## Final Exam

# Design of Digital Circuits (252-0028-00L) ETH Zürich, Spring 2019 

Prof. Onur Mutlu

| Prof. Onur Mutlu |  |  |
| ---: | :--- | :--- |
| Problem 1 (12 Points): | Boolean Algebra |  |
| Problem 2 (20 Points): | Verilog |  |
| Problem 3 (30 Points): | Finite State Machines (FSM) |  |
| Problem 4 (20 Points): | ISA vs. Microarchitecture |  |
| Problem 5 (20 Points): | Performance Evaluation |  |
| Problem 6 (40 Points): | Pipeline (Reverse Engineering) |  |
| Problem 7 (36 Points): | Tomasulo's Algorithm |  |
| Problem 8 (30 Points): | Systolic Arrays |  |
| Problem 9 (35 Points): | GPUs and SIMD |  |
| Problem 10 (40 Points): | Reverse Engineering Caches |  |
| Problem 11 (30 Points): | Dataflow |  |
| Problem 12 (BONUS: 30 Points): | Branch Prediction |  |
| Total (343 (313 + 30 bonus) Points): |  |  |

## Examination Rules:

1. Written exam, 180 minutes in total.
2. No books, no calculators, no computers or communication devices. 3 double-sided A4 sheets of handwritten notes are allowed.
3. Write all your answers on this document; space is reserved for your answers after each question.
4. You are provided with scratchpad sheets. Do not answer questions on them. We will not collect them.
5. Clearly indicate your final answer for each problem. Answers will only be evaluated if they are readable.
6. Put your Student ID card visible on the desk during the exam.
7. If you feel disturbed, immediately call an assistant.
8. Write with a black or blue pen (no pencil, no green or red color).
9. Show all your work. For some questions, you may get partial credit even if the end result is wrong due to a calculation mistake. If you make assumptions, state your assumptions clearly and precisely.
10. Please write your initials at the top of every page.

## Tips:

- Be cognizant of time. Do not spend too much time on one question.
- Be concise. You may be penalized for verbosity.
- Show work when needed. You will receive partial credit at the instructors' discretion.
- Write legibly. Show your final answer.
$\qquad$


## 1 Boolean Algebra [12 Points]

(a) [6 Points] Find the simplest sum-of-products representation of the following Boolean equation. Show your work step-by-step.

$$
F=(\bar{A}+B+C) \cdot(A+B+\bar{C}) \cdot C+A
$$

$\square$
(b) [6 Points] Convert the following Boolean equation so that it contains only NAND operations. Show your work step-by-step.

$$
F=\bar{A}+\overline{(B . C+\overline{A . C})}
$$

$\square$
$\qquad$

## 2 Verilog [20 Points]

Please answer the following three questions about Verilog.
(a) [5 Points] Does the following code result in a single D Flip-Flop with a synchronous active-low reset? Please explain your answer.

```
module mem (input clk, input reset, input [1:0] d, output reg [1:0] q);
always @ (posedge clk or negedge reset)
    begin
        if (!reset) q <= 0;
        else q <= d;
    end
endmodule
```


(b) [5 Points] Does the following code result in a sequential circuit or a combinational circuit? Please explain your answer.

```
module Mask (input [1:0] data_in, input mask, output reg [1:0] data_out);
always @ (*)
    begin
        data_out[1] = data_in[1];
        if (mask)
            data_out[0] = 0;
    end
endmodule
```

$\qquad$
(c) [10 Points] Is the following code syntactically correct? If not, please explain the mistake(s) and how to fix it/them.

```
module fulladd(input a, b, c, output reg s, c_out);
    assign s = a^b;
    assign c_out = (a & b) | (b & c) & (c & a);
endmodule
module top ( input wire [5:0] instr, input wire op, output z);
    reg[1:0] r1, r2;
    wire [3:0] w1, w2;
    fulladd FA1 (.a(instr[0]), .b(instr[1]), .c(instr[2]),
    .c_out(r1[1]), .z(r1[0]));
    fulladd FA2 (.a(instr[3]), .b(instr[4]), .c(instr[5]),
                        .z(r2[0]), .c_out(r2[1]));
    assign z = r1 | op;
    assign w1 = r1 + 1;
    assign w2 = r2 << 1;
    assign op = r1 ^ r2;
endmodule
```

$\qquad$

## 3 Finite State Machines (FSM) [30 Points]

You are given two one-bit input signals $\left(T_{A}\right.$ and $\left.T_{B}\right)$ and one one-bit output signal $(O)$ for the following modular equation: $2 N\left(T_{A}\right)+N\left(T_{B}\right) \equiv 2(\bmod 4)$. In this modular equation, $N\left(T_{A}\right)$ and $N\left(T_{B}\right)$ represent the total number of times the inputs $T_{A}$ and $T_{B}$ are high (i.e., logic 1) at each positive clock edge, respectively. The one-bit output signal, $O$, is set to 1 when the modular equation is satisfied (i.e., $\left.2 N\left(T_{A}\right)+N\left(T_{B}\right) \equiv 2(\bmod 4)\right)$, and 0 otherwise. An example that sets $O=1$ at the end of the fourth cycle would be:

- ( $1^{\text {st }}$ cycle) $T_{A}=0\left(N\left(T_{A}\right)=0\right), T_{B}=0\left(N\left(T_{B}\right)=0\right), 2 N\left(T_{A}\right)+N\left(T_{B}\right) \equiv 0(\bmod 4) \Rightarrow O=0$
- $\left(2^{\text {nd }}\right.$ cycle) $T_{A}=1\left(N\left(T_{A}\right)=1\right), T_{B}=1\left(N\left(T_{B}\right)=1\right), 2 N\left(T_{A}\right)+N\left(T_{B}\right) \equiv 3(\bmod 4) \Rightarrow O=0$
- ( $3^{\text {rd }}$ cycle) $T_{A}=1\left(N\left(T_{A}\right)=2\right), T_{B}=0\left(N\left(T_{B}\right)=1\right), 2 N\left(T_{A}\right)+N\left(T_{B}\right) \equiv 1(\bmod 4) \Rightarrow O=0$
- ( $4^{\text {th }}$ cycle) $T_{A}=0\left(N\left(T_{A}\right)=2\right), T_{B}=1\left(N\left(T_{B}\right)=2\right), 2 N\left(T_{A}\right)+N\left(T_{B}\right) \equiv 2(\bmod 4) \Rightarrow O=1$
(a) [10 Points] You are given a partial Moore machine state transition diagram that corresponds to the modular equation described above. However, the input labels of most of the transitions are still missing in this diagram. Please label the transitions with the correct inputs so that the FSM correctly implements the above specification.

$\qquad$
(b) [10 Points] Describe the FSM with Boolean equations assuming that the states are encoded with one-hot encoding. Assign state encodings while using the minimum possible number of bits to represent the states. Please indicate the values you assign to each state.
$\square$
(c) [10 Points] Describe the FSM with Boolean equations assuming that the states are encoded with binary encoding (i.e., fully encoding). Assign state encodings while using the minimum possible number of bits to represent the states. Please indicate the values you assign to each state.
$\square$
$\qquad$


## 4 ISA vs. Microarchitecture [20 Points]

A new CPU has two comprehensive user manuals available for purchase as shown in Table 1.

| Manual Title | Cost | Description |
| :---: | :---: | :---: |
| the_isa.pdf | CHF 1 million | describes the ISA in detail |
| the_microarchitecture.pdf | CHF 10 million | describes the microarchitecture in detail |

Table 1: Manual Costs

Unfortunately, the manuals are extremely expensive, and you can only afford one of the two. If both manuals might be useful, you would prefer the cheaper one.

For each of the following questions that you would like to answer, decide which manual is more likely to help. Note: we will subtract 1 point for each incorrect answer. For an unanswered question, you will get +0 points.

1. [2 Points] The latency of a branch predictor misprediction.
2. the_isa.pdf
3. the_microarchitecture.pdf
4. [2 Points] The size of a physical memory page.
5. the_isa.pdf
6. the_microarchitecture.pdf
7. [2 Points] The memory-mapped locations of exception vectors.
8. the_isa.pdf
9. the_microarchitecture.pdf
10. [2 Points] The function of each bit in a programmable branch-predictor configuration register.
```
1. the_isa.pdf 2. the_microarchitecture.pdf
```

5. [2 Points] The bit-width of the interface between the CPU and the L1 cache.
6. the_isa.pdf
7. the_microarchitecture.pdf
8. [2 Points] The number of pipeline stages in the CPU.
9. the_isa.pdf
10. the_microarchitecture.pdf
11. [2 Points] The order in which loads and stores are executed by a multi-core CPU.
12. the_isa.pdf
13. the_microarchitecture.pdf
14. [2 Points] The memory addressing modes available for arithmetic operations.
15. the_isa.pdf
16. the_microarchitecture.pdf
17. [2 Points] The program counter width.
18. the_isa.pdf
19. the_microarchitecture.pdf
20. [2 Points] The number of cache sets at each level of the cache hierarchy.
21. the_isa.pdf
22. the_microarchitecture.pdf
$\qquad$

## 5 Performance Evaluation [20 Points]

You are the leading engineer of a new processor. Both the design of the processor and the compiler for it are already done. Now, you need to decide if you will send the processor to manufacturing at its current stage or if you will delay the production to introduce last-minute improvements to the design. To make the decision, you meet with your team to brainstorm about how to improve the design. Together, after profiling the target applications for the processor, you come up with two options:

- Keep the current project. For version A of the processor, the clock frequency is 600 MHz , and the following measurements are obtained:

| Instruction Class | CPI | Frequency of Occurrence |
| :---: | :---: | :---: |
| A | 2 | $40 \%$ |
| B | 3 | $25 \%$ |
| C | 3 | $25 \%$ |
| D | 7 | $10 \%$ |

- Include optimizations to the design. For version B of the processor, the clock frequency is 700 MHz . The ISA for processor B includes three new types of instructions. Those three new types of instructions increase the total number of executed instructions for processor B by $50 \%$, in comparison to processor A. The following measurements are obtained:

| Instruction Class | CPI | Frequency of Occurrence |
| :---: | :---: | :---: |
| A | 2 | $15 \%$ |
| B | 2 | $15 \%$ |
| C | 4 | $10 \%$ |
| D | 6 | $10 \%$ |
| E | 1 | $10 \%$ |
| F | 2 | $20 \%$ |
| G | 2 | $20 \%$ |

(a) [7 Points] What is the CPI of each version? Show your work.
$C P I_{A}$ :
$\square$
$C P I_{B}$ :
$\square$

(b) [6 Points] What are the MIPS (Million Instructions Per Second) of each version? Show your work.
$\qquad$

## $M I P S_{A}:$

$\square$
$M I P S_{B}:$
$\square$
$\square$
(c) [7 Points] Considering your team is aiming to release to the market the processor that gives better performance when executing the target application, which processor version will you choose as the final design? Show your work.
$\square$
$\qquad$

## 6 Pipeline (Reverse Engineering) [40 Points]

The following piece of code runs on a pipelined microprocessor as shown in the table (F: Fetch, D: Decode, E: Execute, M: Memory, W: Write back). Instructions are in the form "Instruction Destination, Source1, Source2." For example, "ADD A, B, C" means A $\leftarrow \mathrm{B}+\mathrm{C}$.

|  | Cycles | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | MUL R5, R6, R7 | F | D | E1 | E2 | E3 | E4 | M | W |  |  |  |  |  |  |  |  |  |  |
| 1 | ADD R4, R6, R7 |  | F | D | E1 | E2 | E3 | - | M | W |  |  |  |  |  |  |  |  |  |
| 2 | ADD R5, R5, R6 |  |  | F | D | - | - | E1 | E2 | E3 | M | W |  |  |  |  |  |  |  |
| 3 | MUL R4, R7, R7 |  |  |  | F | - | - | D | E1 | E2 | E3 | E4 | M | W |  |  |  |  |  |
| 4 | ADD R6, R7, R5 |  |  |  |  |  |  | F | D | - | E1 | E2 | E3 | M | W |  |  |  |  |
| 5 | ADD R3, R0, R6 |  |  |  |  |  |  |  | F | - | D | - | - | E1 | E2 | E3 | M | W |  |
| 6 | ADD R7, R1, R4 |  |  |  |  |  |  |  |  |  | F | - | - | D | E1 | E2 | E3 | M | W |

Use this information to reverse engineer the architecture of this microprocessor to answer the following questions. Answer the questions as precise as possible with the provided information. If the provided information is not sufficient to answer a question, answer "Unknown" and explain your reasoning clearly.
(a) [5 Points] How many cycles does it take for an adder and for a multiplier to calculate a result?
$\square$
(b) [5 Points] What is the minimum number of register file read/write ports that this architecture implements? Explain.

(c) [5 Points] Can we reduce the execution time of this code by enabling more read/write ports in the register file? Explain.

(d) [5 Points] Does this architecture implement any data forwarding? If so, how is data forwarding done between pipeline stages? Explain.
$\square$
$\qquad$
(e) [5 Points] Is it possible to run this code faster by adding more data forwarding paths? If it is, how? Explain.
$\square$
(f) [5 Points] Is there internal forwarding in the register file? If there is not, how would the execution time of the same program change by enabling internal forwarding in the register file? Explain.
$\qquad$
(g) [10 Points] Optimize the assembly code in order to reduce the number of stall cycles. You are allowed to reorder, add, or remove ADD and MUL instructions. You are expected to achieve the minimum possible execution time. Make sure that the register values that the optimized code generates at the end of its execution are identical to the register values that the original code generates at the end of its execution. Justify each individual change you make. Show the execution timeline of each instruction and what stage it is in the table below. (Notice that the table below consists of two parts: the first ten cycles at the top, and the next ten cycles at the bottom.)

| Instructions |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |

$\qquad$

## 7 Tomasulo's Algorithm [36 Points]

In this problem, we consider an in-order fetch, out-of-order dispatch, and out-of-order retirement execution engine that employs Tomasulo's algorithm. This engine behaves as follows:

- The engine has four main pipeline stages: Fetch (F), Decode (D), Execute (E), and Write-back (W).
- The engine can fetch FW instructions per cycle, decode DW instructions per cycle, and write back the result of RW instructions per cycle.
- The engine has two execution units: 1) an integer $A L U$ for executing integer instructions (i.e., addition and multiplication) and 2) a memory unit for executing load/store instructions.
- Each execution unit has an R-entry reservation station.
- An instruction always allocates the first available entry of the reservation station (in top-to-bottom order) of the corresponding execution unit.

The reservation stations are all initally empty. The processor fetches and executes six instructions. Table 2 shows the six instructions and their execution diagram.

Using the information provided above and in Table 2 (see the next page), fill in the blanks below with the configuration of the out-of-order microarchitecture. Write "Unknown" if the corresponding configuration cannot be determined using the information provided in the question.

$\qquad$

| Instruction/Cycle: | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1: $\mathrm{ADD} \mathrm{R} 1 \leftarrow \mathrm{R} 0, \mathrm{R} 1$ | F | D | E1 | E2 | W |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 2: LD R2 $\leftarrow[\mathrm{R} 1]$ | F | D | - | - | - | E1 | E2 | E3 | E4 | E5 | E6 | E7 | E8 | E9 | E10 | W |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 3: ADDI R1 $\leftarrow$ R1, \#4 |  | F | D | - | - | E1 | E2 | W |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 4: $\mathrm{LD} \mathrm{R} 3 \leftarrow[\mathrm{R} 1]$ |  | F | D | - | - | - | - | - | E1 | E2 | E3 | E4 | E5 | E6 | E7 | E8 | E9 | E10 | W |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 5: MUL R4 $\leftarrow \mathrm{R} 2, \mathrm{R} 3$ |  |  | F | - | - | D | - | - | - | - | - | - | - | - | - | - | - | - | - | E1 | E2 | W |  |  |  |  |  |  |  |  |  |  |  |
| 6: $\mathrm{ST}[\mathrm{R} 0] \leftarrow \mathrm{R} 4$ |  |  | F | - | - | - | - | - | - | - | - | - | - | - | - | - | D | - | - | - | - | - | E1 | E2 | E3 | E4 | E5 | E6 | E7 | E8 | E9 | E10 | W |

Table 2: Execution diagram of the six instructions.
$\qquad$

## 8 Systolic Arrays [30 Points]

A systolic array consists of $3 \times 4$ Processing Elements (PEs), interconnected as shown in Figure 1. The inputs of the systolic array are labeled as H0, H1, H2 and V0,V1,V2,V3. Figure 2 shows the PE logic, which performs a multiply and accumulate operation (MAC), and it saves the result in an internal register (reg). Figure 2 also shows how each PE propagates its inputs. We make the following assumptions:

- The latency of each MAC is one cycle.
- The propagation of the values from $i_{0}$ to $o_{0}$, and from $i_{1}$ to $o_{1}$, takes one cycle.
- The initial value of all registers is zero.
- You can input a value more than once in the systolic array.


Figure 1: PE array

Processing Element (PE)


Figure 2: Processing Element (PE)

Your goal is to use this systolic array to perform the convolution of a 3x3 image (matrix I) with three 2 x 2 filters (matrices F, G, and H), to obtain three outputs (matrices $\mathrm{O}, \mathrm{U}$, and E ):

| $\begin{gathered} I_{00} \\ I_{10} \\ I_{20} \end{gathered}$ | $\begin{aligned} & I_{01} \\ & I_{11} \\ & I_{21} \end{aligned}$ | $\begin{aligned} & I_{02} \\ & I_{12} \\ & I_{22} \end{aligned}$ | $\circledast$ | $\begin{aligned} & F_{00} \\ & F_{10} \end{aligned}$ | $\begin{aligned} & F_{01} \\ & F_{11} \end{aligned}$ | $=$ | $\begin{aligned} & O_{00} \\ & O_{10} \end{aligned}$ | $\begin{aligned} & O_{01} \\ & O_{11} \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} I_{00} \\ I_{10} \\ I_{20} \end{gathered}$ | $\begin{aligned} & I_{01} \\ & I_{11} \\ & I_{21} \end{aligned}$ | $\begin{aligned} & I_{02} \\ & I_{12} \\ & I_{22} \end{aligned}$ | $*$ | $\begin{aligned} & G_{00} \\ & G_{10} \end{aligned}$ | $\begin{aligned} & G_{01} \\ & G_{11} \end{aligned}$ |  | $\begin{aligned} & U_{00} \\ & U_{10} \end{aligned}$ | $\begin{aligned} & U_{01} \\ & U_{11} \end{aligned}$ |
| $I_{00}$ <br> $I_{10}$ <br> $I_{20}$ | $\begin{aligned} & I_{01} \\ & I_{11} \\ & I_{22} \end{aligned}$ | $\begin{aligned} & I_{02} \\ & I_{12} \\ & I_{22} \end{aligned}$ | $\circledast$ | $\begin{aligned} & H_{00} \\ & H_{10} \end{aligned}$ | $\begin{aligned} & H_{01} \\ & H_{11} \end{aligned}$ | $=$ | $E_{00}$ $E_{10}$ | $\begin{aligned} & E_{01} \\ & E_{11} \end{aligned}$ |

As an example, the convolution of the matrix I with the filter F is computed as follows:

- $O_{00}=I_{00} * F_{00}+I_{01} * F_{01}+I_{10} * F_{10}+I_{11} * F_{11}$
- $O_{01}=I_{01} * F_{00}+I_{02} * F_{01}+I_{11} * F_{10}+I_{12} * F_{11}$
- $O_{10}=I_{10} * F_{00}+I_{11} * F_{01}+I_{20} * F_{10}+I_{21} * F_{11}$
- $O_{11}=I_{11} * F_{00}+I_{12} * F_{01}+I_{21} * F_{10}+I_{22} * F_{11}$
$\qquad$

You should compute the three convolutions in the minimum possible amount of cycles. Fill the following table with:

1. The input values (matrices I, F, G, and H) in the correct input ports of the systolic array (the values can be repeated).
2. The output values and the corresponding PE where the outputs (matrices $\mathrm{O}, \mathrm{U}$, and E ) are generated.

Fill the gaps only with relevant information.


$\qquad$

## 9 GPUs and SIMD [35 Points]

We define the SIMD utilization of a program that runs on a GPU as the fraction of SIMD lanes that are kept busy with active threads during the run of a program. As we saw in lecture and practice exercises, the SIMD utilization of a program is computed across the complete run of the program.

The following code segment is run on a GPU. Each thread executes a single iteration of the shown loop. Assume that the data values of the arrays A and B are already in vector registers so there are no loads and stores in this program. (Hint: Notice that there are 4 instructions in each iteration.) A warp in the GPU consists of 32 threads, and there are 32 SIMD lanes in the GPU.

```
for (i = 0; i < 1026; i++) {
    if (A[i] < 33) { // Instruction 1
        B[i] = A[i] << 1; // Instruction 2
    }
    if (A[i] > 33) { // Instruction 3
        B[i] = A[i] >> 1; // Instruction 4
    }
}
```

Please answer the following five questions.
(a) [2 Points] How many warps does it take to execute this program?
(b) [10 Points] What is the maximum possible SIMD utilization of this program? Show your work. (Hint: The warp scheduler does not issue instructions where no threads are active).
$\qquad$
(c) [5 Points] Please describe what needs to be true about array A to reach the maximum possible SIMD utilization asked in part (b). (Please cover all cases in your answer.)
$\square$
(d) [13 Points] What is the minimum possible SIMD utilization of this program? Show your work.

(e) [5 Points] Please describe what needs to be true about array A to reach the minimum possible SIMD utilization asked in part (d). (Please cover all cases in your answer.)
$\square$
$\qquad$

## 10 Reverse Engineering Caches [40 Points]

You are trying to reverse-engineer the characteristics of a cache in a system, so that you can design a more efficient, machine-specific implementation of an algorithm you are working on. To do so, you have come up with three sequences of memory accesses to various bytes in the system in an attempt to determine the following four cache characteristics:

- Cache block size $(8,16,32,64$, or 128 B).
- Cache associativity (1-, 2-, 4-, or 8 -way).
- Cache size ( 4 or 8 KB ).
- Cache replacement policy (LRU or FIFO).

The only statistic that you can collect on this system is cache hit rate after performing each sequence of memory accesses. Here is what you observe:

| Sequence | Addresses Accessed (Oldest $\rightarrow$ Youngest) |  |  |  |  |  |  |  |  |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1. | 31 | 8192 | 63 | 16384 | 4096 | 8192 | 64 | 16384 | $3 / 8$ |
| 2. | 32768 | 0 | 129 | 1024 | 3072 | 8192 |  | 0 |  |
| 3. | 0 | 4 | 8 | 4096 | 64 | 128 |  | 1 |  |

Assume that the cache is initially empty at the beginning of the first sequence, but not at the beginning of the second and third sequences. The sequences are executed back-to-back, i.e., no other accesses take place in between the three sequences. Thus, at the beginning of the second (third) sequence, the contents are the same as at the end of the first (second) sequence.

Based on what you observe, what are the following characteristics of the cache? Explain to get points. If a characteristic cannot be known, then write "Unknown" and explain.
(a) [10 Points] Cache block size $(8,16,32,64$, or 128 B)?
$\square$
$\qquad$
(b) [10 Points] Cache associativity (1-, 2-, 4-, or 8-way)?
$\square$
(c) [10 Points] Cache size ( 4 or 8 KB )?
$\square$
(d) [10 Points] Cache replacement policy (LRU or FIFO)?
$\qquad$

## 11 Dataflow [30 Points]

- We define the switch node in Figure 3 to have 2 inputs (I, Ctrl) and 1 output ( $\mathbf{O}$ ). The Ctrl input always enters perpendicularly to the switch node. If the Ctrl input has a True token (i.e., a token with a value of 1 ), the $\mathbf{O}$ wire propagates the value on the $\mathbf{I}$ wire. Else, the 2 input tokens ( $\mathbf{I}$, $\mathbf{C t r l})$ are consumed, and no token is generated at the output $(\mathbf{O})$.
- We define the inverter node in Figure 4 to have 1 input $(\mathbf{I})$ and 1 output $(\mathbf{O})$. The node negates the input token (i.e., $\mathrm{O}=!\mathrm{I}$ ).
- We define the TF node in Figure 5 to have 3 inputs ( $I_{F}, I_{T}, \mathbf{C t r l}$ ) and 1 output ( $\mathbf{O}$ ). When Ctrl is set to True, $\mathbf{O}$ takes $I_{T}$. When Ctrl is set to False, $\mathbf{O}$ takes $I_{F}$.
- The $\geq$ node outputs True only when the left input is greater than or equal to the right input.
- The +1 node outputs the input plus one.
- The + node outputs the sum of the two inputs.
- A node generates an output token when tokens exist at every input, and all input tokens are consumed.
- Where a single wire splits into multiple wires, the token travelling on the wire is replicated to all wires.


Figure 3: Switch Node


Figure 4: Inverter Node


Figure 5: TF Node

Consider the dataflow graph on the following page. Numbers in dashed boxes represent tokens (with the value indicated by the number) in the initial state. The $\mathbf{X}$ and $\mathbf{Y}$ inputs automatically produce tokens as soon as the previous token on the wire is consumed. The order of these tokens follows the pattern (note, the following are all single digit values spaced appropriately for the reader to easily notice the pattern):

$$
\text { X: } 001011011101111
$$

$$
\mathbf{Y}: 122333444455555
$$

Consider the dataflow graph on the following page. Please clearly describe the sequence of tokens generated at the output (OUT).
$\qquad$

$\qquad$

## 12 BONUS: Branch Prediction [30 Points]

Assume a machine with a two-bit global history register (GHR) shared by all branches, which starts with Not Taken, Not Taken (2'b00). Each pattern history table entry (PHTE) contains a 2-bit saturating counter. The saturating counter values are as follows:

2'b00 - Strongly Not Taken
2'b01 - Weakly Not Taken
2'b10 - Weakly Taken
2'b11 - Strongly Taken
Assume the following piece of code runs on this machine. The code has two branches (labeled B1 and B2). When we say that a branch is taken, we mean that the code inside the curly brackets is executed. For the following questions, assume that this is the only block of code that will ever be run, and the loop-condition branch (B1) is resolved first in the iteration before the if-condition branch (B2).

```
for (int i = 0; i < 1000000; i++) { /* B1 */
    /* TAKEN PATH for B1 */
    if (i % 3 == 0) { /* B2 */
        j[i] = k[i] -1; /* TAKEN PATH for B2 */
        }
}
```

(a) [20 Points] Is it possible to observe that the branch predictor mispredicts $100 \%$ of the times in the first 5 iterations of the loop? If yes, fill in the table below with all possible initial values each entry can take. We represent Not Taken with N, and Taken with T.

Table 3: PHT

| PHT Entry | Value |
| :---: | :---: |
| TT |  |
| TN |  |
| NT |  |
| NN |  |

Show your work here.
$\square$
(b) [10 Points] At steady-state, we observe the following pattern which repeats over time: TTTNTN, with T representing Taken, and N representing Not Taken. When GHR pattern equals to NT or TT, the predictor will observe that the branch outcome will be either T or N. Therefore, no matter what the initial values for these two entries are in the pattern history table (PHT), only one of the branches can be predicted correctly. Thus prediction accuracy will never reach $100 \%$. Explain how using local history registers instead of the global history register will help bring the prediction accuracy up to $100 \%$ during the steady state, by showing what each PHTE will saturate to.

