Digital Design & Computer Arch.

Lecture 8: Timing and Verification

Prof. Onur Mutlu

ETH Zürich
Spring 2022
18 March 2022

Readings (This Week)

- Hardware Description Languages and Verilog
 - H&H Chapter 4 in full
- Timing and Verification
 - H&H Chapters 2.9 and 3.5 + (start Chapter 5)

- By tomorrow, make sure you are done with
 - P&P Chapters 1-3 + H&H Chapters 1-4

Readings (Next Week)

- Von Neumann Model, LC-3, and MIPS
 - P&P, Chapter 4, 5
 - H&H, Chapter 6
 - P&P, Appendices A and C (ISA and microarchitecture of LC-3)
 - H&H, Appendix B (MIPS instructions)
- Programming
 - P&P, Chapter 6
- Recommended: Digital Building Blocks
 - H&H, Chapter 5

Assignment: Lecture Video (April 1)

- Why study computer architecture? Why is it important?
- Future Computing Platforms: Challenges & Opportunities

Required Assignment

- Watch one of Prof. Mutlu's lectures and analyze either (or both)
- https://www.youtube.com/watch?v=kgiZlSOcGFM (May 2017)
- https://www.youtube.com/watch?v=mskTeNnf-i0 (Feb 2021)

Optional Assignment – for 1% extra credit

- Write a 1-page summary of one of the lectures and email us
 - What are your key takeaways?
 - What did you learn?
 - What did you like or dislike?
 - Submit your summary to <u>Moodle</u> by April 1

Extra Assignment: Moore's Law (I)

- Paper review
- G.E. Moore. "Cramming more components onto integrated circuits," Electronics magazine, 1965

- Optional Assignment for 1% extra credit
 - Write a 1-page review
 - Upload PDF file to Moodle Deadline: April 7

 I strongly recommend that you follow my guidelines for (paper) review (see next slide)

Extra Assignment 2: Moore's Law (II)

- Guidelines on how to review papers critically
 - Guideline slides: pdf ppt
 - Video: https://www.youtube.com/watch?v=tOL6FANAJ8c
 - Example reviews on "Main Memory Scaling: Challenges and Solution Directions" (link to the paper)
 - Review 1
 - Review 2
 - Example review on "Staged memory scheduling: Achieving high performance and scalability in heterogeneous systems" (link to the paper)
 - Review 1

Agenda

Wrap up FSMs in Verilog

Timing in combinational circuits

Timing in sequential circuits

Circuit verification

Wrap Up: FSMs in Verilog

Recall: Why Use (Non)-Blocking Statements

- Non-blocking statements allow operating on "old" values
 - Enable easy sequential logic descriptions
- Blocking statements allow a sequence of operations
 - Allow operating on immediately updated values
 - More like a "software" programming language
- If the sensitivity list is correct, blocks with non-blocking statements will always evaluate to the same result
 - This may require some additional iterations

Rules for Signal Assignment

 Use always @(posedge clk) and non-blocking assignments (<=) to model synchronous sequential logic

```
always @ (posedge clk)
q <= d; // non-blocking</pre>
```

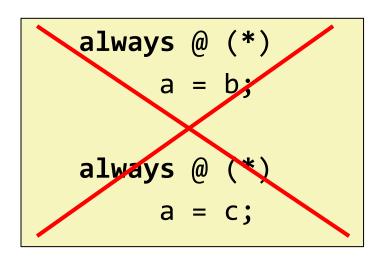
 Use continuous assignments (assign) to model simple combinational logic

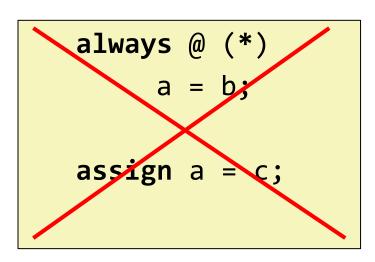
```
assign y = a & b;
```

Rules for Signal Assignment (Cont.)

 Use always @ (*) and blocking assignments (=) to model more complicated combinational logic.

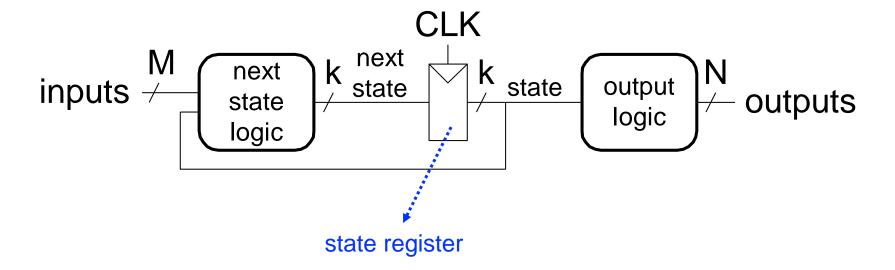
 You cannot make assignments to the same signal in more than one always block or in a continuous assignment





Recall: Finite State Machines (FSMs)

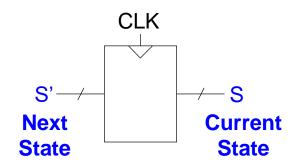
- Each FSM consists of three separate parts:
 - next state logic
 - state register
 - output logic



Recall: Finite State Machines (FSMs) Comprise

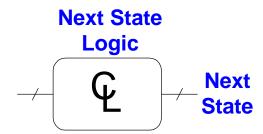
Sequential circuits

- State register(s)
 - Store the current state and
 - Load the next state at the clock edge

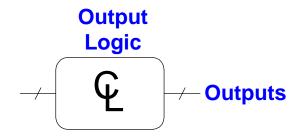


Combinational Circuits

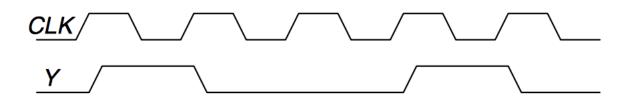
- Next state logic
 - Determines what the next state will be



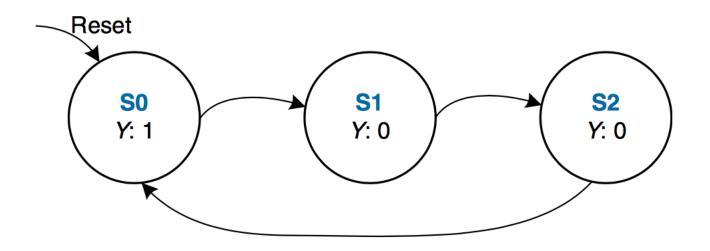
- Output logic
 - Generates the outputs



FSM Example 1: Divide the Clock Frequency by 3



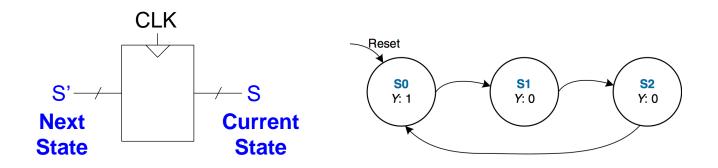
The output Y is HIGH for **one clock cycle out of every 3**. In other words, the output **divides the frequency of the clock by 3**.



Implementing FSM Example 1: Definitions

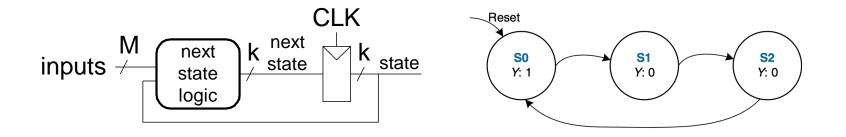
- We define state and nextstate as 2-bit reg
- The parameter descriptions are optional, it makes reading easier

Implementing FSM Example 1: State Register

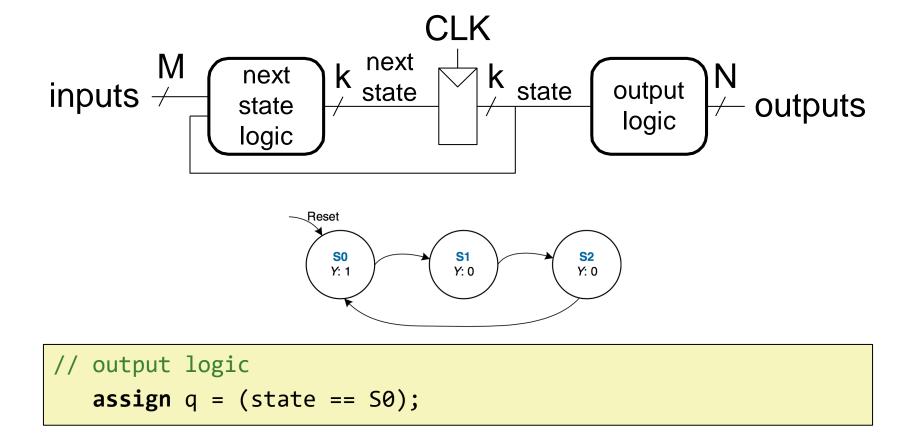


- This part defines the state register (memorizing process)
- Sensitive to only clk, reset
- In this example, reset is active when it is '1' (active-high)

Implementing FSM Example 1: Next State Logic



Implementing FSM Example 1: Output Logic



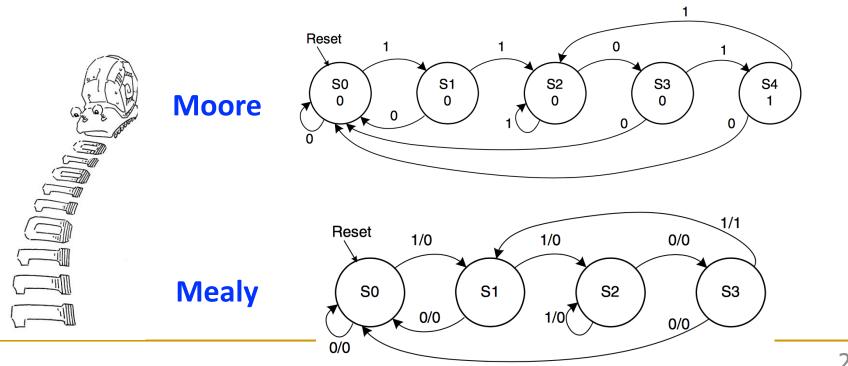
- In this example, output depends only on state
 - Moore type FSM

Implementation of FSM Example 1

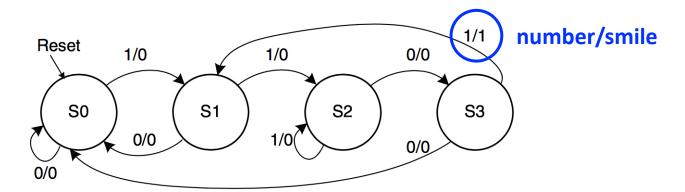
```
module divideby3FSM (input clk, input reset, output q);
  reg [1:0] state, nextstate;
  parameter S0 = 2'b00; parameter S1 = 2'b01; parameter S2 = 2'b10;
  always @ (posedge clk, posedge reset) // state register
     if (reset) state <= S0;</pre>
     always @ (*)
                                     // next state logic
     case (state)
        S0: nextstate = S1;
        S1: nextstate = S2;
        S2: nextstate = S0;
        default: nextstate = S0;
     endcase
  assign q = (state == S0);  // output logic
endmodule
```

FSM Example 2: Smiling Snail

- Alyssa P. Hacker has a snail that crawls down a paper tape with 1's and 0's on it
- The snail smiles whenever the last four digits it has crawled over are 1101
- Design Moore and Mealy FSMs of the snail's brain



Implementing FSM Example 2: Definitions

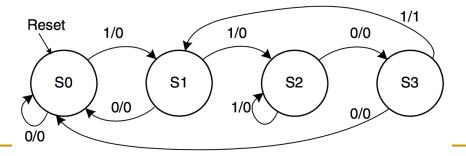


Implementing FSM Example 2: State Register

- This part defines the state register (memorizing process)
- Sensitive to only clk, reset
- In this example reset is active when '1' (active-high)

Implementing FSM Example 2: Next State Logic

```
// next state logic
 always @ (*)
    case (state)
       S0: if (number) nextstate = S1;
           else nextstate = S0;
       S1: if (number) nextstate = S2;
           else nextstate = S0;
       S2: if (number) nextstate = S2;
           else nextstate = S3;
       S3: if (number) nextstate = S1;
           else nextstate = S0;
       default: nextstate = S0;
    endcase
```



Implementing FSM Example 2: Output Logic

```
// output logic
assign smile = (number & state == S3);
```

- In this example, output depends on state and input
 - Mealy type FSM
- We used a simple combinational assignment

Implementation of FSM Example 2

```
module SmilingSnail (input clk,
                      input reset,
                      input number,
                      output smile);
   reg [1:0] state, nextstate;
   parameter S0 = 2'b00;
   parameter S1 = 2'b01;
   parameter S2 = 2'b10;
   parameter S3 = 2'b11;
  // state register
   always @ (posedge clk, posedge
reset)
      if (reset) state <= S0;</pre>
      else     state <= nextstate;</pre>
```

```
always @ (*) // next state logic
     case (state)
         S0: if (number)
                  nextstate = S1;
             else nextstate = S0;
         S1: if (number)
                  nextstate = S2;
             else nextstate = S0;
         S2: if (number)
                  nextstate = S2:
             else nextstate = S3;
         S3: if (number)
                  nextstate = S1;
             else nextstate = S0;
         default: nextstate = S0;
      endcase
  // output logic
assign smile = (number & state==S3);
endmodule
```

What Did We Learn?

- Basics of describing sequential circuits in Verilog
- The always statement
 - Needed for defining memorizing elements (flip-flops, latches)
 - Can also be used to define combinational circuits
- Blocking vs Non-blocking statements
 - = assigns the value immediately
 - <= assigns the value at the end of the block</p>
- Describing FSMs in Verilog
 - Next state logic
 - State assignment
 - Output logic

Now:

Timing and Verification

What Will We Learn Today?

- Timing in combinational circuits
 - Propagation delay and contamination delay
 - Glitches
- Timing in sequential circuits
 - Setup time and hold time
 - Determining how fast a circuit can operate

Circuit Verification

- How to make sure a circuit works correctly
- Functional verification
- Timing verification

Tradeoffs in Circuit Design

Circuit Design is a Tradeoff Between:

- Area
 - Circuit area is proportional to the cost of the device
- Speed / Throughput
 - We want faster, more capable circuits
- Power / Energy
 - Mobile devices need to work with a limited power supply
 - High performance devices dissipate more than 100W/cm²
- Design Time
 - Designers are expensive in time and money
 - The competition will not wait for you

Requirements and Goals Depend On Application



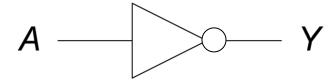
Circuit Timing

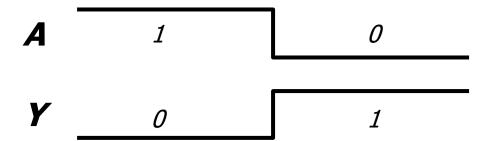
- Until now, we investigated logical functionality
- What about timing?
 - How fast is a circuit?
 - How can we make a circuit faster?
 - What happens if we run a circuit too fast?
- A design that is logically correct can still fail because of real-world implementation issues!

Part 1: Combinational Circuit Timing

Digital Logic Abstraction

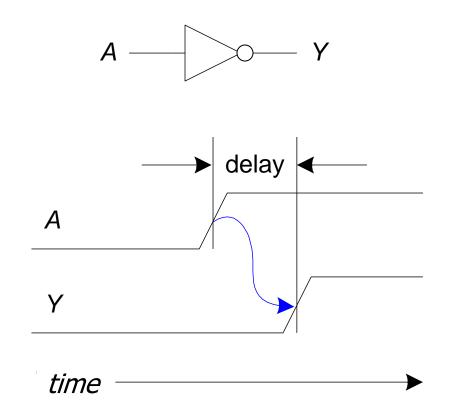
- "Digital logic" is a convenient abstraction
 - Output changes *immediately* with the input



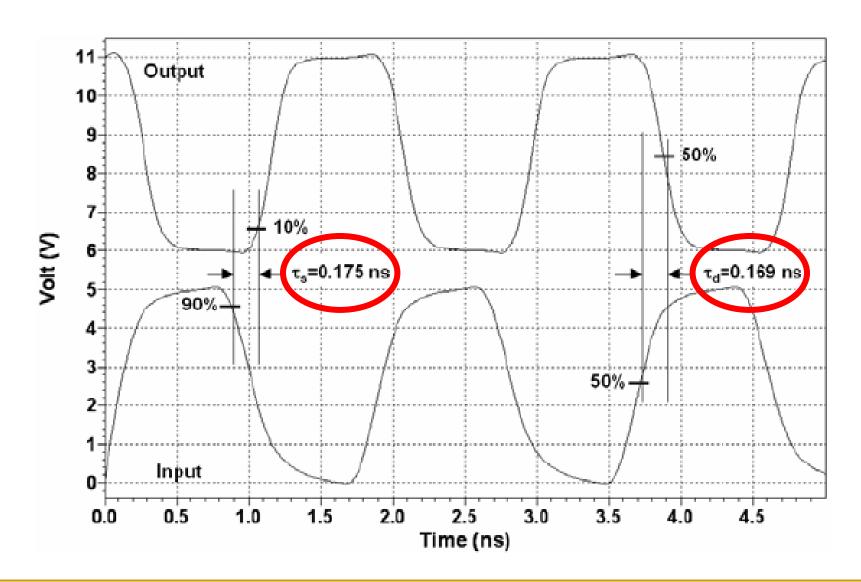


Combinational Circuit Delay

- In reality, outputs are delayed from inputs
 - Transistors take a finite amount of time to switch



Real Inverter Delay Example



Circuit Delay and Its Variation

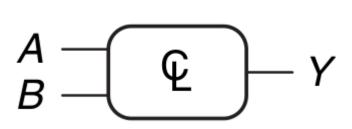
- Delay is fundamentally caused by
 - Capacitance and resistance in a circuit
 - Finite speed of light (not so fast on a nanosecond scale!)
- Anything affecting these quantities can change delay:
 - Rising (i.e., 0 -> 1) vs. falling (i.e., 1 -> 0) inputs
 - Different inputs have different delays
 - Changes in environment (e.g., temperature)
 - Aging of the circuit
- We have a range of possible delays from input to output

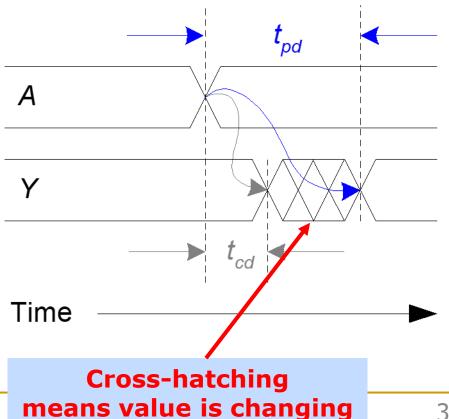
Delays from Input to Output Y

- Contamination delay (t_{cd}): delay until Y starts changing
- Propagation delay (t_{pd}): delay until Y *finishes changing*

Example Circuit

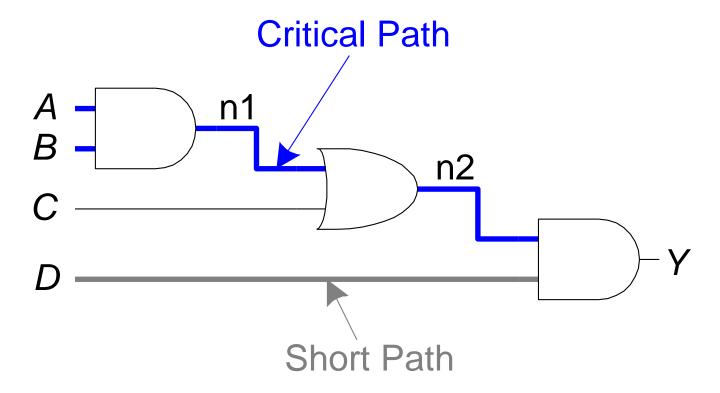
Effect of Changing Input 'A'





Calculating Longest & Shortest Delay Paths

We care about **both** the *longest* and *shortest* delay paths in a circuit (we will see why later in the lecture)

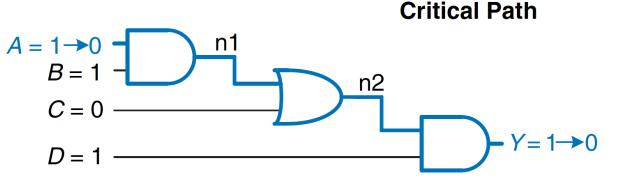


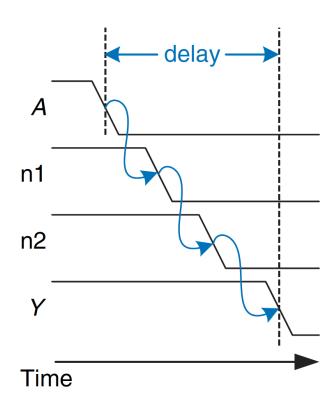
- Critical (Longest) Path:
- Shortest Path:

$$t_{pd} = 2 t_{pd_AND} + t_{pd_OR}$$

$$t_{cd} = t_{cd_AND}$$

Calculating Longest Delay Path (Critical Path)





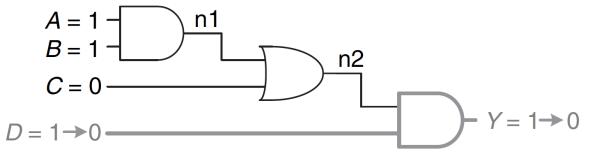
- Critical (Longest) Path:
- Shortest Path:

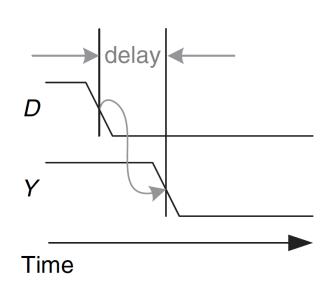
$$t_{pd} = 2 t_{pd_AND} + t_{pd_OR}$$

 $t_{cd} = t_{cd_AND}$

Calculating Shortest Delay Path

Short Path





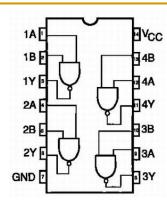
- Critical (Longest) Path:
- Shortest Path:

$$t_{pd} = 2 t_{pd_AND} + t_{pd_OR}$$

 $t_{cd} = t_{cd_AND}$

Example t_{pd} for a Real NAND-2 Gate





Symbol	Parameter	Conditions	25 °C			-40 °C to +125 °C		Unit
			Min	Тур	Max	Max (85 °C)	Max (125 °C)	
74HC00								
t _{pd}	propagation delay	nA, nB to nY; see Figure 6						
		V _{CC} = 2.0 V	-	25	-	115	135	ns
		V _{CC} = 4.5 V	-	9	-	23	27	ns
		V _{CC} = 5.0 V; C _L = 15 pF	-	7		-	-	ns
		V _{CC} = 6.0 V	_ (7	-	20	23	ns

Heavy dependence on voltage and temperature!

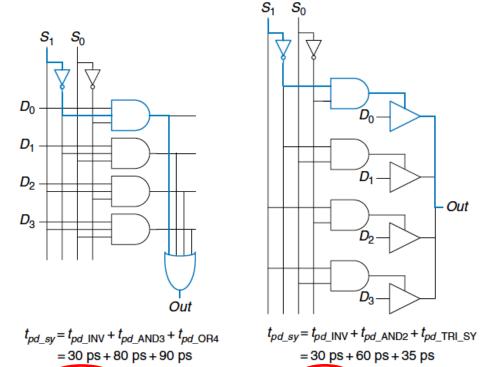
Example Worst-Case t_{pd}

Two different implementations of a 4:1 multiplexer

Gate Delays

Gate	t _{pd} (ps)			
NOT	30			
2-input AND	60			
3-input AND	80			
4-input OR	90			
tristate (A to Y)	50			
tristate (enable to Y)	35			

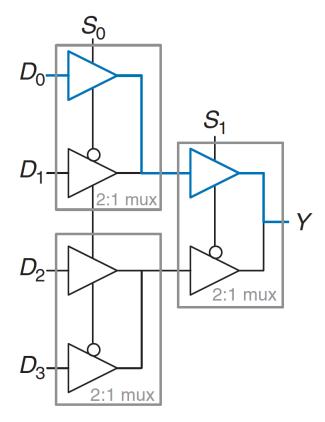
<u>Implementation 1</u>



Implementation 2

Different designs lead to very different delays

Aside: A Third 4:1 MUX Implementation



$$t_{pd_s0y} = t_{pd_TRLSY} + t_{pd_TRL_AY} =$$
85 ns
 $t_{pd_dy} = 2 t_{pd_TRI_AY} =$ 100 ns

Figure 2.74 4:1 multiplexer propagation delays: hierarchical using 2:1 multiplexers

Disclaimer: Calculating Long/Short Paths

- It's not always this easy to determine the long/short paths!
 - Not all input transitions affect the output
 - Can have multiple different paths from an input to output
- In reality, circuits are not all built equally
 - Different instances of the same gate have different delays
 - Wires have nonzero delay (increasing with length)
 - Temperature/voltage affect circuit speeds
 - Not all circuit elements are affected the same way
 - Can even change the critical path!
- Designers assume "worst-case" conditions and run many statistical simulations to balance yield/performance

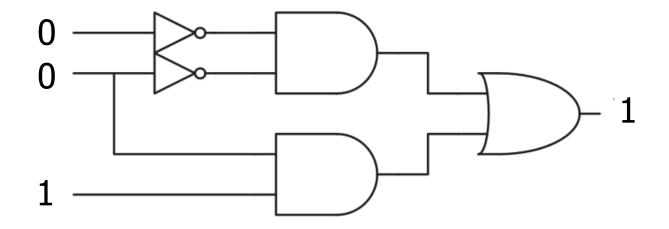
Combinational Timing Summary

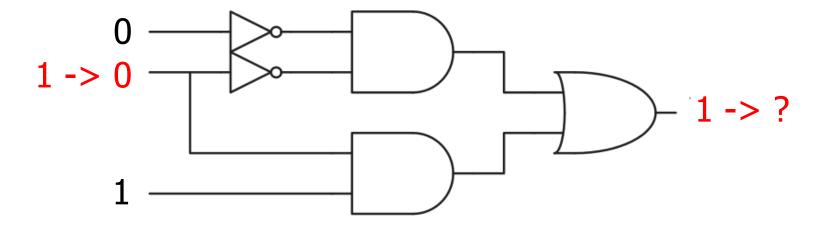
- Circuit outputs change some time after the inputs change
 - Caused by finite speed of light (not so fast on a ns scale!)
 - Delay is dependent on inputs, environmental state, etc.
- The range of possible delays is characterized by:
 - Contamination delay (t_{cd}): minimum possible delay
 - Propagation delay (t_{pd}): maximum possible delay
- Delays change with:
 - Circuit design (e.g., topology, materials)
 - Operating conditions

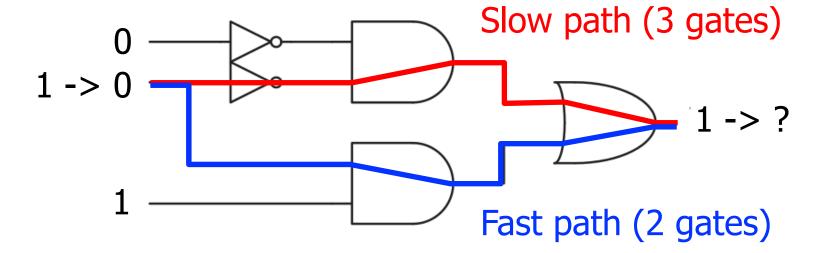
Output Glitches

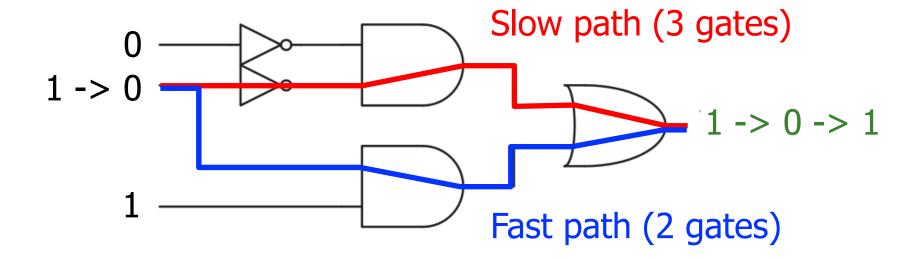
Glitch: one input transition causes multiple output transitions

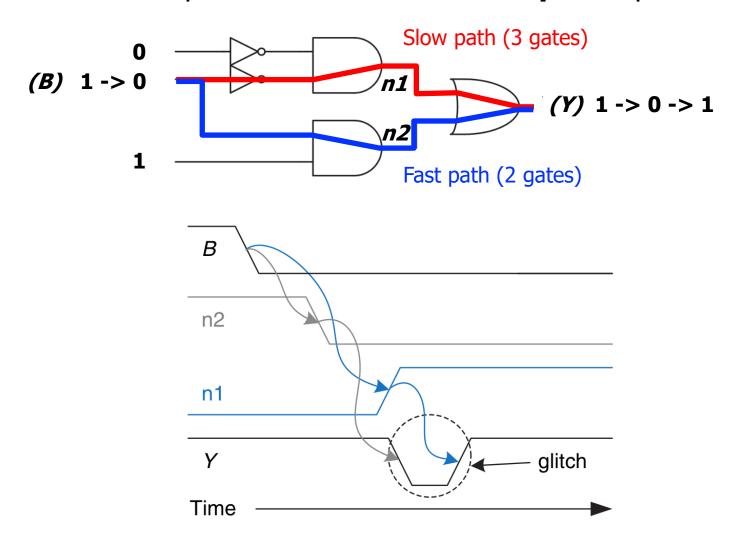
Circuit initial state





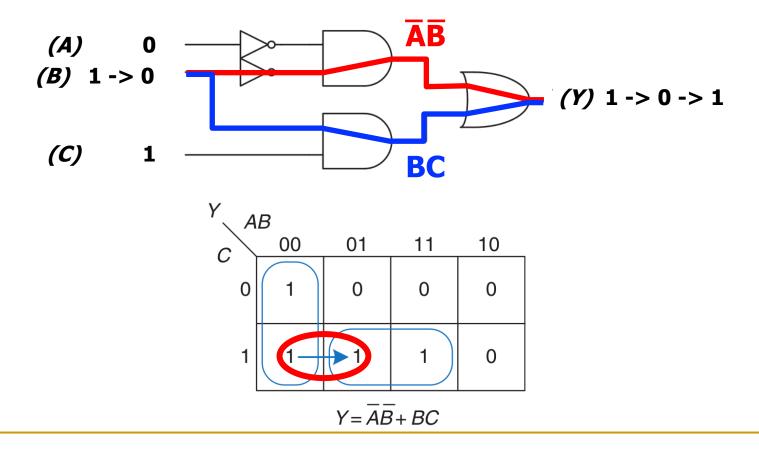






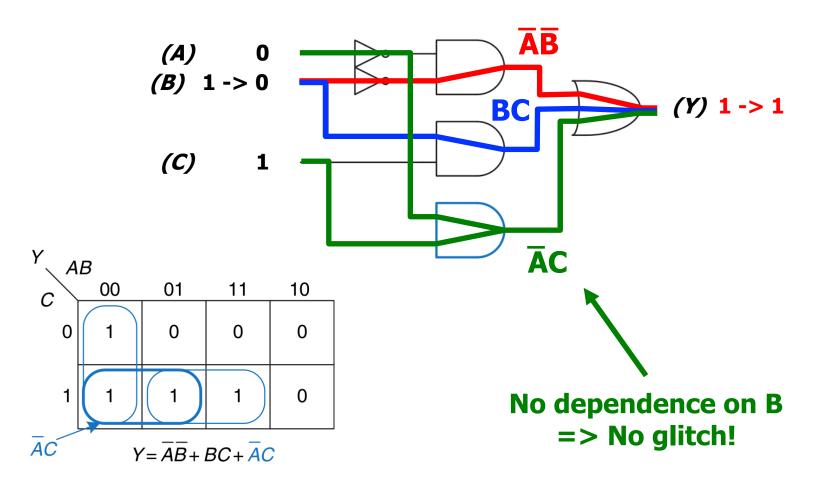
Optional: Avoiding Glitches Using K-Maps

- Glitches are visible in K-maps
 - Recall: K-maps show the results of a change in a single input
 - A glitch occurs when moving between prime implicants



Optional: Avoiding Glitches Using K-Maps

- We can fix the issue by adding in the consensus term
 - Ensures no transition between different prime implicants



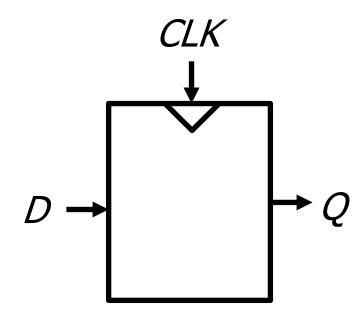
Avoiding Glitches

- Q: Do we always care about glitches?
 - Fixing glitches is undesirable
 - More chip area
 - More power consumption
 - More design effort
 - The circuit is eventually guaranteed to converge to the right value regardless of glitchiness
- A: No, not always!
 - If we only care about the long-term steady state output, we can safely ignore glitches
 - Up to the designer to decide if glitches matter in their application
 - When examining simulation output, important to recognize glitches

Part 2: Sequential Circuit Timing

Recall: D Flip-Flop

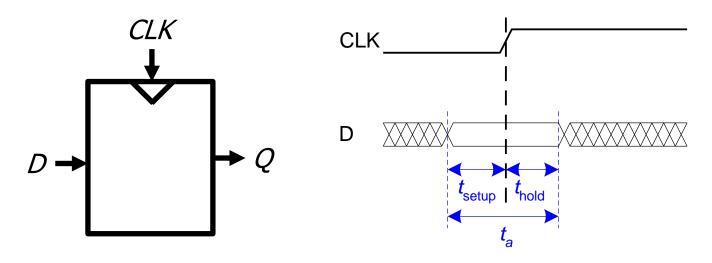
- Flip-flop samples D at the active clock edge
 - It outputs the sampled value to Q
 - It "stores" the sampled value until the next active clock edge



- The D flip-flop is made from combinational elements
- D, Q, CLK all have timing requirements!

D Flip-Flop Input Timing Constraints

D must be stable when sampled (i.e., at active clock edge)

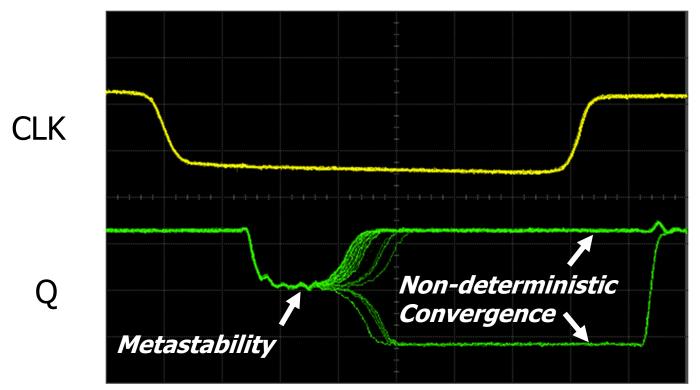


- Setup time (t_{setup}): time before the clock edge that data must be stable (i.e. not changing)
- Hold time (t_{hold}): time after the clock edge that data must be stable
- Aperture time (t_a) : time around clock edge that data must be stable $(t_a = t_{setup} + t_{hold})$

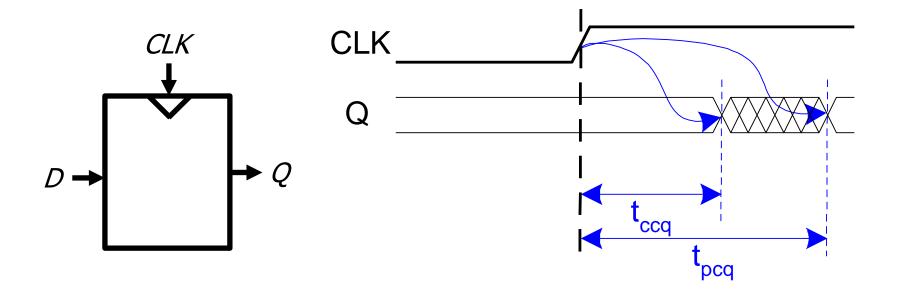
Violating Input Timing: Metastability

- If D is changing when sampled, metastability can occur
 - Flip-flop output is stuck somewhere between '1' and '0'
 - Output eventually settles non-deterministically

Example Timing Violations (NAND RS Latch)

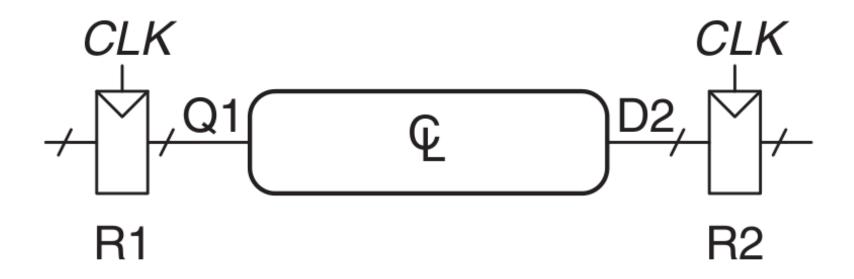


Flip-Flop Output Timing



- Contamination delay clock-to-q (t_{ccq}): earliest time after the clock edge that Q starts to change (i.e., is unstable)
- Propagation delay clock-to-q (t_{pcq}): latest time after the clock edge that Q stops changing (i.e., is stable)

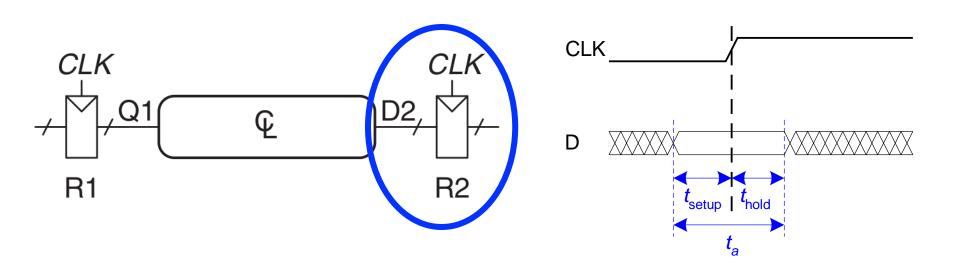
Recall: Sequential System Design



- Multiple flip-flops are connected with combinational logic
- Clock runs with period T_c (cycle time)
- Must meet timing requirements for both R1 and R2!

Ensuring Correct Sequential Operation

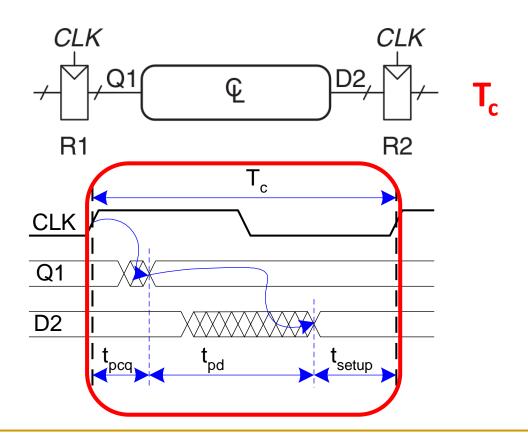
- Need to ensure correct input timing on R2
- Specifically, D2 must be stable:
 - at least t_{setup} before the clock edge
 - at least until thold after the clock edge



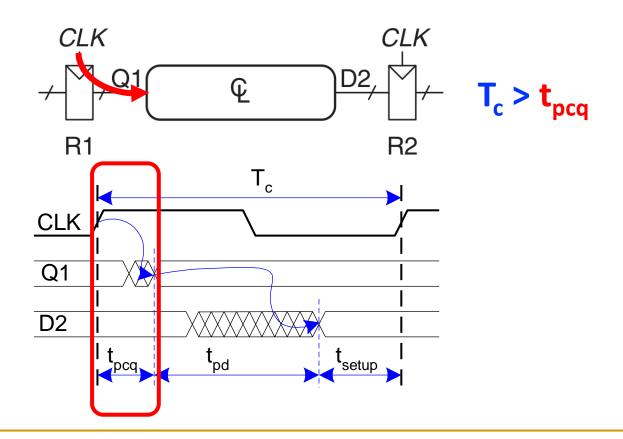
Ensuring Correct Sequential Operation

This means there is both a **minimum** and **maximum** delay between two flip-flops Potential CL too fast -> R2 thold violation CL too slow -> R2 t_{setup} violation **VIOLATION! CLK** CLK Q1 R2 R1 (a) CLK Q1 D2 (b)

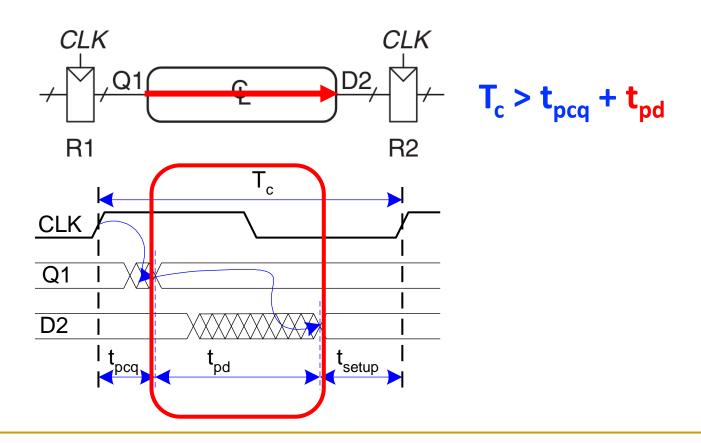
- Safe timing depends on the maximum delay from R1 to R2
- The input to R2 must be stable at least t_{setup} before the clock edge.



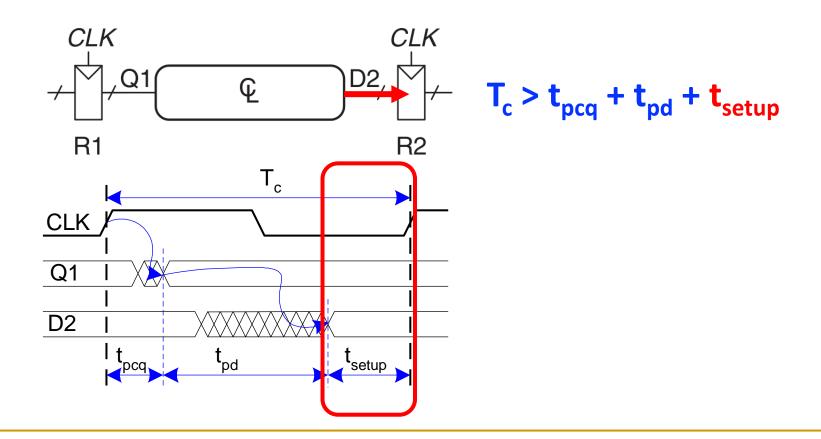
- Safe timing depends on the maximum delay from R1 to R2
- The input to R2 must be stable at least t_{setup} before the clock edge.



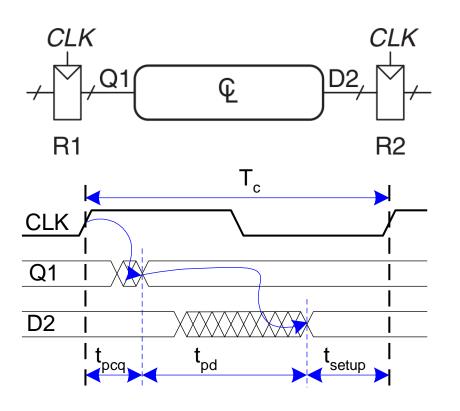
- Safe timing depends on the maximum delay from R1 to R2
- The input to R2 must be stable at least t_{setup} before the clock edge.

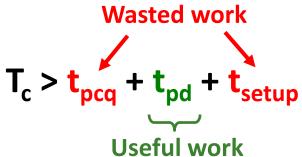


- Safe timing depends on the maximum delay from R1 to R2
- The input to R2 must be stable at least t_{setup} before the clock edge.



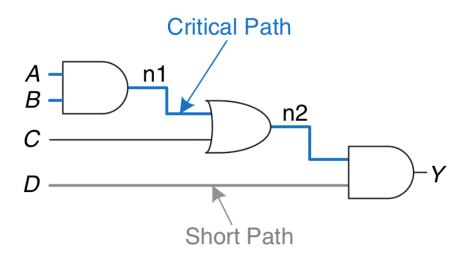
- Safe timing depends on the maximum delay from R1 to R2
- The input to R2 must be stable at least t_{setup} before the clock edge.





Sequencing overhead: amount of time wasted each cycle due to sequencing element timing requirements

t_{setup} Constraint and Design Performance



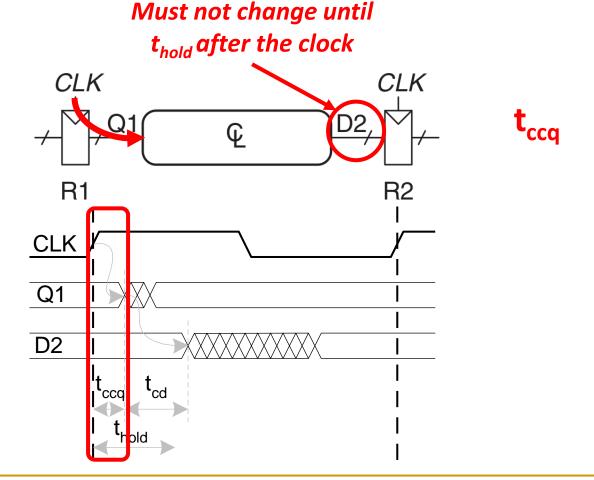
Critical path: path with the longest t_{pd}

$$T_c > t_{pcq} + t_{pd} + t_{setup}$$

- Overall design performance is determined by the critical path tpd
 - Determines the minimum clock period (i.e., max operating frequency)
 - If the critical path is too long, the design will run slowly
 - If critical path is too short, each cycle will do very little useful work
 - i.e., most of the cycle will be wasted in sequencing overhead

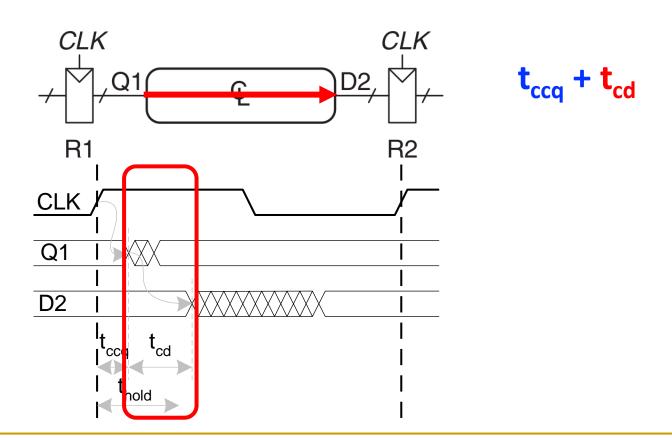
Hold Time Constraint

- Safe timing depends on the minimum delay from R1 to R2
- D2 (i.e., R2 input) must be stable for at least thold after the clock edge



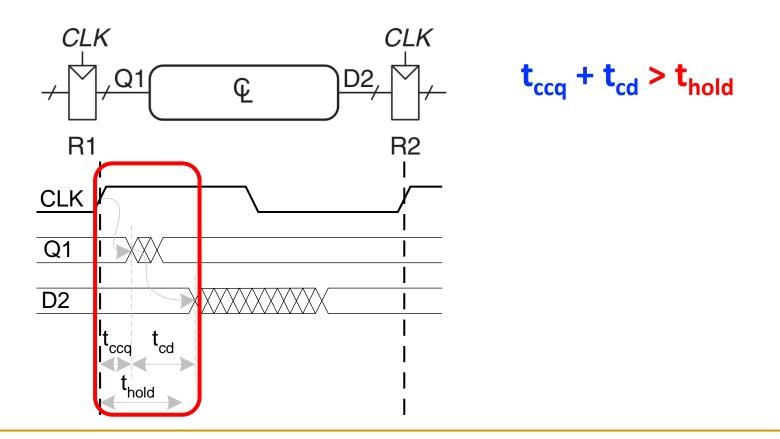
Hold Time Constraint

- Safe timing depends on the minimum delay from R1 to R2
- D2 (i.e., R2 input) must be stable for at least thold after the clock edge



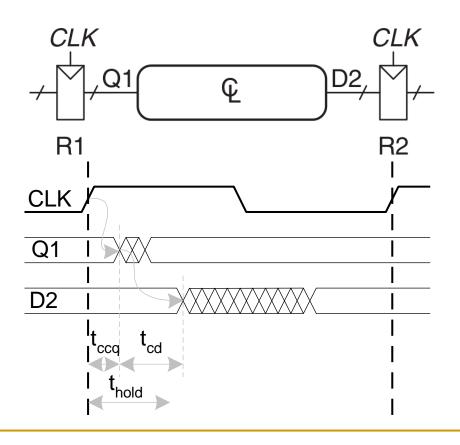
Hold Time Constraint

- Safe timing depends on the minimum delay from R1 to R2
- D2 (i.e., R2 input) must be stable for at least thold after the clock edge



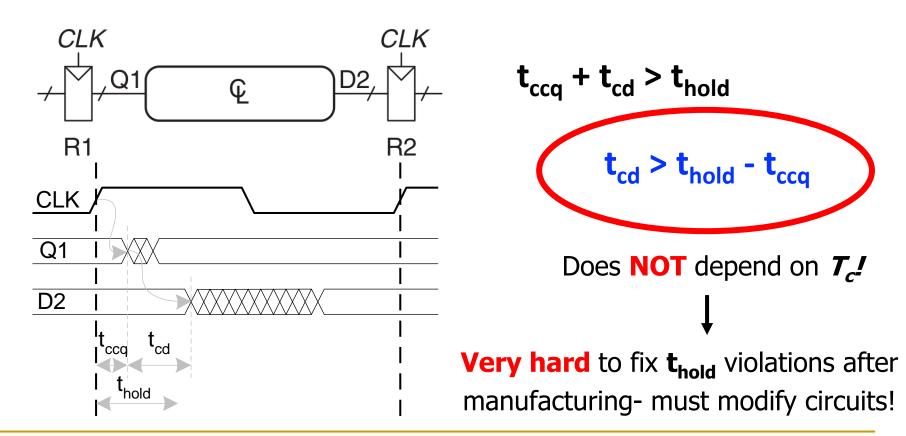
Hold Time Constraint

- Safe timing depends on the minimum delay from R1 to R2
- D2 (i.e., R2 input) must be stable for at least though after the clock edge



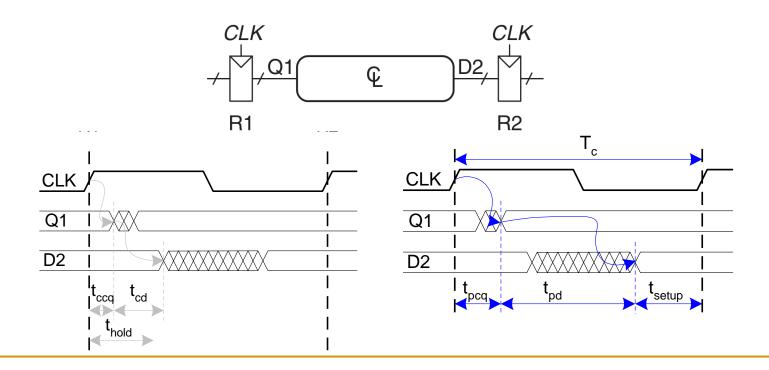
Hold Time Constraint

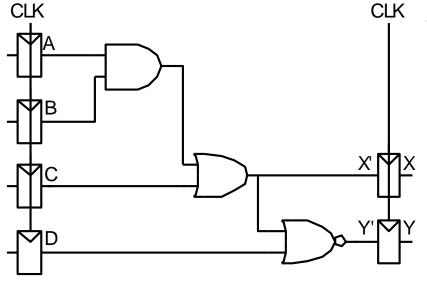
- Safe timing depends on the minimum delay from R1 to R2
- D2 (i.e., R2 input) must be stable for at least thought after the clock edge



Sequential Timing Summary

t _{ccq} / t _{pcq}	clock-to-q delay (contamination/propagation)		
t_{cd}/t_{pd}	combinational logic delay (contamination/propagation)		
t _{setup}	time that FF inputs must be stable before next clock edge		
t _{hold}	time that FF inputs must be stable after a clock edge		
T _c	clock period		





$$t_{pd} =$$

$$t_{cd} =$$

Check setup time constraints:

$$T_c > t_{pcq} + t_{pd} + t_{setup}$$

$$T_c >$$

$$f_{max} = 1/T_c =$$

Timing Characteristics

$$t_{ccq}$$
 = 30 ps

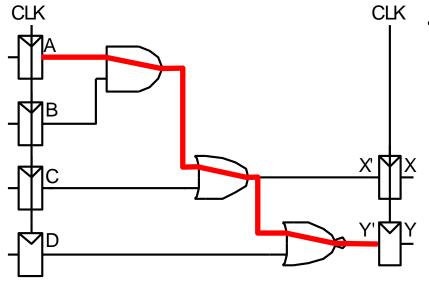
$$t_{pca} = 50 \text{ ps}$$

$$t_{\text{setup}} = 60 \text{ ps}$$

$$t_{\text{hold}}$$
 = 70 ps

$$\begin{array}{ccc} & & & & = 35 \text{ ps} \\ & & & & = 25 \text{ ps} \\ & & & & & = 25 \text{ ps} \\ \end{array}$$

$$t_{\text{ccq}} + t_{cd} > t_{\text{hold}}$$
?



$$t_{pd}$$
 = 3 x 35 ps = 105 ps

$$t_{cd} =$$

Check setup time constraints:

$$T_c > t_{pcq} + t_{pd} + t_{setup}$$

$$T_c >$$

$$f_{max} = 1/T_c =$$

Timing Characteristics

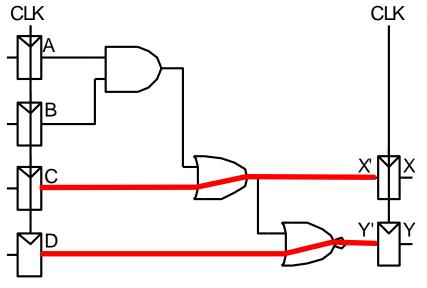
$$t_{ccq}$$
 = 30 ps

$$t_{pcq}$$
 = 50 ps

$$t_{\text{setup}} = 60 \text{ ps}$$

$$t_{\text{hold}}$$
 = 70 ps

$$t_{\text{ccq}} + t_{cd} > t_{\text{hold}}$$
?



$$t_{pd}$$
 = 3 x 35 ps = 105 ps

$$t_{cd} = 25 \text{ ps}$$

Check setup time constraints:

$$T_c > t_{pcq} + t_{pd} + t_{setup}$$

$$T_c >$$

$$f_{max} = 1/T_c =$$

Timing Characteristics

$$t_{ccq}$$
 = 30 ps

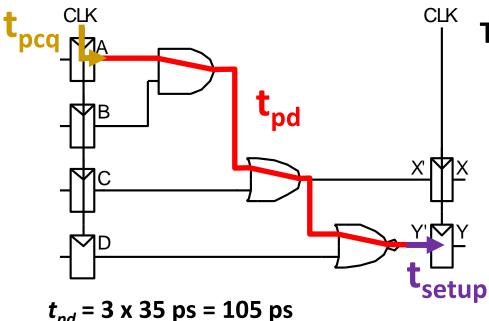
$$t_{pcq}$$
 = 50 ps

$$t_{\text{setup}} = 60 \text{ ps}$$

$$t_{\text{hold}}$$
 = 70 ps

$$\begin{array}{ccc} & & & & = 35 \text{ ps} \\ & & & & = 25 \text{ ps} \\ & & & & & = 25 \text{ ps} \\ \end{array}$$

$$t_{\text{ccq}} + t_{cd} > t_{\text{hold}}$$
?



Timing Characteristics

$$t_{ccq}$$
 = 30 ps

$$t_{pca} = 50 \text{ ps}$$

$$t_{\text{setup}} = 60 \text{ ps}$$

$$t_{\text{hold}}$$
 = 70 ps

$$\begin{array}{ccc} & & & & = 35 \text{ ps} \\ & & & & = 25 \text{ ps} \\ & & & & & = 25 \text{ ps} \\ \end{array}$$

$$t_{pd}$$
 = 3 x 35 ps = 105 ps

$$t_{cd} = 25 \text{ ps}$$

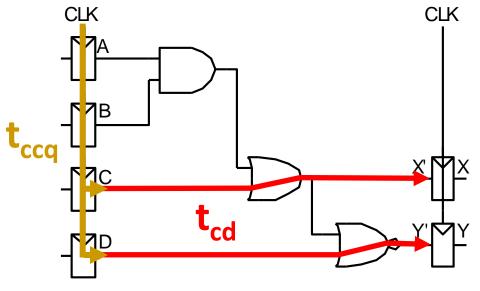
Check setup time constraints:

$$T_c > t_{pcq} + t_{pd} + t_{setup}$$

$$T_c > (50 + 105 + 60) \text{ ps} = 215 \text{ ps}$$

$$f_{max} = 1/T_c = 4.65 \text{ GHz}$$

$$t_{\text{ccq}} + t_{cd} > t_{\text{hold}}$$
?



$$t_{pd}$$
 = 3 x 35 ps = 105 ps

$$t_{cd} = 25 \text{ ps}$$

Check setup time constraints:

$$T_c > t_{pcq} + t_{pd} + t_{setup}$$

$$T_c > (50 + 105 + 60) \text{ ps} = 215 \text{ ps}$$

$$f_{max} = 1/T_c = 4.65 \text{ GHz}$$

Timing Characteristics

$$t_{ccq}$$
 = 30 ps

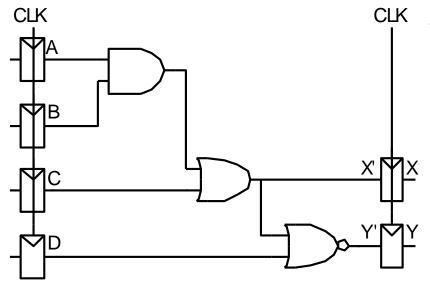
$$t_{pca} = 50 \text{ ps}$$

$$t_{\text{setup}} = 60 \text{ ps}$$

$$t_{\text{hold}}$$
 = 70 ps

$$t_{\text{ccq}} + t_{cd} > t_{\text{hold}}$$
?

$$(30 + 25) ps > 70 ps ?$$



$$t_{pd}$$
 = 3 x 35 ps = 105 ps

$$t_{cd} = 25 \text{ ps}$$

Check setup time constraints:

$$T_c > t_{pcq} + t_{pd} + t_{setup}$$

$$T_c > (50 + 105 + 60) \text{ ps} = 215 \text{ ps}$$

$$f_{max} = 1/T_c = 4.65 \text{ GHz}$$

Timing Characteristics

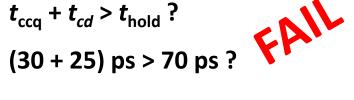
$$t_{ccq}$$
 = 30 ps

$$t_{pcq} = 50 \text{ ps}$$

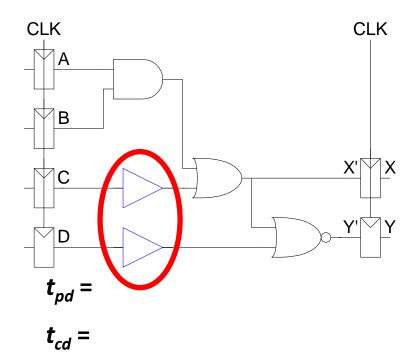
$$t_{\text{setup}} = 60 \text{ ps}$$

$$t_{\text{hold}}$$
 = 70 ps

$$t_{\text{ccq}} + t_{cd} > t_{\text{hold}}$$
?



Add buffers to the short paths:



Check setup time constraints:

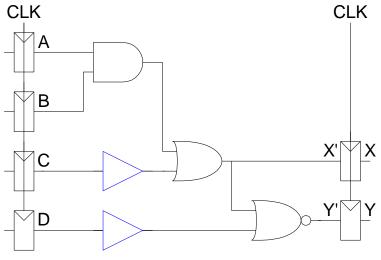
$$T_c > t_{pcq} + t_{pd} + t_{setup}$$
 $T_c > f_c = f_c$

Timing Characteristics

$$t_{ccq}$$
 = 30 ps
 t_{pcq} = 50 ps
 t_{setup} = 60 ps
 t_{hold} = 70 ps
 t_{pd} = 35 ps
 t_{cd} = 25 ps

$$t_{\text{ccq}} + t_{cd} > t_{\text{hold}}$$
?

Add buffers to the short paths:



$$t_{pd}$$
 = 3 x 35 ps = 105 ps

$$t_{cd}$$
 = 2 x 25 ps = 50 ps

Check setup time constraints:

$$T_c > t_{pcq} + t_{pd} + t_{setup}$$

 $T_c >$

$$f_c =$$

Timing Characteristics

$$t_{ccq}$$
 = 30 ps

$$t_{pcq}$$
 = 50 ps

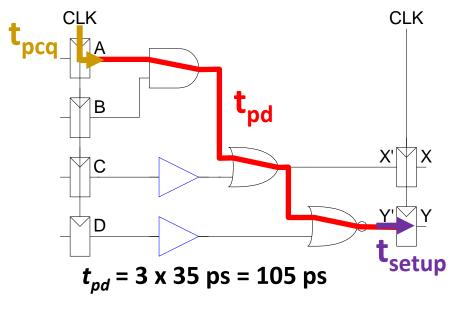
$$t_{\text{setup}} = 60 \text{ ps}$$

$$t_{\text{hold}}$$
 = 70 ps

$$\begin{array}{ccc} & & & = 35 \text{ ps} \\ & & & \\ & &$$

$$t_{\text{ccq}} + t_{cd} > t_{\text{hold}}$$
?

Add buffers to the short paths:



$$t_{cd}$$
 = 2 x 25 ps = 50 ps

Check setup time constraints:

$$T_c > t_{pcq} + t_{pd} + t_{setup}$$
 $T_c > (50 + 105 + 60) \text{ ps} = 215 \text{ ps}$
 $f_c = 1/T_c = 4.65 \text{ GHz}$

Timing Characteristics

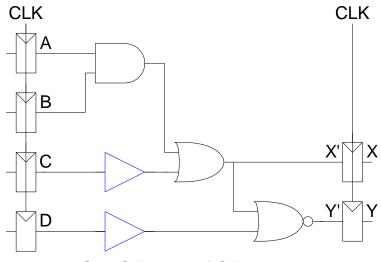
$$t_{ccq}$$
 = 30 ps
 t_{pcq} = 50 ps
 t_{setup} = 60 ps
 t_{hold} = 70 ps
 t_{pd} = 35 ps
 t_{cd} = 25 ps

$$t_{\text{ccq}} + t_{cd} > t_{\text{hold}}$$
?

Note: no change

to max frequency!

Add buffers to the short paths:



$$t_{pd}$$
 = 3 x 35 ps = 105 ps

$$t_{cd}$$
 = 2 x 25 ps = 50 ps

Check setup time constraints:

$$T_c > t_{pcq} + t_{pd} + t_{setup}$$

$$T_c > (50 + 105 + 60) \text{ ps} = 215 \text{ ps}$$

$$f_c = 1/T_c = 4.65 \text{ GHz}$$

Timing Characteristics

$$t_{cca}$$
 = 30 ps

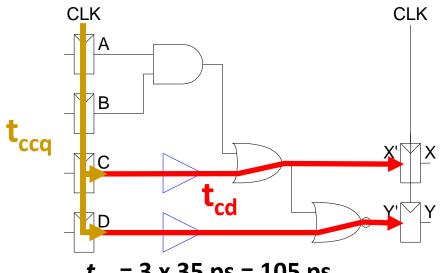
$$t_{pcq} = 50 \text{ ps}$$

$$t_{\text{setup}} = 60 \text{ ps}$$

$$t_{\text{hold}}$$
 = 70 ps

$$t_{ccq} + t_{cd} > t_{hold}$$
?

Add buffers to the short paths:



$$t_{pd}$$
 = 3 x 35 ps = 105 ps

$$t_{cd}$$
 = 2 x 25 ps = 50 ps

Check setup time constraints:

$$T_c > t_{pcq} + t_{pd} + t_{setup}$$

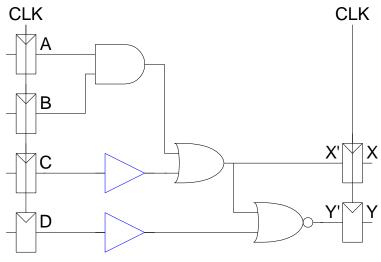
 $T_c > (50 + 105 + 60) \text{ ps} = 215 \text{ ps}$
 $f_c = 1/T_c = 4.65 \text{ GHz}$

Timing Characteristics

$$t_{ccq}$$
 = 30 ps
 t_{pcq} = 50 ps
 t_{setup} = 60 ps
 t_{hold} = 70 ps
 t_{pd} = 35 ps
 t_{cd} = 25 ps

$$t_{ccq} + t_{cd} > t_{hold}$$
?
(30 + 50) ps > 70 ps ?

Add buffers to the short paths:



$$t_{pd}$$
 = 3 x 35 ps = 105 ps

$$t_{cd}$$
 = 2 x 25 ps = 50 ps

Check setup time constraints:

$$T_c > t_{pcq} + t_{pd} + t_{setup}$$

 $T_c > (50 + 105 + 60) \text{ ps} = 215 \text{ ps}$

$$f_c = 1/T_c = 4.65 \text{ GHz}$$

Timing Characteristics

$$t_{cca}$$
 = 30 ps

$$t_{pcq}$$
 = 50 ps

$$t_{\text{setup}} = 60 \text{ ps}$$

$$t_{\text{hold}}$$
 = 70 ps

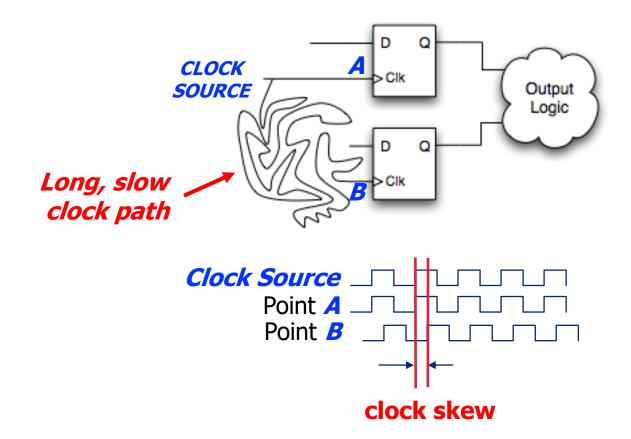
$$t_{ccq} + t_{cd} > t_{hold}$$
?





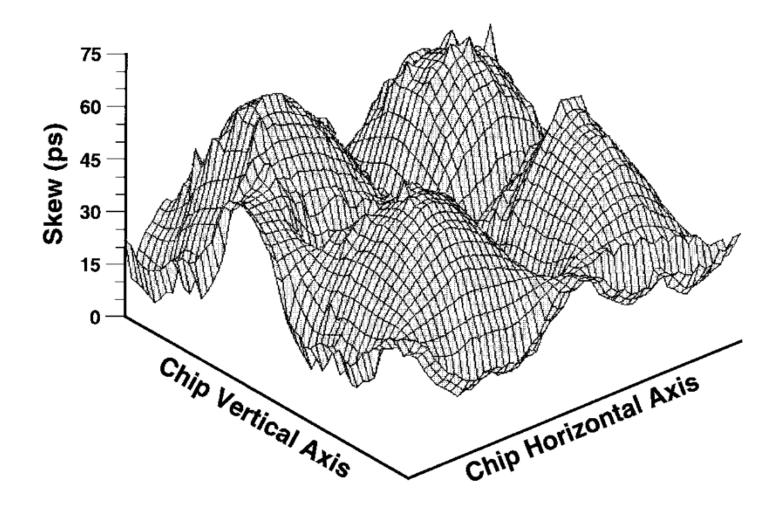
Clock Skew

- To make matters worse, clocks have delay too!
 - The clock does **not** reach all parts of the chip at the same time!
- Clock skew: time difference between two clock edges



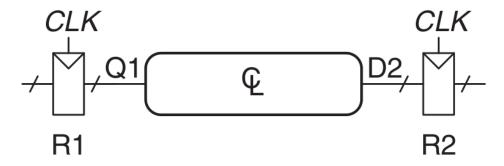
Clock Skew Example

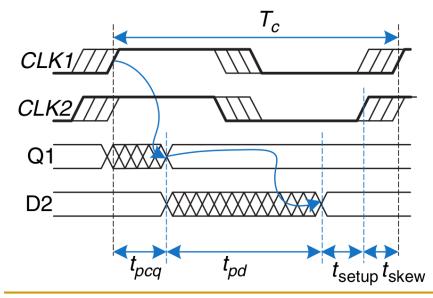
Example of the Alpha 21264 clock skew spatial distribution



Clock Skew: Setup Time Revisited

- Safe timing requires considering the worst-case skew
 - Clock arrives at R2 before R1
 - Leaves as little time as possible for the combinational logic





Signal must arrive at D2 earlier!

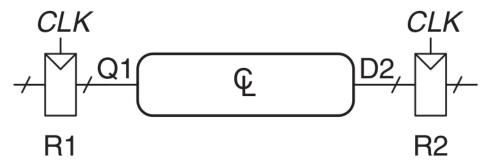
This effectively *increases* t_{setup}:

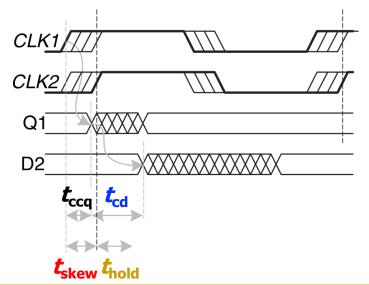
$$T_c > t_{pcq} + t_{pd} + t_{setup} + t_{skew}$$

$$T_c > t_{pcq} + t_{pd} + t_{setup, effective}$$

Clock Skew: Hold Time Revisited

- Safe timing requires considering the worst-case skew
 - Clock arrives at R2 after R1
 - Increases the minimum required delay for the combinational logic





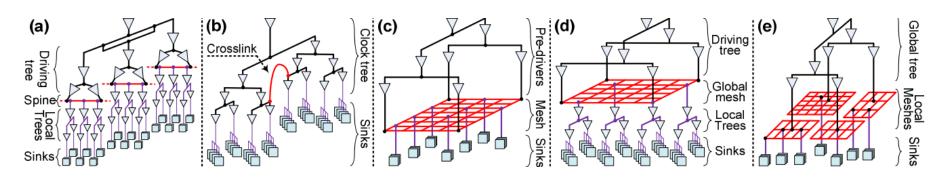
Signal must arrive at D2 *later*!

This effectively *increases* t_{hold}:

$$t_{cd} + t_{ccq} > t_{hold} + t_{skew}$$
 $t_{cd} + t_{ccq} > t_{hold, effective}$

Clock Skew: Summary

- Skew effectively increases both t_{setup} and t_{hold}
 - Increased sequencing overhead
 - □ i.e., less useful work done per cycle
- Designers must keep skew to a minimum
 - Requires intelligent "clock network" across a chip
 - Goal: clock arrives at all locations at roughly the same time



Source: Abdelhadi, Ameer, et al. "Timing-driven variation-aware nonuniform clock mesh synthesis." GLSVLSI'10.

Part 3: Circuit Verification

How Do You Know That A Circuit Works?

- You have designed a circuit
 - Is it functionally correct?
 - Even if it is logically correct, does the hardware meet all timing constraints?
- How can you test for:
 - Functionality?
 - Timing?
- Answer: simulation tools!
 - Formal verification tools (e.g., SAT solvers)
 - HDL timing simulation (e.g., Vivado)
 - Circuit simulation (e.g., SPICE)

Testing Large Digital Designs

- Testing can be the most time consuming design stage
 - Functional correctness of all logic paths
 - Timing, power, etc. of all circuit elements
- Unfortunately, low-level (e.g., circuit) simulation is much slower than high-level (e.g., HDL, C) simulation
- Solution: we split responsibilities:
 - 1) Check only functionality at a high level (e.g., C, HDL)
 - (Relatively) fast simulation time allows high code coverage
 - Easy to write and run tests
 - 2) Check only timing, power, etc. at low level (e.g., circuit)
 - No functional testing of low-level model
 - Instead, test functional equivalence to high-level model
 - Hard, but easier than testing logical functionality at this level

Testing Large Digital Designs

- We have tools to handle different levels of verification
 - Logic synthesis tools guarantee equivalence of high-level logic and synthesized circuit-level description
 - Timing verification tools check all circuit timings
 - Design rule checks ensure that physical circuits are buildable
- The task of a logic designer is to:
 - Provide functional tests for logical correctness of the design
 - Provide timing constraints (e.g., desired operating frequency)
- Tools and/or circuit engineers will decide if it can be built!

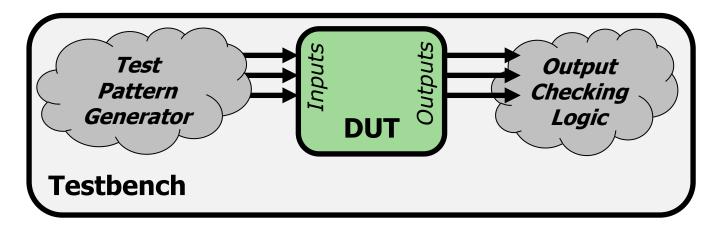
Part 4: Functional Verification

Functional Verification

- Goal: check logical correctness of the design
- Physical circuit timing (e.g., t_{setup}/t_{hold}) is typically ignored
 - May implement simple checks to catch obvious bugs
 - We'll discuss timing verification later in this lecture
- There are two primary approaches
 - Logic simulation (e.g., C/C++/Verilog test routines)
 - Formal verification techniques
- In this course, we will use Verilog for functional verification

Testbench-Based Functional Testing

- Testbench: a module created specifically to test a design
 - Tested design is called the "device under test (DUT)"



- Testbench provides inputs (test patterns) to the DUT
 - Hand-crafted values
 - Automatically generated (e.g., sequential or random values)
- Testbench checks outputs of the DUT against:
 - Hand-crafted values
 - A "golden design" that is known to be bug-free

Testbench-Based Functional Testing

- A testbench can be:
 - HDL code written to test other HDL modules
 - Circuit schematic used to test other circuit designs
- The testbench is not designed for hardware synthesis!
 - Runs in **simulation** only
 - HDL simulator (e.g., Vivado simulator)
 - SPICE circuit simulation
 - Testbench uses simulation-only constructs
 - E.g., "wait 10ns"
 - E.g., ideal voltage/current source
 - Not suitable to be physically built!

Common Verilog Testbench Types

Testbench	Input/Output Generation	Error Checking
Simple	Manual	Manual
Self-Checking	Manual	Automatic
Automatic	Automatic	Automatic

Example DUT

We will walk through different types of testbenches to test a module that implements the logic function:

$$y = (\overline{b} \cdot \overline{c}) + (a \cdot \overline{b})$$

```
// performs y = ~b \& ~c | a \& ~b
module sillyfunction (input a, b, c,
                      output y);
      wire b n, c n;
      wire m1, m2;
      not not b(b n, b);
      not not c(c n, c);
      and minterm1 (m1, b n, c n);
      and minterm2 (m2, a, b n);
      or out func(y, m1, m2);
endmodule
```

Useful Verilog Syntax for Testbenching

```
module example syntax();
  reg a;
  // like "always" block, but runs only once at sim start
  initial
  begin
      a = 0; // set value of req: use blocking assignments
      #10; // wait (do nothing) for 10 ns
      a = 1;
       $display("printf() style message!"); // print message
  end
endmodule
```

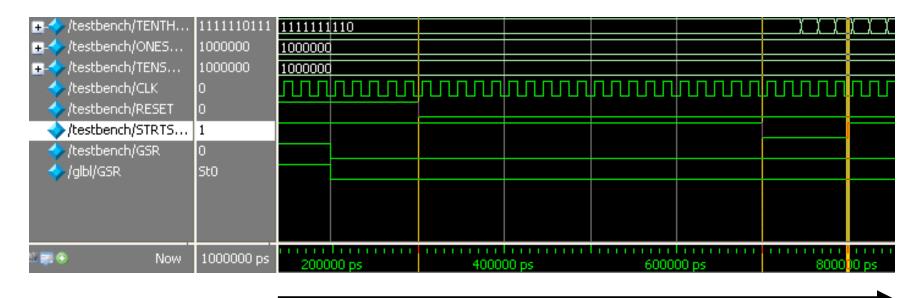
Simple Testbench

Simple Testbench

```
module testbench1(); // No inputs, outputs
 reg a, b, c; // Manually assigned
 wire y;
          // Manually checked
  // instantiate device under test
  sillyfunction dut (.a(a), .b(b), .c(c), .y(y));
  // apply hardcoded inputs one at a time
  initial begin
   a = 0; b = 0; c = 0; #10; // apply inputs, wait 10ns
   c = 1; #10;
                       // apply inputs, wait 10ns
   b = 1; c = 0; #10; // etc ... etc...
   c = 1; #10;
   a = 1; b = 0; c = 0; #10;
 end
endmodule
```

Simple Testbench: Output Checking

- Most common method is to look at waveform diagrams
 - Thousands of signals over millions of clock cycles
 - Too many to just printf()!



time

Manually check that output is correct at all times

Simple Testbench

Pros:

- Easy to design
- Can easily test a few, specific inputs (e.g., corner cases)

Cons:

- Not scalable to many test cases
- Outputs must be checked manually outside of the simulation
 - E.g., inspecting dumped waveform signals
 - E.g., printf() style debugging

Self-Checking Testbench

Self-Checking Testbench

```
module testbench2();
  reg a, b, c;
 wire y;
  sillyfunction dut(.a(a), .b(b), .c(c), .y(y));
  initial begin
     a = 0; b = 0; c = 0; #10; // apply input, wait 10ns
     if (y !== 1) $display("000 failed."); // check result
     c = 1; #10;
     if (y !== 0) $display("001 failed.");
     b = 1; c = 0; #10;
     if (y !== 0) $display("010 failed.");
  end
endmodule
```

Self-Checking Testbench

Pros:

- Still easy to design
- Still easy to test a few, specific inputs (e.g., corner cases)
- Simulator will print whenever an error occurs

Cons:

- Still not scalable to millions of test cases
- Easy to make an error in hardcoded values
 - You make just as many errors writing a testbench as actual code
 - Hard to debug whether an issue is in the testbench or in the DUT

Self-Checking Testbench using Testvectors

- Write testvector file
 - List of inputs and expected outputs
 - Can create vectors manually or automatically using an already verified, simpler "golden model" (more on this later)
- Example file:

```
$ cat testvectors.tv

000_1

001_0

010_0

011_0

100_1

101_1

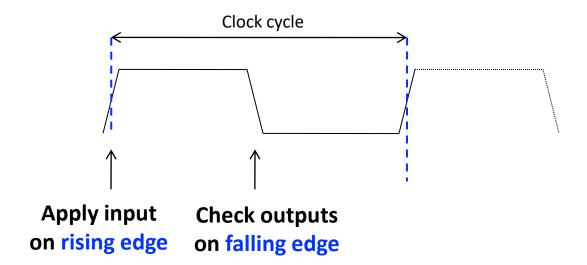
110_0

111_0

...
```

Testbench with Testvectors Design

- Use a "clock signal" for assigning inputs, reading outputs
 - Test one testvector each "clock cycle"



- Note: "clock signal" simply separates inputs from outputs
 - Allows us to observe the inputs/outputs in waveform diagrams
 - □ Not used for checking physical circuit timing (e.g., t_{setup}/t_{hold})
 - We'll discuss circuit timing verification later in this lecture

Testbench Example (1/5): Signal Declarations

Declare signals to hold internal state

H&H Section 4.9, Example 4.39

Testbench Example (2/5): Clock Generation

Testbench Example (3/5): Read Testvectors into Array

```
// at start of test, load vectors and pulse reset
 initial // Only executes once
 begin
     $readmemb("example.tv", testvectors); // Read vectors
     reset = 1; #27; reset = 0;  // Apply reset wait
 end
// Note: $readmemh reads testvector files written in
// hexadecimal
```

Testbench Example (4/5): Assign Inputs/Outputs

```
// apply test vectors on rising edge of clk
always @(posedge clk)
begin
    {a, b, c, yexpected} = testvectors[vectornum];
end
```

- Apply {a, b, c} inputs on the rising edge of the clock
- Get yexpected for checking the output on the falling edge
- Rising/falling edges are chosen only by convention
 - You can use any part of the clock signal
 - Your H+H textbook uses this convention

Testbench Example (5/5): Check Outputs

```
always @ (negedge clk)
begin
     if (~reset) // don't test during reset
    begin
         if (y !== yexpected)
        begin
            $display("Error: inputs = %b", {a, b, c});
            $display(" outputs = %b (%b exp)", y, yexpected);
            errors = errors + 1;
        end
         // increment array index and read next testvector
        vectornum = vectornum + 1;
         if (testvectors[vectornum] === 4'bx)
        begin
            $display("%d tests completed with %d errors",
                 vectornum, errors);
                               // End simulation
            $finish;
        end
    end
end
```

Self-Checking Testbench with Testvectors

Pros:

- Still easy to design
- Still easy to test a few, specific inputs (e.g., corner cases)
- Simulator will print whenever an error occurs
- No need to change hardcoded values for different tests

Cons:

- May be error-prone depending on source of testvectors
- More scalable, but still limited by reading a file
 - Might have many more combinational paths to test than will fit in memory

Automatic Testbench

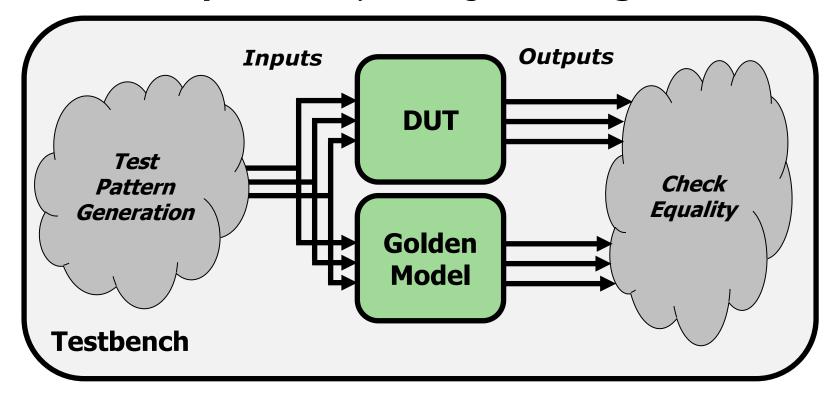
Golden Models

- A golden model represents the ideal circuit behavior
 - Must be developed, and might be difficult to write
 - Can be done in C, Perl, Python, Matlab or even in Verilog
- For our example circuit:

- Simpler than our earlier gate-level description
 - Golden model is usually easier to design and understand
 - Golden model is much easier to verify

Automatic Testbench

The DUT output is compared against the golden model



- Challenge: need to generate inputs to the designs
 - Sequential values to cover the entire input space?
 - Random values?

Automatic Testbench: Code

```
module testbench1();
   ... // variable declarations, clock, etc.
  // instantiate device under test
  sillyfunction dut (a, b, c, y_dut);
  golden model gold (a, b, c, y gold);
  // instantiate test pattern generator
  test pattern generator tgen (a, b, c, clk);
  // check if y dut is ever not equal to y gold
  always @(negedge clk)
  begin
       if(y dut !== y gold)
           $display(...)
  end
endmodule
```

Automatic Testbench

Pros:

- Output checking is fully automated
- Could even compare timing using a golden timing model
- Highly scalable to as much simulation time as is feasible
 - Leads to high coverage of the input space
- Better separation of roles
 - Separate designers can work on the DUT and the golden model
 - DUT testing engineer can focus on important test cases instead of output checking

Cons:

- Creating a correct golden model may be (very) difficult
- Coming up with good testing inputs may be difficult

However, Even with Automatic Testing...

- How long would it take to test a 32-bit adder?
 - □ In such an adder there are **64** inputs = 2^{64} possible inputs
 - If you test one input in 1ns, you can test 10⁹ inputs per second
 - or 8.64 x 10¹⁴ inputs per day
 - or 3.15 x 10¹⁷ inputs per year
 - we would still need 58.5 years to test all possibilities
- Brute force testing is not feasible for most circuits!
 - Need to prune the overall testing space
 - E.g., formal verification methods, choosing 'important cases'
- Verification is a hard problem

Part 5: Timing Verification

Timing Verification Approaches

- High-level simulation (e.g., C, Verilog)
 - Can model timing using "#x" statements in the DUT
 - Useful for hierarchical modeling
 - Insert delays in FF's, basic gates, memories, etc.
 - High level design will have some notion of timing
 - Usually not as accurate as real circuit timing
- Circuit-level timing verification
 - Need to first synthesize your design to actual circuits
 - No one general approach- very design flow specific
 - Your FPGA/ASIC/etc. technology has special tool(s) for this
 - E.g., Xilinx Vivado (what you're using in lab)
 - □ E.g., Synopsys/Cadence Tools (for VLSI design)

The Good News

- Tools will try to meet timing for you!
 - Setup times, hold times
 - Clock skews
 - **...**
- They usually provide a 'timing report' or 'timing summary'
 - Worst-case delay paths
 - Maximum operation frequency
 - Any timing errors that were found

The Bad News

- The tool can fail to find a solution
 - Desired clock frequency is too aggressive
 - Can result in setup time violation on a particularly long path
 - Too much logic on clock paths
 - Introduces excessive clock skew
 - Timing issues with asynchronous logic
- The tool will provide (hopefully) helpful errors
 - Reports will contain paths that failed to meet timing
 - Gives a place from where to start debugging
- Q: How can we fix timing errors?

Meeting Timing Constraints

- Unfortunately, this is often a manual, iterative process
 - Meeting strict timing constraints (e.g., high performance designs) can be tedious
- Can try synthesis/place-and-route with different options
 - Different random seeds
 - Manually provided **hints** for place-and-route
- Can manually optimize the reported problem paths
 - Simplify complicated logic
 - Split up long combinational logic paths
 - Recall: fix hold time violations by adding more logic!

Meeting Timing Constraints: Principles

- Let's go back to the fundamentals
- Clock cycle time is determined by the maximum logic delay we can accommodate without violating timing constraints
- Good design principles
 - Critical path design: Minimize the maximum logic delay
 - → Maximizes performance
 - Balanced design: Balance maximum logic delays across different parts of a system (i.e., between different pairs of flip flops)
 - → No bottlenecks + minimizes wasted time
 - Bread and butter design: Optimize for the common case, but make sure non-common-cases do not overwhelm the design
 - → Maximizes performance for realistic cases

Lecture Summary

- Timing in combinational circuits
 - Propagation delay and contamination delay
 - Glitches
- Timing in sequential circuits
 - Setup time and hold time
 - Determining how fast a circuit can operate

Circuit Verification

- How to make sure a circuit works correctly
- Functional verification
- Timing verification

Digital Design & Computer Arch.

Lecture 8: Timing and Verification

Prof. Onur Mutlu

ETH Zürich
Spring 2022
18 March 2022