hit latency or hit cost
- The above three **together** affect performance

Improving Basic Cache Performance

■ Reducing miss rate

- ❑ More associativity
- ❑ Alternatives/enhancements to associativity
 - Victim caches, hashing, pseudo-associativity, skewed associativity
- ❑ Better replacement/insertion policies
- ❑ Software approaches

■ Reducing miss latency/cost

- ❑ Multi-level caches
- ❑ Critical word first
- ❑ Subblocking/sectoring
- ❑ Better replacement/insertion policies
- ❑ Non-blocking caches (multiple cache misses in parallel)
- ❑ Multiple accesses per cycle
- ❑ Software approaches

Software Approaches for Higher Hit Rate

- Restructuring data access patterns
- Restructuring data layout

- Loop interchange
- Data structure separation/merging
- Blocking
- ...

Restructuring Data Access Patterns (I)

- **Idea: Restructure data layout or data access patterns**
- **Example: If column-major**
 - $x[i+1,j]$ follows $x[i,j]$ in memory
 - $x[i,j+1]$ is far away from $x[i,j]$

Poor code

```
for i = 1, rows
  for j = 1, columns
    sum = sum + x[i,j]
```

Better code

```
for j = 1, columns
  for i = 1, rows
    sum = sum + x[i,j]
```

- This is called **loop interchange**
- Other optimizations can also increase hit rate
 - Loop fusion, array merging, ...

Restructuring Data Access Patterns (II)

- **Blocking**
 - Divide loops operating on arrays into computation chunks so that each chunk can hold its data in the cache
 - Avoids cache conflicts between different chunks of computation
 - Essentially: Divide the working set so that each piece fits in the cache
- Also called Tiling

We did not cover the following slides.
They are for your preparation for the
next lecture.

Restructuring Data Layout (I)

```
struct Node {  
    struct Node* next;  
    int key;  
    char [256] name;  
    char [256] school;  
}
```

```
while (node) {  
    if (node→key == input-key) {  
        // access other fields of node  
    }  
    node = node→next;  
}
```

- Pointer based traversal (e.g., of a linked list)
- Assume a huge linked list (1B nodes) and unique keys
- Why does the code on the left have poor cache hit rate?
 - “Other fields” occupy most of the cache line even though rarely accessed!

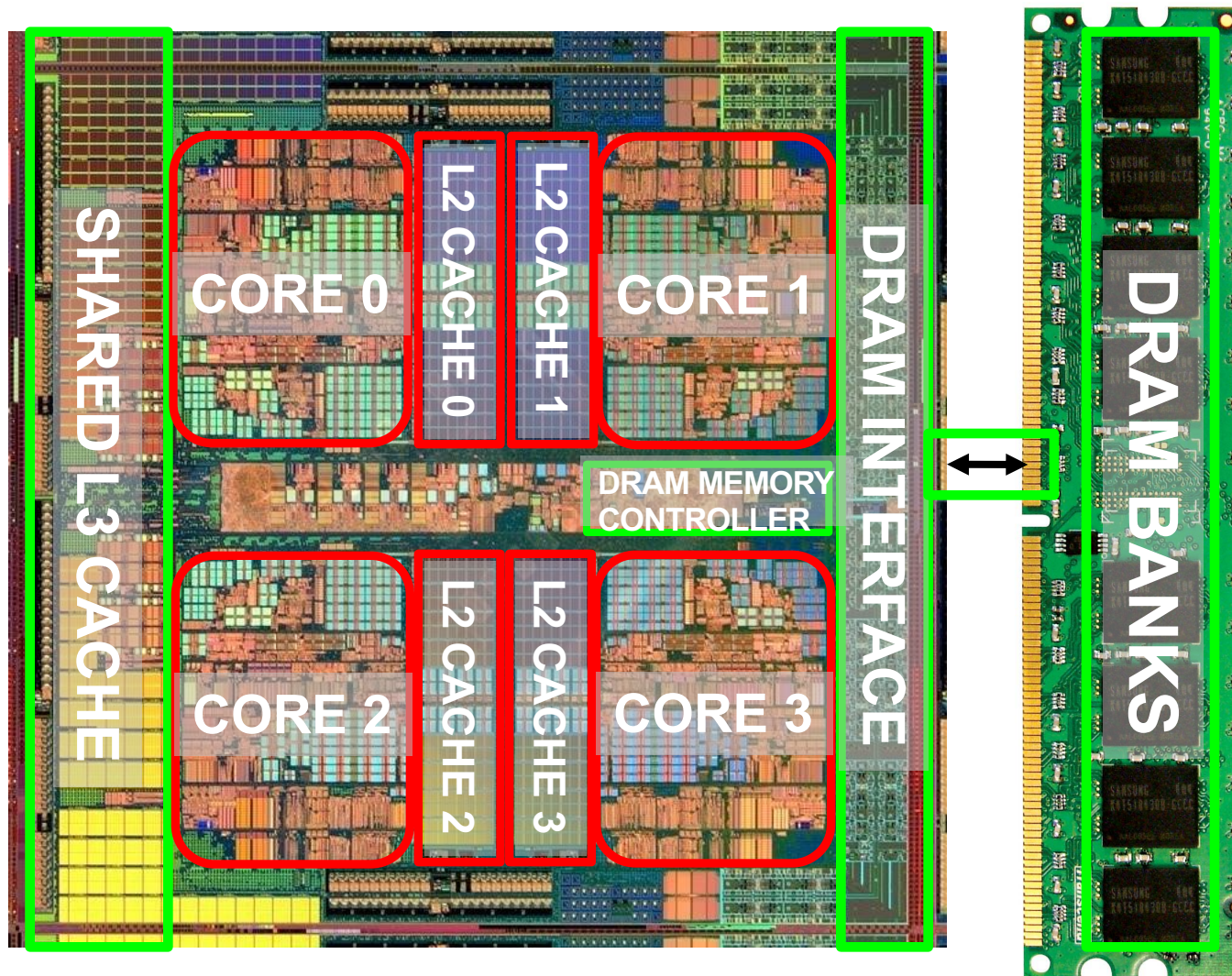
Restructuring Data Layout (II)

```
struct Node {  
    struct Node* next;  
    int key;  
    struct Node-data* node-data;  
}  
  
struct Node-data {  
    char [256] name;  
    char [256] school;  
}  
  
while (node) {  
    if (node→key == input-key) {  
        // access node→node-data  
    }  
    node = node→next;  
}
```

- Idea: separate frequently-used fields of a data structure and pack them into a separate data structure
- Who should do this?
 - Programmer
 - Compiler
 - Profiling vs. dynamic
 - Hardware?
 - Who can determine what is frequently used?

Multi-Core Issues in Caching

Caches in a Multi-Core System

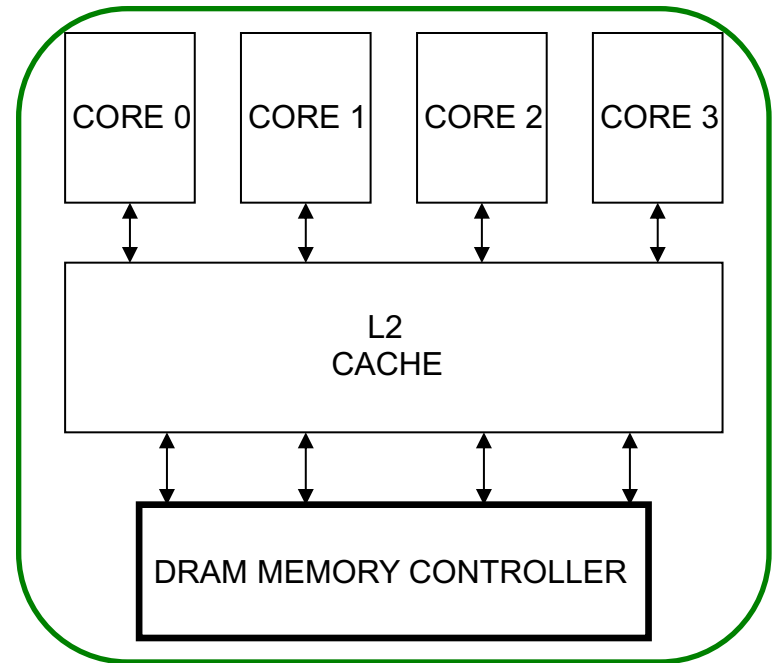
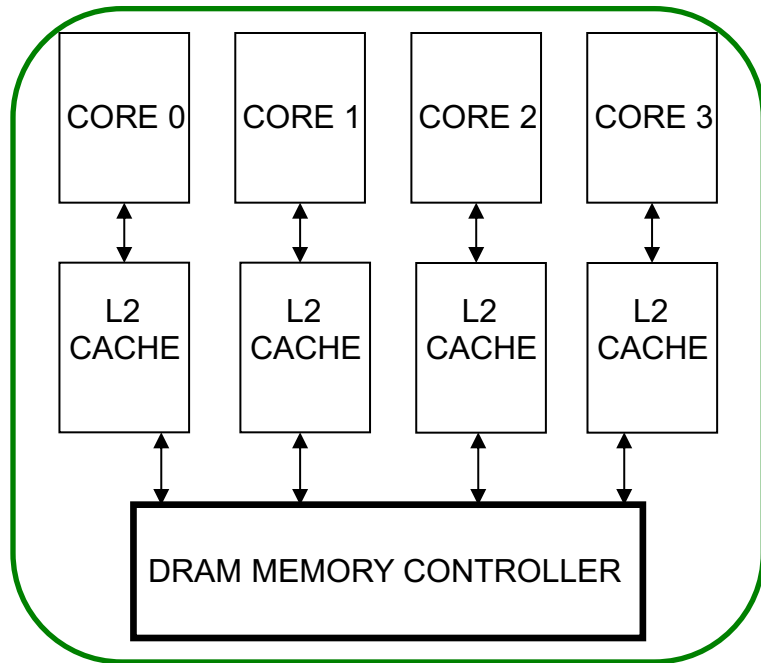


Caches in Multi-Core Systems

- Cache efficiency becomes even more important in a multi-core/multi-threaded system
 - ❑ Memory bandwidth is at premium
 - ❑ Cache space is a limited resource across cores/threads
- How do we design the caches in a multi-core system?
- Many decisions
 - ❑ Shared vs. private caches
 - ❑ How to maximize performance of the entire system?
 - ❑ How to provide QoS to different threads in a shared cache?
 - ❑ Should cache management algorithms be aware of threads?
 - ❑ How should space be allocated to threads in a shared cache?

Private vs. Shared Caches

- **Private** cache: Cache belongs to one core (a shared block can be in multiple caches)
- **Shared** cache: Cache is shared by multiple cores



Resource Sharing Concept and Advantages

- Idea: Instead of dedicating a hardware resource to a hardware context, allow multiple contexts to use it
 - Example resources: functional units, pipeline, caches, buses, memory
 - Why?
-
- + Resource sharing improves utilization/efficiency → throughput
 - When a resource is left idle by one thread, another thread can use it; no need to replicate shared data
 - + Reduces communication latency
 - For example, data shared between multiple threads can be kept in the same cache in multithreaded processors
 - + Compatible with the shared memory programming model

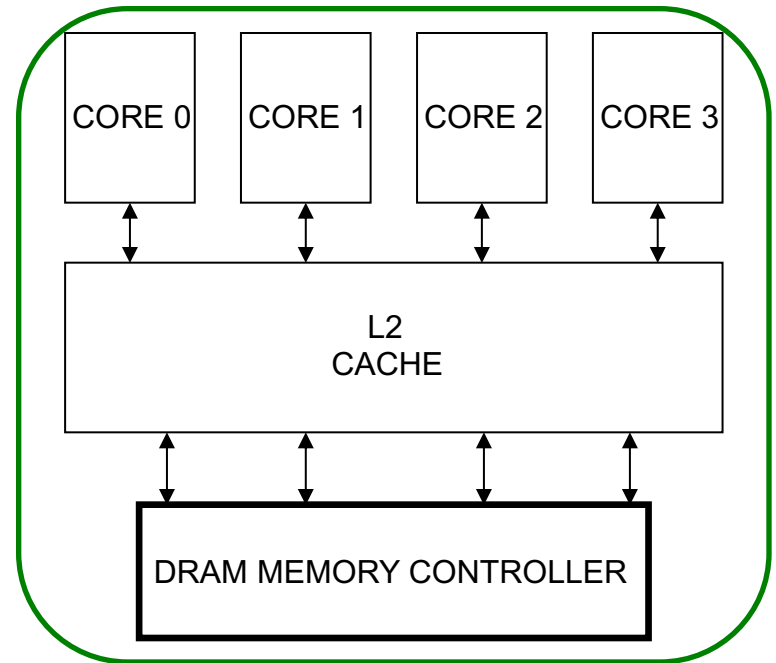
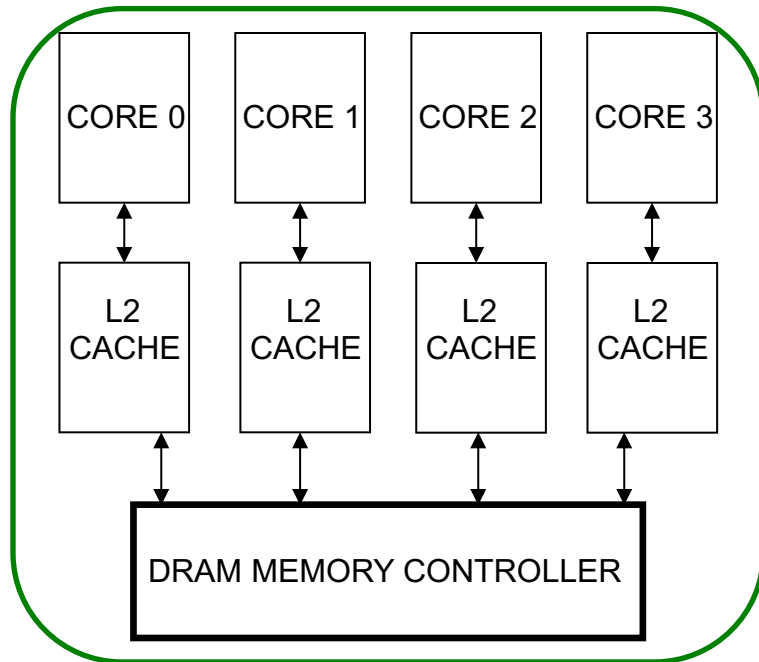
Resource Sharing Disadvantages

- Resource sharing results in **contention for resources**
 - When the resource is not idle, another thread cannot use it
 - If space is occupied by one thread, another thread needs to re-occupy it
- **Sometimes reduces each or some thread's performance**
 - Thread performance can be worse than when it is run alone
- **Eliminates performance isolation** → inconsistent performance across runs
 - Thread performance depends on co-executing threads
- Uncontrolled (free-for-all) sharing **degrades QoS**
 - Causes unfairness, starvation

Need to efficiently and fairly utilize shared resources

Private vs. Shared Caches

- **Private** cache: Cache belongs to one core (a shared block can be in multiple caches)
- **Shared** cache: Cache is shared by multiple cores



Shared Caches Between Cores

■ Advantages:

- ❑ High effective capacity
- ❑ **Dynamic partitioning** of available cache space
 - No fragmentation due to static partitioning
 - If one core does not utilize some space, another core can
- ❑ **Easier to maintain coherence (a cache block is in a single location)**

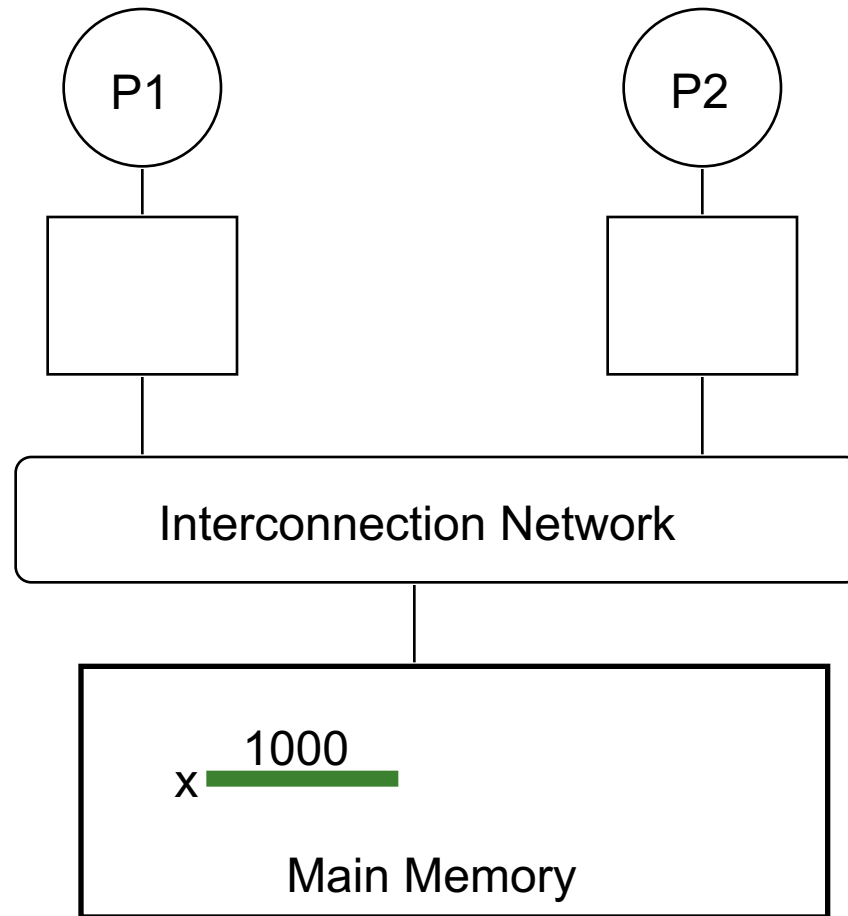
■ Disadvantages

- ❑ Slower access (cache not tightly coupled with the core)
- ❑ Cores incur **conflict misses due to other cores' accesses**
 - Misses due to inter-core interference
 - Some cores can destroy the hit rate of other cores
- ❑ Guaranteeing a minimum level of service (or fairness) to each core is harder (how much space, how much bandwidth?)

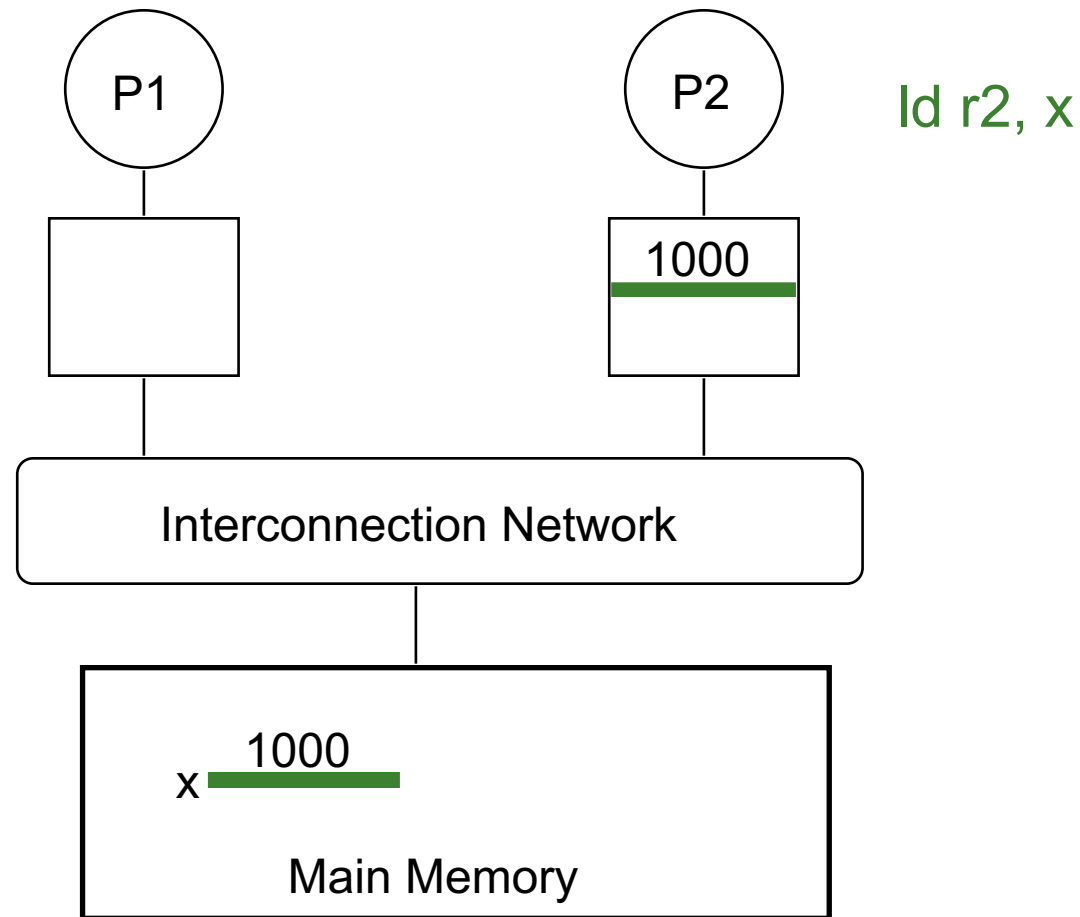
Cache Coherence

Cache Coherence

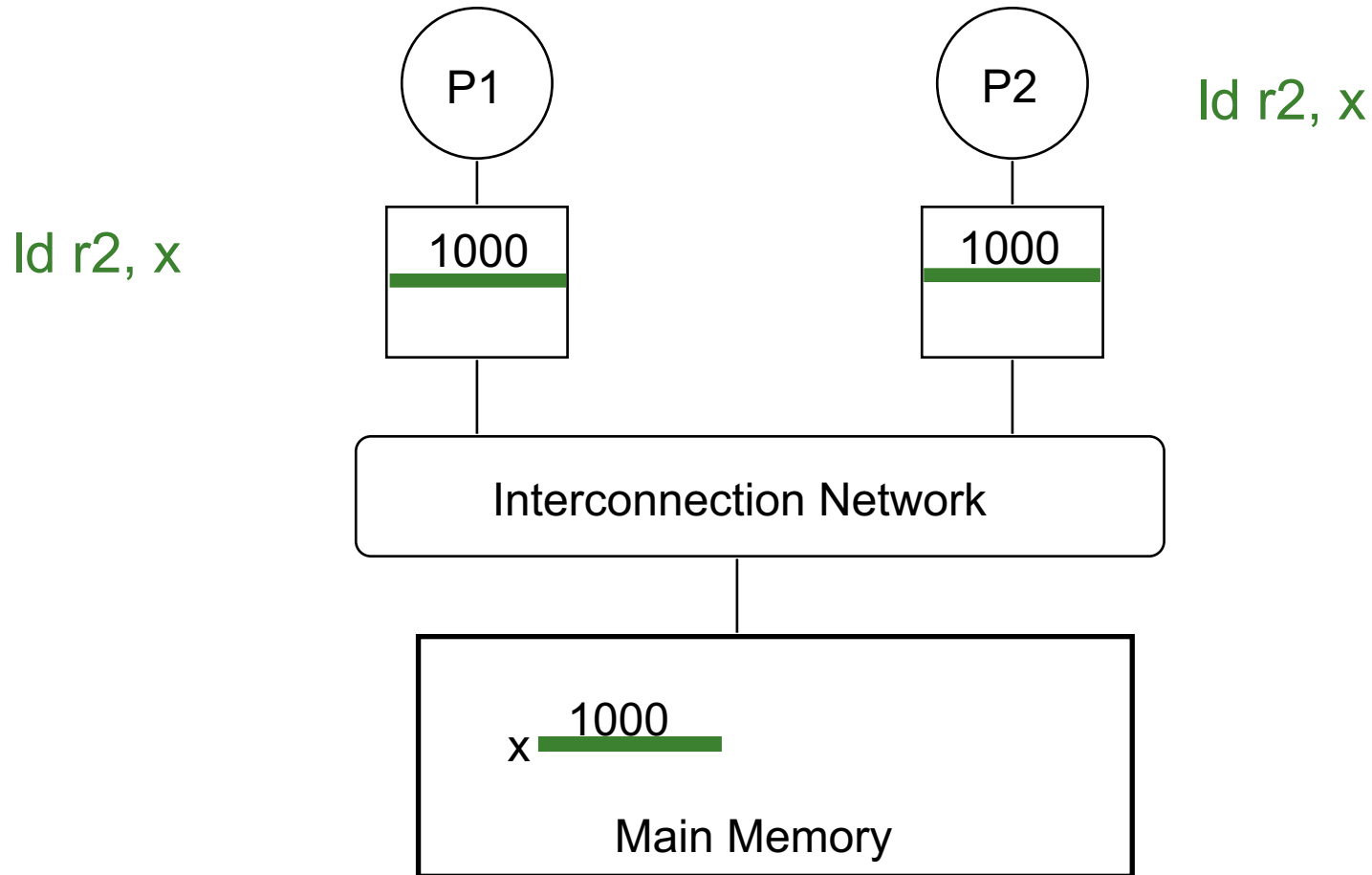
- Basic question: If multiple processors cache the same block, how do they ensure they all see a consistent state?



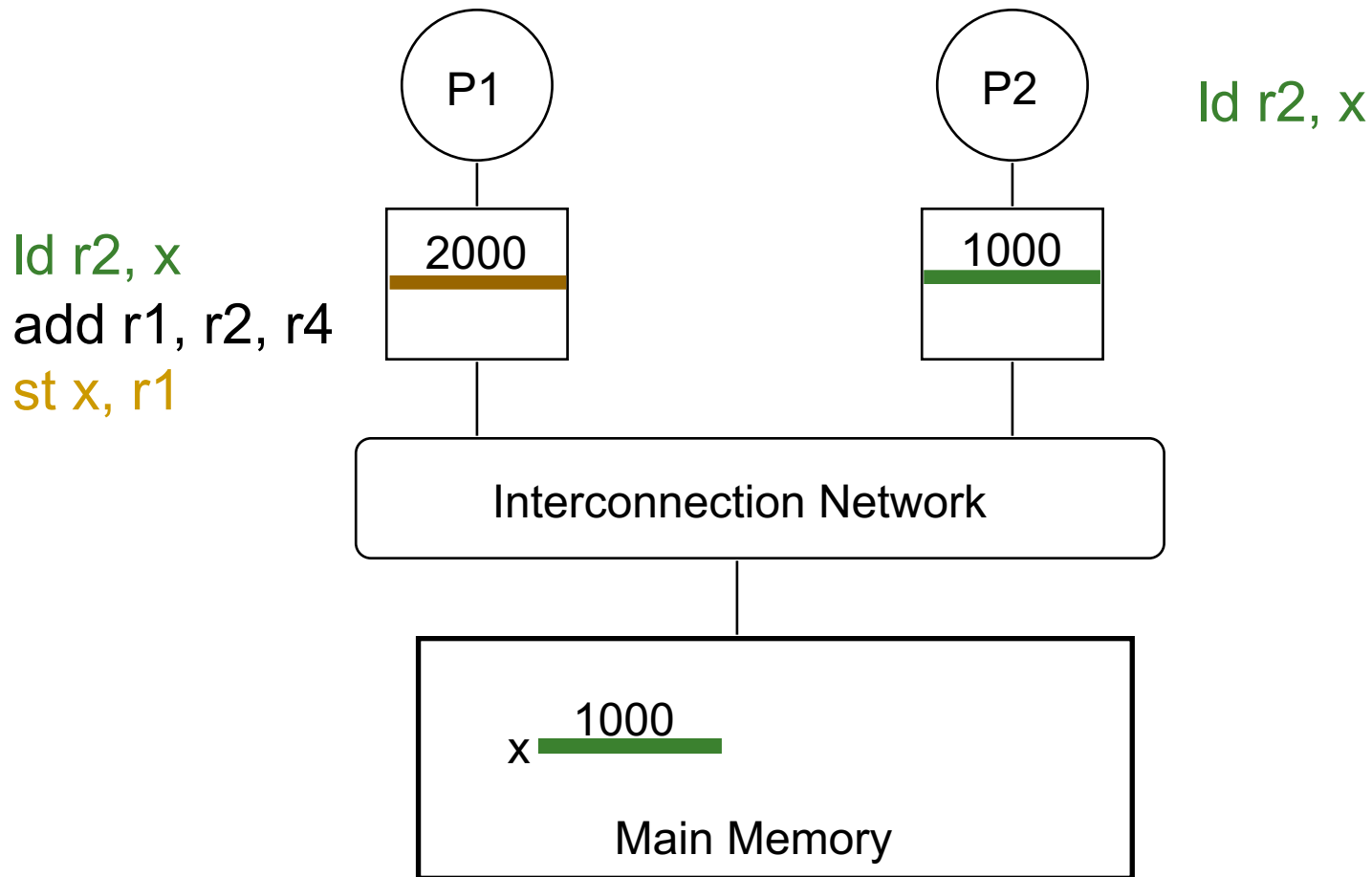
The Cache Coherence Problem



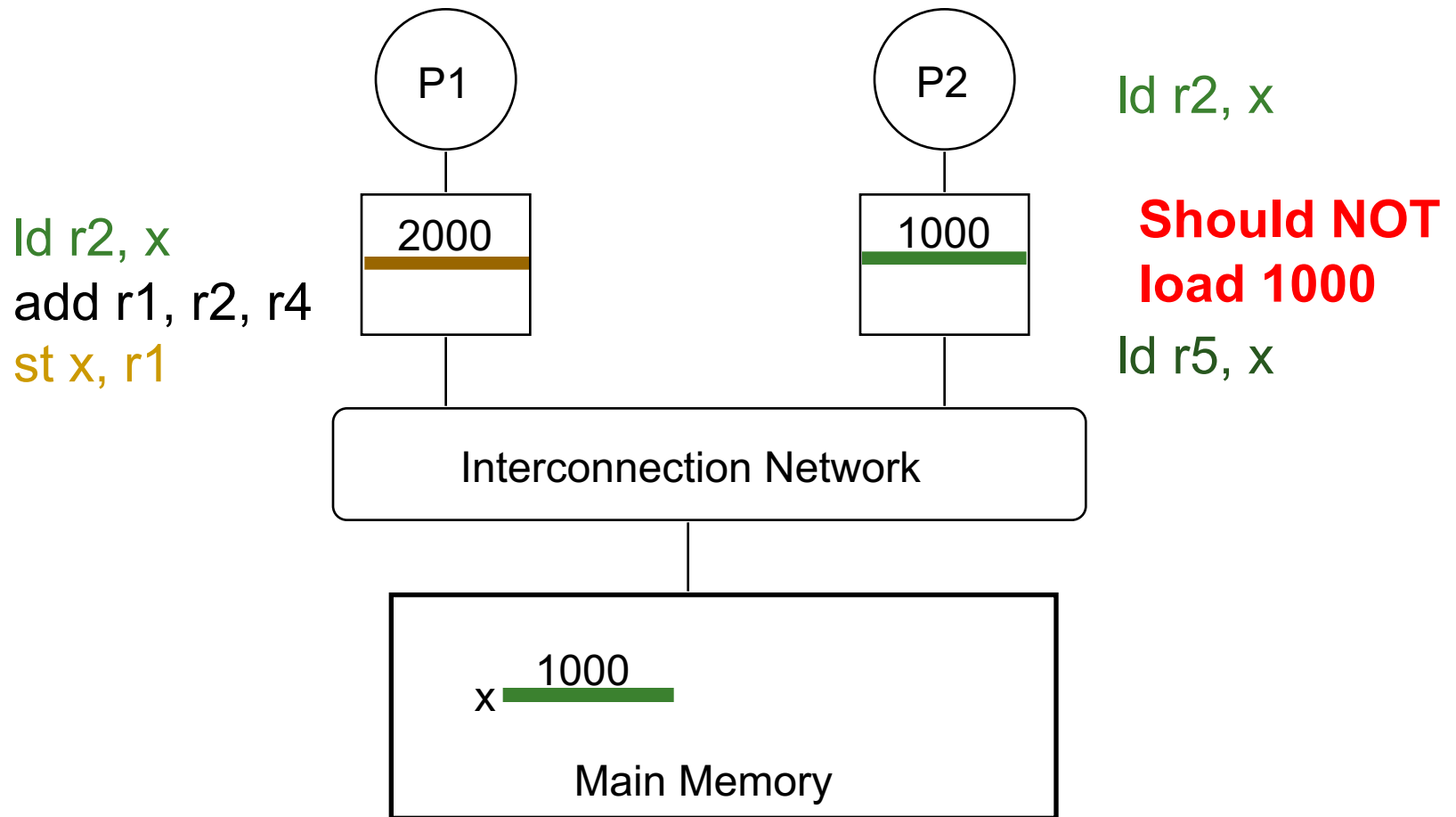
The Cache Coherence Problem



The Cache Coherence Problem



The Cache Coherence Problem



Cache Examples: For You to Study

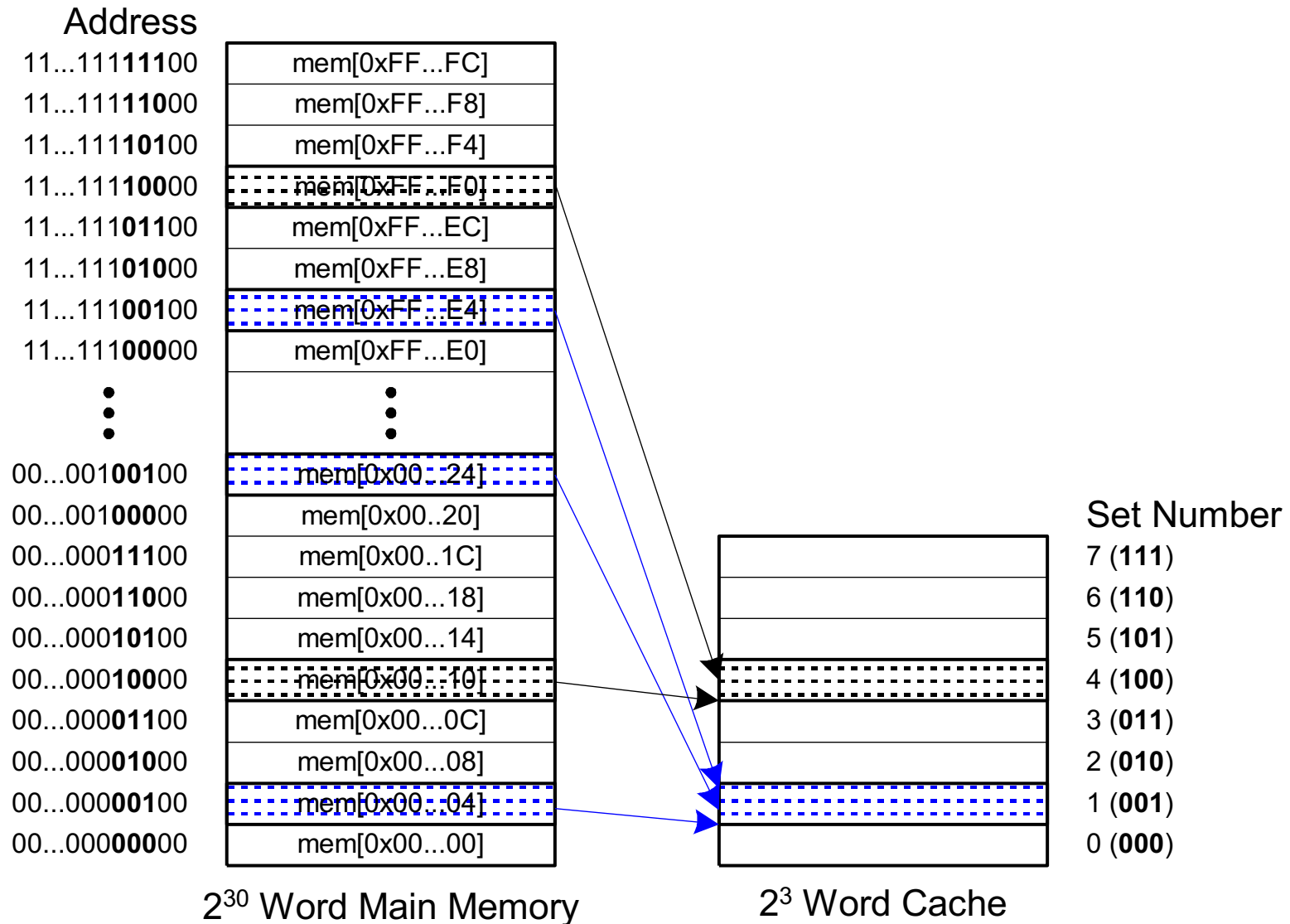
Cache Terminology

- Capacity (C):
 - the number of data bytes a cache stores
- Block size (b):
 - bytes of data brought into cache at once
- Number of blocks ($B = C/b$):
 - number of blocks in cache: $B = C/b$
- Degree of associativity (M):
 - number of blocks in a set
- Number of sets ($S = B/M$):
 - each memory address maps to exactly one cache set

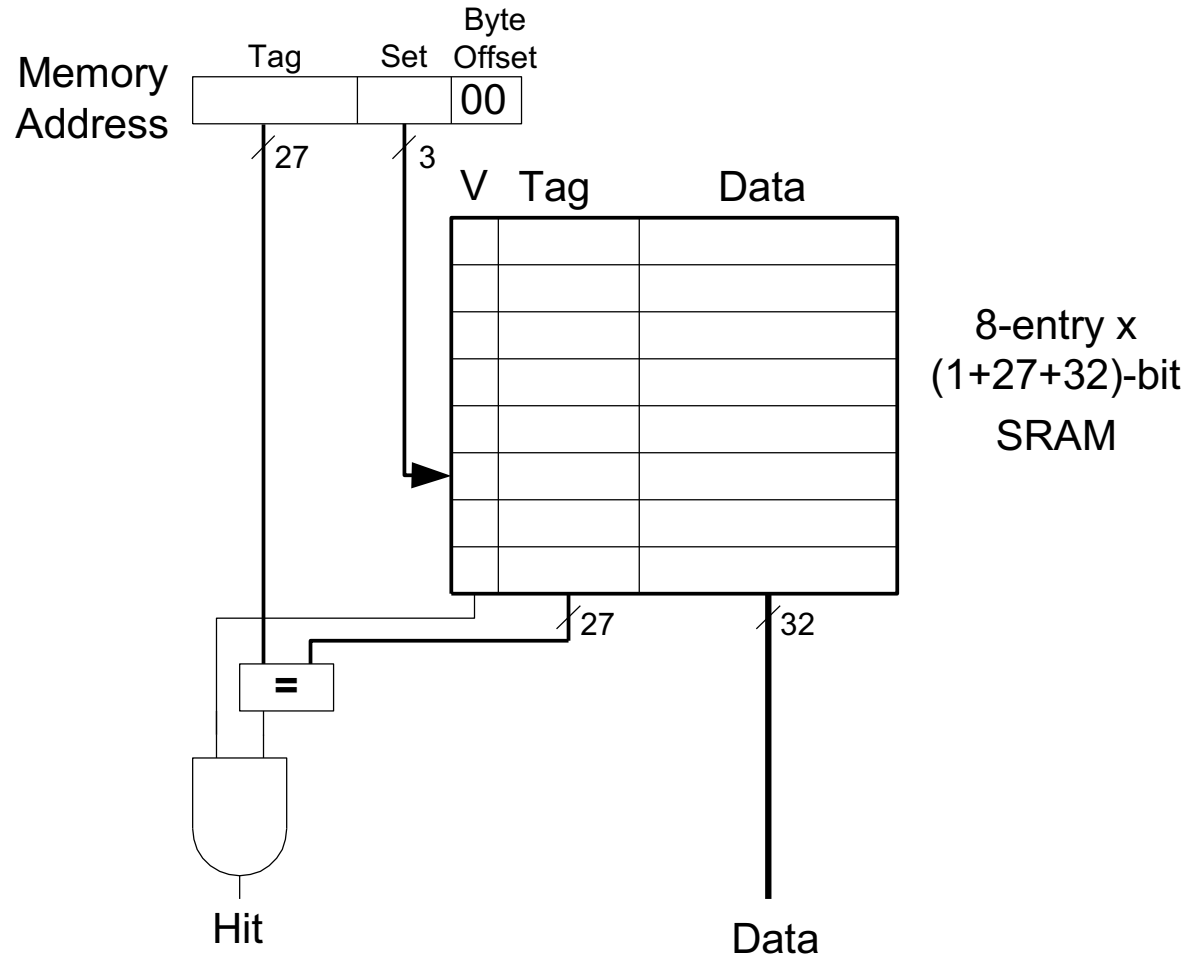
How is data found?

- Cache organized into S sets
- Each memory address maps to exactly one set
- Caches categorized by number of blocks in a set:
 - **Direct mapped**: 1 block per set
 - **N-way set associative**: N blocks per set
 - **Fully associative**: all cache blocks are in a single set
- Examine each organization for a cache with:
 - Capacity ($C = 8$ words)
 - Block size ($b = 1$ word)
 - So, number of blocks ($B = 8$)

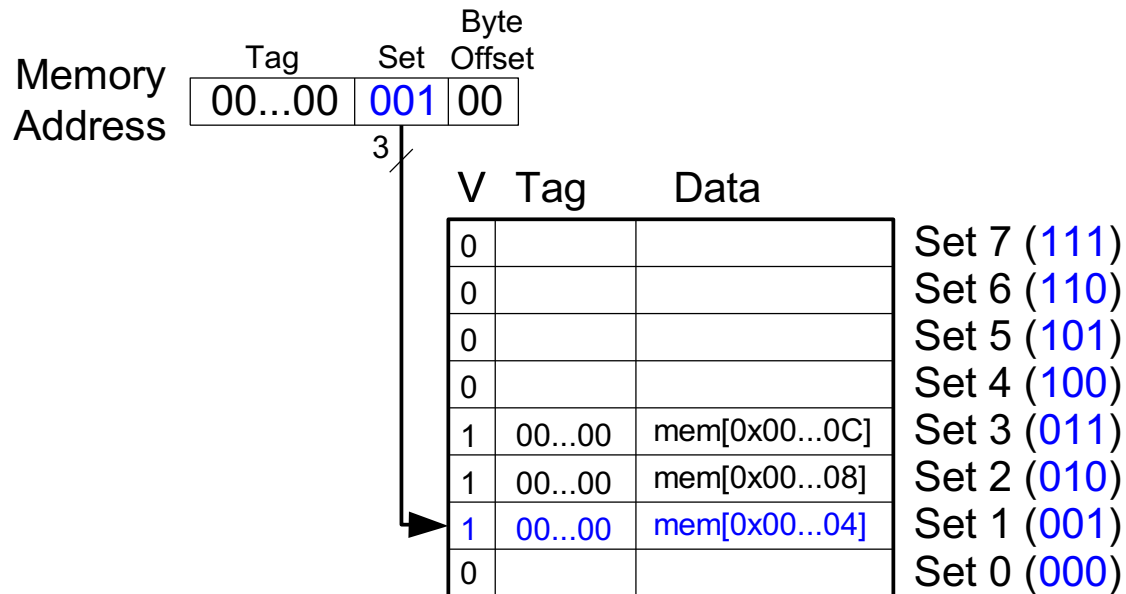
Direct Mapped Cache



Direct Mapped Cache Hardware



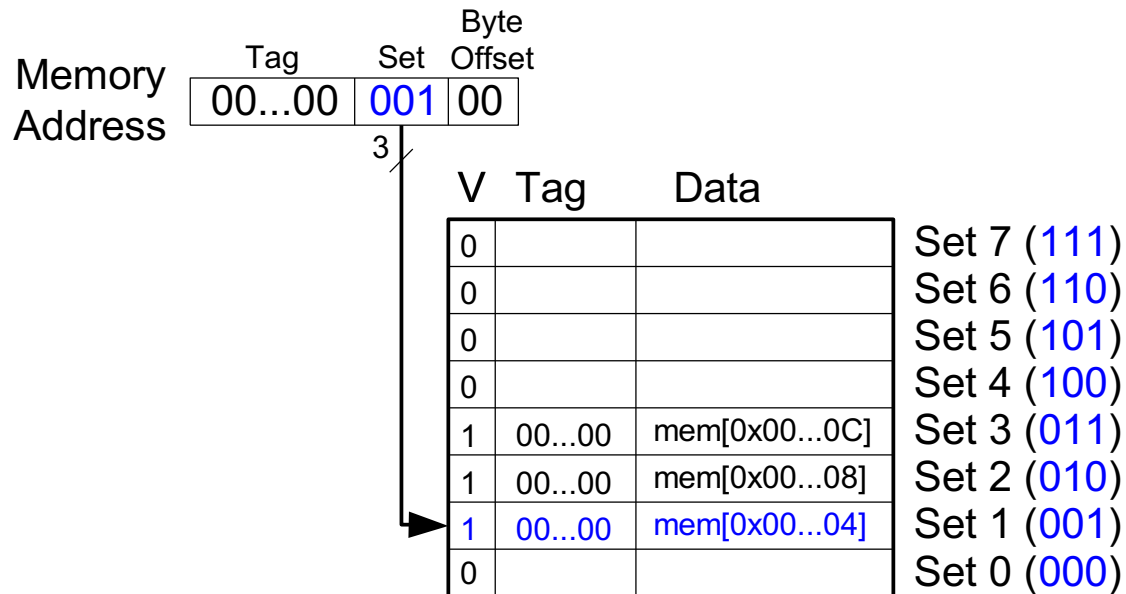
Direct Mapped Cache Performance



```
# MIPS assembly code
      addi $t0, $0, 5
loop: beq  $t0, $0, done
      lw   $t1, 0x4($0)
      lw   $t2, 0xC($0)
      lw   $t3, 0x8($0)
      addi $t0, $t0, -1
      j    loop
done:
```

Miss Rate =

Direct Mapped Cache Performance



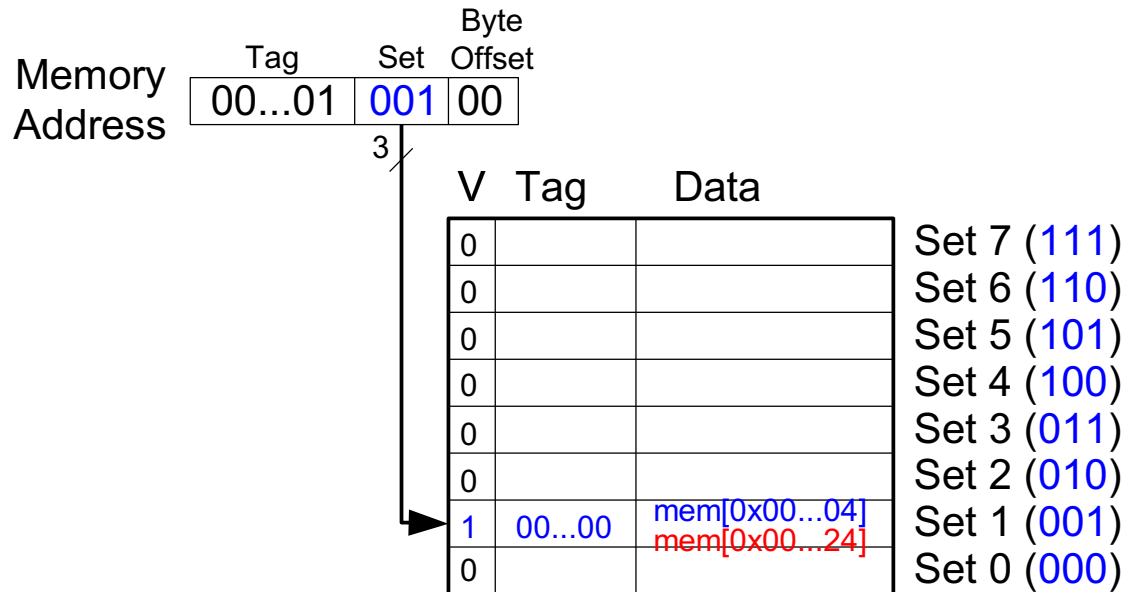
```
# MIPS assembly code
      addi $t0, $0, 5
loop:  beq  $t0, $0, done
      lw   $t1, 0x4($0)
      lw   $t2, 0xC($0)
      lw   $t3, 0x8($0)
      addi $t0, $t0, -1
      j    loop
done:
```

$$\text{Miss Rate} = 3/15 =$$

20%

Temporal Locality
Compulsory Misses

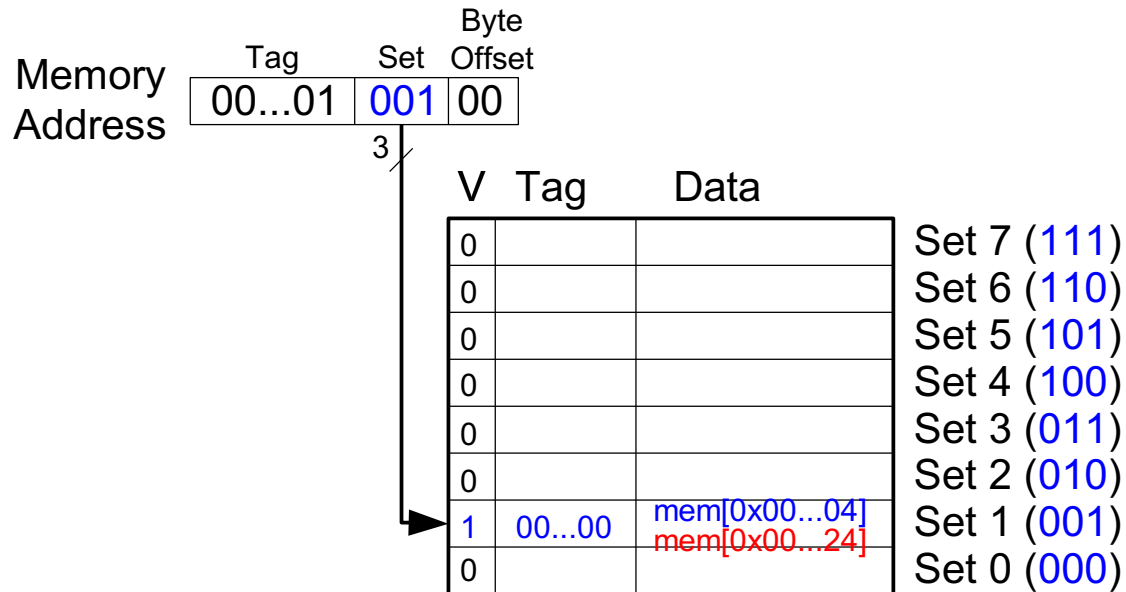
Direct Mapped Cache: Conflict



```
# MIPS assembly code
      addi $t0, $0, 5
loop: beq  $t0, $0, done
      lw   $t1, 0x4($0)
      lw   $t2, 0x24($0)
      addi $t0, $t0, -1
      j    loop
done:
```

Miss Rate =

Direct Mapped Cache: Conflict

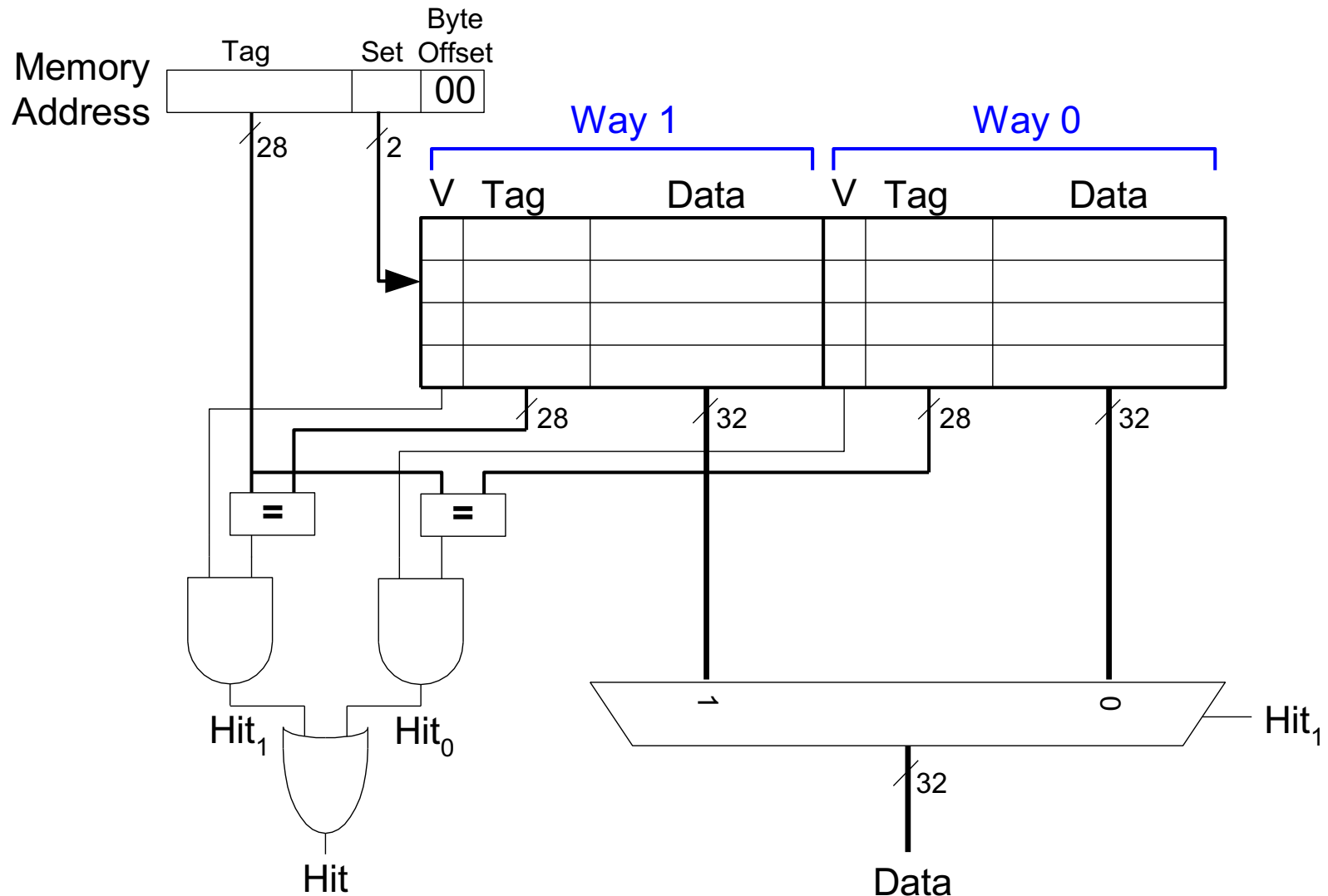


```
# MIPS assembly code
      addi $t0, $0, 5
loop: beq  $t0, $0, done
      lw   $t1, 0x4($0)
      lw   $t2, 0x24($0)
      addi $t0, $t0, -1
      j    loop
done:
```

Miss Rate = 10/10
= 100%

Conflict Misses

N-Way Set Associative Cache



N-way Set Associative Performance

MIPS assembly code

```
      addi $t0, $0, 5
loop:  beq  $t0, $0, done
      lw   $t1, 0x4($0)
      lw   $t2, 0x24($0)
      addi $t0, $t0, -1
      j    loop
done:
```

Miss Rate =

Way 1			Way 0			
V	Tag	Data	V	Tag	Data	
0			0			Set 3
0			0			Set 2
1	00...10	mem[0x00...24]	1	00...00	mem[0x00...04]	Set 1
0			0			Set 0

N-way Set Associative Performance

MIPS assembly code

```
      addi $t0, $0, 5
loop:  beq  $t0, $0, done
      lw   $t1, 0x4($0)
      lw   $t2, 0x24($0)
      addi $t0, $t0, -1
      j    loop
done:
```

Miss Rate = 2/10

= 20%

Associativity reduces
conflict misses

Way 1

Way 0

Way 1			Way 0			
V	Tag	Data	V	Tag	Data	
0			0			Set 3
0			0			Set 2
1	00...10	mem[0x00...24]	1	00...00	mem[0x00...04]	Set 1
0			0			Set 0

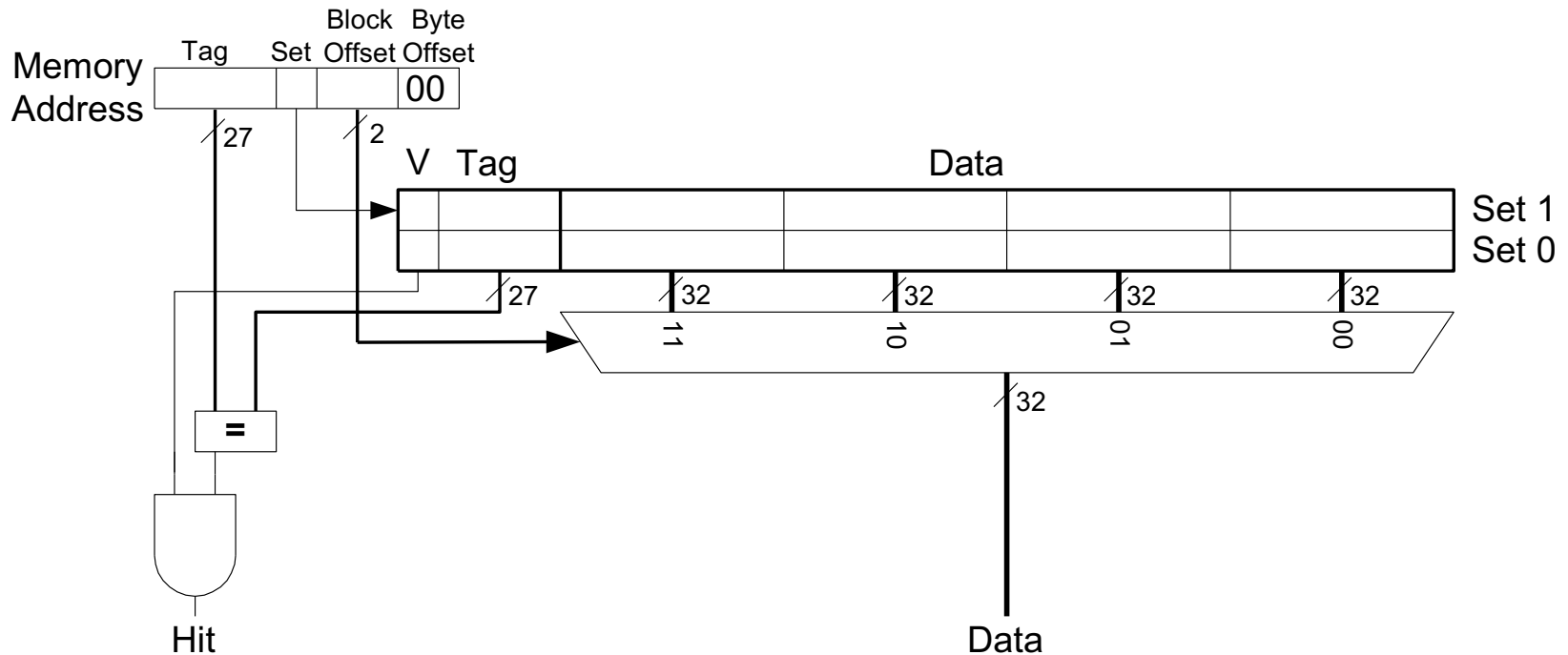
Fully Associative Cache

- No conflict misses
- Expensive to build

V	Tag	Data	V	Tag	Data	V	Tag	Data	V	Tag	Data	V	Tag	Data	V	Tag	Data	V	Tag	Data

Spatial Locality?

- Increase block size:
 - ❑ Block size, **$b = 4$** words
 - ❑ $C = 8$ words
 - ❑ Direct mapped (1 block per set)
 - ❑ Number of blocks, $B = C/b = 8/4 = 2$



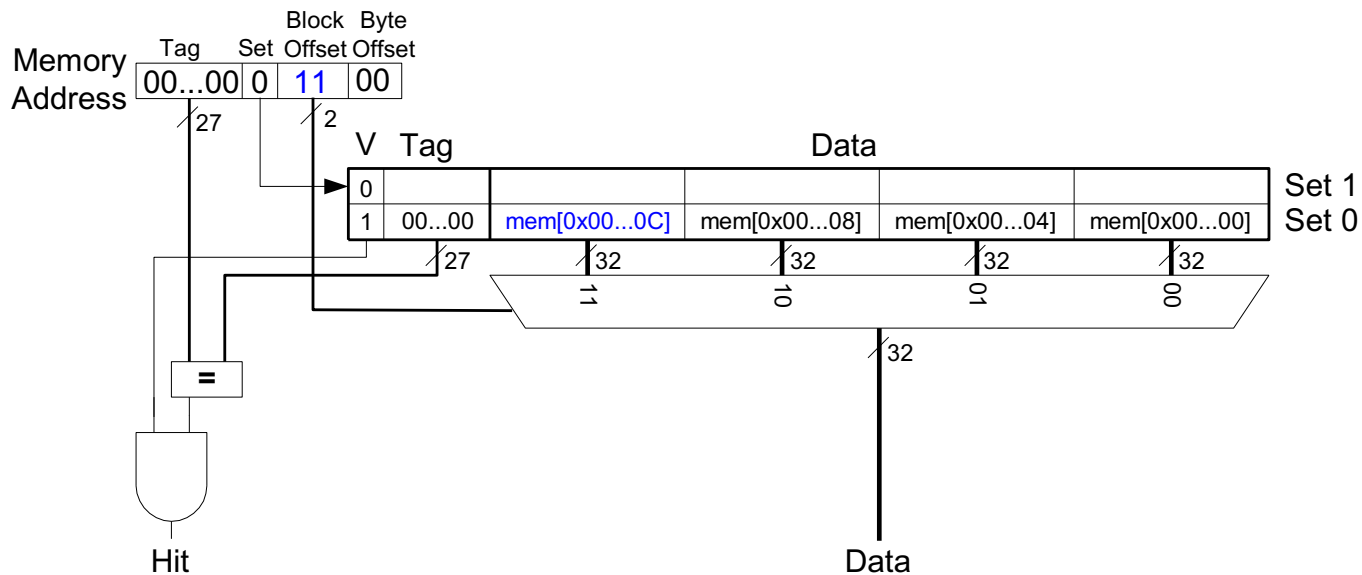
Direct Mapped Cache Performance

```

    addi $t0, $0, 5
loop: beq  $t0, $0, done
      lw   $t1, 0x4($0)
      lw   $t2, 0xC($0)
      lw   $t3, 0x8($0)
      addi $t0, $t0, -1
      j    loop
done:

```

Miss Rate =

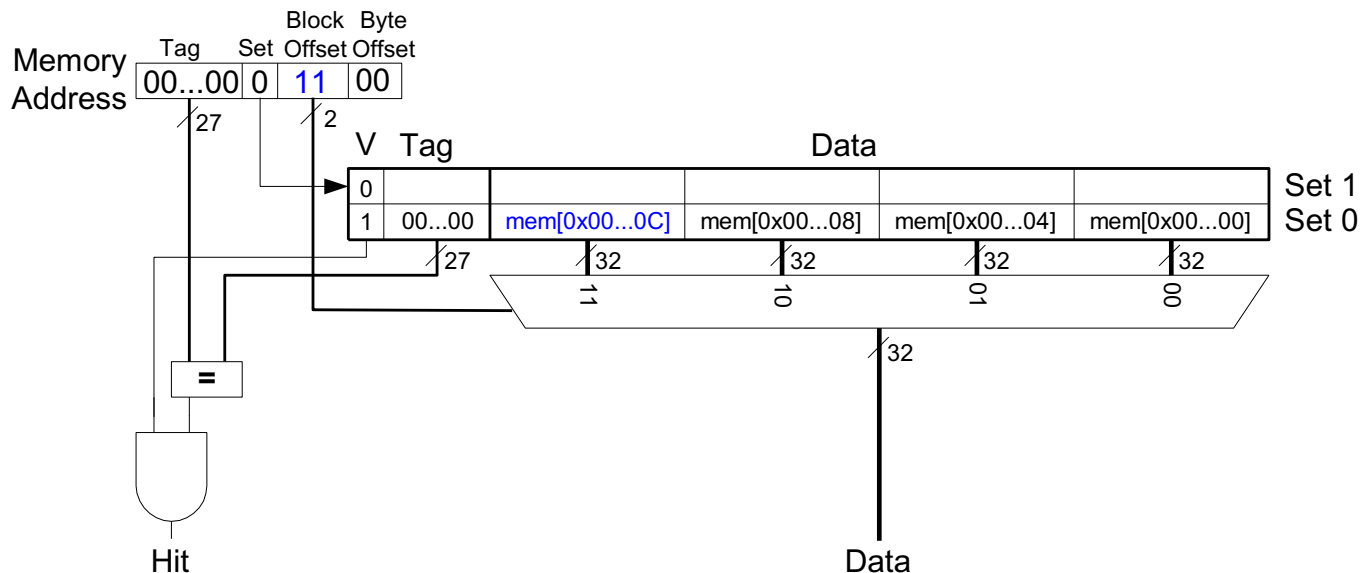


Direct Mapped Cache Performance

```
loop:    addi $t0, $0, 5
        beq  $t0, $0, done
        lw   $t1, 0x4($0)
        lw   $t2, 0xC($0)
        lw   $t3, 0x8($0)
        addi $t0, $t0, -1
        j    loop
done:
```

$$\text{Miss Rate} = 1/15 \\ = 6.67\%$$

Larger blocks reduce compulsory misses through spatial locality



Cache Organization Recap

■ Main Parameters

- ❑ Capacity: C
- ❑ Block size: b
- ❑ Number of blocks in cache: $B = C/b$
- ❑ Number of blocks in a set: N
- ❑ Number of Sets: $S = B/N$

Organization	Number of Ways (N)	Number of Sets (S = B/N)
Direct Mapped	1	B
N-Way Set Associative	$1 < N < B$	B / N
Fully Associative	B	1

Capacity Misses

- Cache is too small to hold all data of interest at one time
 - If the cache is full and program tries to access data X that is not in cache, cache must evict data Y to make room for X
 - **Capacity miss** occurs if program then tries to access Y again
 - X will be placed in a particular set based on its address
- In a **direct mapped** cache, there is only one place to put X
- In an **associative cache**, there are multiple ways where X could go in the set.
- How to choose Y to minimize chance of needing it again?
 - Least recently used (LRU) replacement: the least recently used block in a set is evicted when the cache is full.

Types of Misses

- **Compulsory**: first time data is accessed
- **Capacity**: cache too small to hold all data of interest
- **Conflict**: data of interest maps to same location in cache
- **Miss penalty**: time it takes to retrieve a block from lower level of hierarchy

LRU Replacement

```
# MIPS assembly
```

```
lw $t0, 0x04($0)
```

```
lw $t1, 0x24($0)
```

```
lw $t2, 0x54($0)
```

(a)

V	U	Tag	Data	V	Tag	Data	Set Number
							3 (11)
							2 (10)
							1 (01)
							0 (00)

(b)

V	U	Tag	Data	V	Tag	Data	Set Number
							3 (11)
							2 (10)
							1 (01)
							0 (00)

LRU Replacement

```
# MIPS assembly
```

```
lw $t0, 0x04($0)
lw $t1, 0x24($0)
lw $t2, 0x54($0)
```

Way 1				Way 0				
V	U	Tag	Data	V	Tag	Data		
0	0			0				Set 3 (11)
0	0			0				Set 2 (10)
1	0	00...010	mem[0x00...24]	1	00...000	mem[0x00...04]		Set 1 (01)
0	0			0				Set 0 (00)

(a)

Way 1				Way 0				
V	U	Tag	Data	V	Tag	Data		
0	0			0				Set 3 (11)
0	0			0				Set 2 (10)
1	1	00...010	mem[0x00...24]	1	00...101	mem[0x00...54]		Set 1 (01)
0	0			0				Set 0 (00)

(b)